

Package ‘GWnorm’

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Type Package

Title G-Wishart Normalising Constants for Gaussian Graphical Models

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Description Computes G-Wishart normalising constants through a Fourier approach. Either exact analytical results, numerical integration or Monte Carlo estimation are employed. Details at C. Wong, G. Moffa and J. Kuipers (2024), <[doi:10.48550/arXiv.2404.06803](https://doi.org/10.48550/arXiv.2404.06803)>. Also includes approximations of the ratio of normalising constants, see details at C. Wong, G. Moffa and J. Kuipers (2025), <[doi:10.48550/arXiv.2503.13046](https://doi.org/10.48550/arXiv.2503.13046)>.

License GPL (>= 2)

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annotate_cliques	<i>this helper function adds information to cliques related to the missing edges</i>
------------------	--

Description

this helper function adds information to cliques related to the missing edges

Usage

```
annotate_cliques(cliques, clique_flags, missing_edges, beta)
```

Arguments

cliques	list of cliques
clique_flags	indicator of whether the elements are cliques (TRUE) or separators (FALSE)
missing_edges	array of missing edges
beta	A constant > 0

Value

annotated list of cliques

check_prime_connected *This function just checks if a graph is connected and prime*

Description

This function just checks if a graph is connected and prime

Usage

```
check_prime_connected(graph, check_prime = TRUE)
```

Arguments

graph An igraph object
check_prime Boolean flag to check primality too (default TRUE)

Value

A boolean, TRUE if connected and prime

chordal_factor *Chordal Factor # do not export*

Description

Chordal Factor # do not export

Usage

```
chordal_factor(graph)
```

Arguments

graph An igraph object, a chordal graph

Value

A list of maximal cliques and separators

Clique_complete	<i>Clique-completion</i>
-----------------	--------------------------

Description

This function returns the completion of a matrix with respect to a graph. The entries of the given matrix are such that in the clique decomposition of the chordal completion there is no linear term in the determinant expansion.

Usage

```
Clique_complete(
  D,
  missing_edges,
  cliques,
  cliques_ann,
  prec_count = 0,
  tol = 1e-12
)
```

Arguments

D	A real symmetric positive definite p by p matrix
missing_edges	argument of edges to complete
cliques	list of cliques
cliques_ann	list of clique annotations
prec_count	Use Hessian after a this number of iterations (default is to always use)
tol	A tolerance to stop the numerical iterations

Value

A real symmetric positive definite p by p matrix

clique_update_D	<i>Newton-Raphson update for the clique-completion</i>
-----------------	--

Description

Newton-Raphson update for the clique-completion

Usage

```
clique_update_D(D, tau, cliques, cliques_ann, prec_flag = TRUE)
```

Arguments

D	A real symmetric positive definite p by p matrix
tau	number of missing edges
cliques	list of cliques
cliques_ann	list of clique annotations
prec_flag	whether to use the full Hessian

Value

the update step

C_GtoI_G	<i>This function returns the log of the G-Wishart normalising constant $I_G(\beta, D) = \int [S^p_{++}(G)] \det(K)^\beta \exp(-\text{tr}(KD)) dK$ from the transformed version $\log(C_G(\delta, D)) = \int [S^p_{++}(G)] \det(K)^{(\delta-2)/2} \exp(-\text{tr}(KD)/2) dK$</i>
----------	---

Description

This function returns the log of the G-Wishart normalising constant $I_G(\beta, D) = \int [S^p_{++}(G)] \det(K)^\beta \exp(-\text{tr}(KD)) dK$ from the transformed version $\log(C_G(\delta, D)) = \int [S^p_{++}(G)] \det(K)^{(\delta-2)/2} \exp(-\text{tr}(KD)/2) dK$

Usage

C_GtoI_G(graph, CGval, delta)

Arguments

graph	An igraph object, corresponding to a prime connected graph
CGval	A number $\log(C_G(\delta, D))$
delta	A constant > 0

Value

A number $\log(I_G(\beta, D))$

form_triangle	<i>Find triangle contains two missing edges # do not export</i>
---------------	---

Description

This function checks whether there is a triangle in the graph(graph2) contains at least two edges from the missing edges (graph1).

Usage

```
form_triangle(graph1, graph2)
```

Arguments

graph1	An igraph object, corresponding to the missing edges
graph2	An igraph object, corresponding to the super graph

Value

TRUE if there is such a triangle

Iss_cmat	<i>Isserlis complement matrix</i>
----------	-----------------------------------

Description

This function returns the Isserlis matrix (rows/columns arranged in some order) with respect to a matrix and a graph for the missing edges (complement of the graph).

Usage

```
Iss_cmat(M, graph)
```

Arguments

M	An p by p matrix
graph	An igraph object, corresponding to the graph

Value

An m by m matrix, where m is the number of missing edges in the graph

Examples

```
# example code
adj <- matrix(0, nrow = 5, ncol = 5)
adj[1,5] <- adj[1,2] <- adj[2,3] <- adj[3,4] <- adj[4,5] <- 1 # 5-cycle
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
Iss_cmat(matrix(1:25, nrow = 5, byrow = TRUE), graph)
```

Iss_mat

Isserlis matrix

Description

This function returns the Isserlis matrix (rows/columns arranged in some order) with respect to a matrix and a graph

Usage

```
Iss_mat(M, graph)
```

Arguments

M	An p by p matrix
graph	An igraph object, corresponding to the graph

Value

An m by m matrix, where m is the number of vertices and edges in the graph

Examples

```
# example code
adj <- matrix(0, nrow = 5, ncol = 5)
adj[1,5] <- adj[1,2] <- adj[2,3] <- adj[3,4] <- adj[4,5] <- 1 # 5-cycle
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
Iss_mat(matrix(1:25, nrow = 5, byrow = TRUE), graph)
```

`is_6_cycle`*Determine whether the graph is the cycle of length 6 or its complement*

Description

Input an igraph object, this function tells you whether graph is the cycle of length 6, or its complement.

Usage

```
is_6_cycle(graph)
```

Arguments

`graph` An igraph object

Value

An integer, 1 means the graph is the cycle of length 6, 2 means the the graph is the complement of the cycle of length 6, 0 means otherwise

Examples

```
# C6 example 5 1 3 2 4 6
is_6_cycle(igraph::make_graph(edges = c(1,3, 1,5, 2,3, 2,4, 5,6, 6,4),
  n = 6, directed = FALSE))
# C6 complement example
is_6_cycle(igraph::make_graph(edges = c(1,2, 1,4, 1,6, 2,5, 2,6, 3,4,
  3,5, 3,6, 4,5), n = 6, directed = FALSE))
# not C6 examples
is_6_cycle(igraph::make_graph(edges = c(1,3, 1,5, 2,3, 2,4, 5,6, 6,4),
  n = 7, directed = FALSE))
is_6_cycle(igraph::make_graph(edges = c(1,4, 1,5, 2,3, 2,4, 5,6, 6,4),
  n = 6, directed = FALSE))
```

`is_k_partite`*Determine whether the graph is complete k partite*

Description

Input an igraph object, this function tells you the size of the partition if the graph is a k partite graph.

Usage

```
is_k_partite(graph)
```

Arguments

graph An igraph object

Value

A vector of the size of the partition. The length of the vector is k. Empty vector means that the graph is not a complete k partite graph.

Examples

```
# not complete k-partite example
is_k_partite(igraph::make_graph(edges = c(1,2, 2,4, 2,5, 1,3, 3,5, 5,6, 6,7,
5,7, 4,7), n = 7, directed = FALSE))
# complete 4-partite example, (1,5), (2,4), (3,7), (6)
is_k_partite(igraph::make_graph(edges = c(1,2, 1,3, 1,4, 1,6, 1,7, 2,3, 2,5, 2,6,
2,7, 3,4, 3,5, 3,6, 4,5, 4,6, 4,7, 5,6, 5,7, 6,7), n = 7, directed = FALSE))
```

I_Gnorm

G Wishart normalising constant

Description

This function returns the log of transformed G-Wishart normalising constant $I_G(\beta, D) = \int [S^p_{++}(G)] \det(K)^\beta \exp(-\text{tr}(KD)) dK$ for graphs G. Graphs are decomposed into connected prime components. For each component if there is no explicit formula, or the integral cannot be reduced into one dimension, MC integration is used.

Usage

```
I_Gnorm(
  graph,
  beta,
  D,
  connected = FALSE,
  prime = FALSE,
  chordal = NULL,
  n_samp = 1000,
  nu = 10,
  robust = FALSE,
  quench_k = 0,
  err_flag = FALSE,
  useBDgraph = FALSE
)
```

Arguments

graph	An igraph object, corresponding to a prime connected graph
beta	A constant > 0
D	A p by p real symmetric positive definite matrix
connected	Whether the graph is connected, if known (default FALSE)
prime	Whether the graph is prime, if known (default FALSE)
chordal	Optional. An igraph object, corresponding to a chordal completion of graph
n_samp	number of sample points used in MC integration
nu	degree of freedom of the MC importance distribution (nu=0 is Gaussian)
robust	flag of whether to use robust means (default not to, but may offer numerical stability at the risk of bias)
quench_k	scaling factor of von Mises quenching (default value of 0 means not used, but value around 1 may offer numerical stability at the risk of bias)
err_flag	flag of whether to return the log relative error estimate (or not, default), only considered for prime connected graphs
useBDgraph	flag of whether to use BDgraph instead (or not, default), useful wrapper for comparisons

Value

A number $\log(I_G(\text{beta}, D))$

Examples

```
set.seed(42)
p <- 11
data <- matrix(runif(10*p), ncol = p)
D <- t(data) %% data
beta <- 1
graph <- igraph::make_graph(edges = c(1,2, 2,4, 2,5, 1,3, 3,5, # disconnected
                                     5,6, 6,7, 5,7, 4,7, # with prime decomposition too
                                     8,9, 8,11, 9,10, 10,11), n = 11, directed = FALSE)

I_Gnorm(graph, beta, D)
# compare with BDgraph
I_Gnorm(graph, beta, D, n_samp = 1e5, useBDgraph = TRUE)
```

I_GtoC_G

*This function returns the log of the G-Wishart normalising constant $\log(C_G(\text{delta}, D)) = \int [S^p_{++}(G)] \det(K)^{(\text{delta}-2)/2} * \exp(-\text{tr}(KD)/2) dK$ from the transformed version $I_G(\text{beta}, D) = \int [S^p_{++}(G)] \det(K)^\beta * \exp(-\text{tr}(KD)) dK$*

Description

This function returns the log of the G-Wishart normalising constant $\log(C_G(\delta, D)) = \int_{\mathcal{S}^p_{++}(G)} \det(K)^{((\delta-2)/2)} * \exp(-\text{tr}(KD)/2) dK$ from the transformed version $I_G(\beta, D) = \int_{\mathcal{S}^p_{++}(G)} \det(K)^\beta * \exp(-\text{tr}(KD)) dK$

Usage

```
I_GtoC_G(graph, IGval, beta)
```

Arguments

graph	An igraph object, corresponding to a prime connected graph
IGval	A number $\log(I_G(\beta, D))$
beta	A constant > 0

Value

A number $\log(C_G(\delta, D))$

I_G_BD	<i>This function is a wrapper for BDgraph to compare and to avoid the NOTE in the package checks since we only had BDgraph in the examples</i>
--------	--

Description

This function is a wrapper for BDgraph to compare and to avoid the NOTE in the package checks since we only had BDgraph in the examples

Usage

```
I_G_BD(graph, beta, D, n_samp = 1000, C_G_flag = FALSE)
```

Arguments

graph	An igraph object, corresponding to a prime connected graph
beta	A constant > 0
D	A p by p real symmetric positive definite matrix
n_samp	number of sample points used in MC integration
C_G_flag	boolean whether to return C_G instead of I_G

Value

A number $\log(I_G(\beta, D))$ [or $\log(C_G(\delta, D))$]

I_G_chordal

G Wishart normalising constant for chordal graphs**Description**

This function returns the log of transformed G-Wishart normalising constant $I_G(\beta, D) = \int_{S^p} \det(K)^\beta \exp(-\text{tr}(KD)) dK$ for chordal graphs G , using explicit formula (cliques / separators).

Usage

```
I_G_chordal(
  graph,
  beta,
  D = NULL,
  cliques = NULL,
  separators = NULL,
  ratio = FALSE
)
```

Arguments

graph	An igraph object, corresponding to a chordal graph
beta	A constant > 0
D	A p by p real symmetric positive definite matrix (default, NULL for identity matrix)
cliques	A list of cliques (if known)
separators	A list of separators (if known)
ratio	Whether to output just the ratio compared to the value with I (default FALSE)

Value

A number $\log(I_G(\beta, D))$

Examples

```
set.seed(42)
p <- 5
data <- matrix(runif(10*p), ncol = p)
D <- t(data) %*% data
beta <- 1
adj <- matrix(0, nrow = p, ncol = p)
adj[1,c(2:5)] <- adj[2,3] <- adj[3,4] <- adj[4,5] <- 1 # chordal completion of 5-cycle
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
I_G_chordal(graph, beta, D)
# compare with BDgraph gnorm()
I_G_BD(graph, beta, D, n_samp = 1e4)
```

I_G_complete	<i>G Wishart normalising constant for complete graphs</i>
--------------	---

Description

This function returns the log of the transformed G-Wishart normalising constant $I_G(\beta, D) = \int [S^p_{++}(G)] \det(K)^\beta \exp(-\text{tr}(KD)) dK$ for complete graphs G, using explicit formula $\det(D)^{-\beta-(p+1)/2} \Gamma_n(\beta+(p+1)/2)$

Usage

```
I_G_complete(p, beta, D = NULL, ratio = FALSE)
```

Arguments

p	A positive integer, indicating the number of vertices of the graph
beta	A constant > 0
D	A p by p real symmetric positive definite matrix (default, NULL, if for identity matrix)
ratio	Whether to output just the ratio compared to the value with I (default FALSE)

Value

A number $\log(I_G(\beta, D))$

Examples

```
set.seed(42)
p <- 6
data <- matrix(runif(10*p), ncol = p)
D <- t(data) %*% data
beta <- 1
I_G_complete(6, beta, D)
# compare with BDgraph gnorm()
adj <- matrix(1, nrow = 6, ncol = 6)
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
I_G_BD(graph, beta, D)
```

I_G_MC

G Wishart normalising constant through MC integration**Description**

This function returns the log of transformed G-Wishart normalising constant $I_G(\beta, D) = \int [S^p_{++}(G)] \det(K)^\beta \exp(-\text{tr}(KD)) dK$ for connected graphs G . If there is no explicit formula, or the integral cannot be reduced into lower dimensions, MC integration is used.

Usage

```
I_G_MC(
  graph,
  beta,
  D,
  n_samp = 1000,
  nu = 10,
  err_flag = FALSE,
  int1d = TRUE,
  robust = FALSE,
  quench_k = 0,
  chordal = NULL
)
```

Arguments

graph	An igraph object, corresponding to a prime connected graph
beta	A constant > 0
D	A p by p real symmetric positive definite matrix
n_samp	number of sample points used in MC integration
nu	degree of freedom of the MC importance distribution (nu=0 is Gaussian)
err_flag	flag of whether to return the log relative error estimate (or not, default)
int1d	flag of whether to integrate numerically in 1d (default, MC integration otherwise)
robust	flag of whether to use robust means (default not to, but may offer numerical stability at the risk of bias)
quench_k	scaling factor of von Mises quenching (default not used, value of 0, but value around 1 may offer numerical stability at the risk of bias)
chordal	Optional. An igraph object, corresponding to a chordal completion of graph

Value

A number $\log(I_G(\beta, D))$

Examples

```

set.seed(42)
p <- 5
data <- matrix(runif(10*p), ncol = p)
D <- t(data) %*% data
beta <- 1
adj <- matrix(0, nrow = p, ncol = p)
adj[1,5] <- adj[1,2] <- adj[2,3] <- adj[3,4] <- adj[4,5] <- 1 # 5-cycle
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
I_G_MC(graph, beta, D)
# compare with BDgraph gnorm()
I_G_BD(graph, beta, D, n_samp = 1e5)

```

I_G_ratio_approx	<i>G</i> Wishart normalising constant
------------------	---------------------------------------

Description

This function returns the approximation of the ratio of log transformed G-Wishart normalising constants $I_G(\beta, D) / I_G(\beta, I)$ for graphs G . Graphs are decomposed into connected prime components. For each component if there is no explicit formula, the approximation is used. Note that this is the same as the ratio $C_G(\delta, D) / C_G(\delta, I)$ with $\delta = 2*\beta + 2$

Usage

```

I_G_ratio_approx(
  graph,
  beta,
  D,
  connected = FALSE,
  prime = FALSE,
  chordal = NULL,
  use_comp = NULL
)

```

Arguments

graph	An igraph object, corresponding to a prime connected graph
beta	A constant > 0
D	A p by p real symmetric positive definite matrix
connected	Whether the graph is connected, if known (default FALSE)
prime	Whether the graph is prime, if known (default FALSE)
chordal	Optional. An igraph object, corresponding to a chordal completion of graph
use_comp	Whether to approximate using the graph (FALSE), the complement (TRUE) or the more efficient (default NULL)

Value

A number approximating $\log(I_G(\beta, D)) - \log(I_G(\beta, I))$

Examples

```
set.seed(42)
p <- 11
data <- matrix(runif(10*p), ncol = p)
D <- t(data) %*% data
beta <- 1
graph <- igraph::make_graph(edges = c(1,2, 2,4, 2,5, 1,3, 3,5, # disconnected
                                     5,6, 6,7, 5,7, 4,7, # with prime decomposition too
                                     8,9, 8,11, 9,10, 10,11), n = 11, directed = FALSE)

I_G_ratio_approx(graph, beta, D)
# compare with MC estimates
I_G_MC(graph, beta, D, n_samp = 1e5) - I_G_MC(graph, beta, diag(p), n_samp = 1e5)
```

I_G_ratio_approx_prime

This function returns the approximation of the ratio of log transformed G-Wishart normalising constants $I_G(\beta, D) / I_G(\beta, I)$ for connected prime graphs G . If there is no explicit formula, the approximation is used. Note that this is the same as the ratio $C_G(\delta, D) / C_G(\delta, I)$ with $\delta = 2\beta + 2$*

Description

This function returns the approximation of the ratio of log transformed G-Wishart normalising constants $I_G(\beta, D) / I_G(\beta, I)$ for connected prime graphs G . If there is no explicit formula, the approximation is used. Note that this is the same as the ratio $C_G(\delta, D) / C_G(\delta, I)$ with $\delta = 2*\beta + 2$

Usage

```
I_G_ratio_approx_prime(graph, beta, D, chordal = NULL, use_comp = NULL)
```

Arguments

graph	An igraph object, corresponding to a prime connected graph
beta	A constant > 0
D	A p by p real symmetric positive definite matrix
chordal	Optional. An igraph object, corresponding to a chordal completion of graph
use_comp	Whether to approximate using the graph (FALSE), the complement (TRUE) or the more efficient (default NULL)

Value

A number approximating $\log(I_G(\beta, D)) - \log(I_G(\beta, I))$

Examples

```
set.seed(42)
p <- 5
data <- matrix(runif(10*p), ncol = p)
D <- t(data) %*% data
beta <- 1
adj <- matrix(0, nrow = p, ncol = p)
adj[1,5] <- adj[1,2] <- adj[2,3] <- adj[3,4] <- adj[4,5] <- 1 # 5-cycle
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
I_G_ratio_approx_prime(graph, beta, D, use_comp = TRUE)
# compare with MC estimates
I_G_MC(graph, beta, D, n_samp = 1e5) - I_G_MC(graph, beta, diag(p), n_samp = 1e5)
```

I_G_special

G Wishart normalising constant for special cases

Description

This function returns the log of transformed *G*-Wishart normalising constant $I_G(\beta, I) = \int_{\mathcal{S}^p} \det(K)^\beta \exp(-\text{tr}(K)) dK$ for connected graphs *G* for special cases where there is an explicit formula, including involving a low-dimensional integral.

Usage

```
I_G_special(
  graph,
  beta,
  connected = FALSE,
  prime = FALSE,
  test_6_cycle = TRUE,
  test_k_partite = TRUE,
  chordal = NULL
)
```

Arguments

graph	An igraph object, corresponding to a prime connected graph
beta	A constant > 0
connected	Whether the graph is connected, if known (default FALSE)
prime	Whether the graph is prime, if known (default FALSE)
test_6_cycle	Flag whether to test whether the graph is a 6-cycle or its complement (default TRUE)
test_k_partite	Flag whether to test whether the graph is complete <i>k</i> partite (default TRUE)
chordal	Optional. An igraph object, corresponding to a chordal completion of graph

Value

A number $\log(I_G(\beta, I))$

Examples

```

beta <- 1
p <- 5
adj <- matrix(0, nrow = p, ncol = p)
adj[1,5] <- adj[1,2] <- adj[2,3] <- adj[3,4] <- adj[4,5] <- 1 # 5-cycle
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
I_G_special(graph, beta)
# compare with BDgraph gnorm()
I_G_BD(graph, beta, diag(p), n_samp = 1e5)
p <- 6
adj <- matrix(0, nrow = p, ncol = p)
adj[1,6] <- adj[1,2] <- adj[2,3] <- adj[3,4] <- adj[4,5] <- adj[5,6] <- 1 # 6-cycle
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
I_G_special(graph, beta)
# compare with BDgraph gnorm()
I_G_BD(graph, beta, diag(p), n_samp = 1e5)
graph <- igraph::complementer(graph) # complement of 6-cycle
I_G_special(graph, beta)
# compare with BDgraph gnorm()
I_G_BD(graph, beta, diag(p), n_samp = 1e5)
adj[upper.tri(adj)] <- 1
adj[2,3] <- adj[1,4] <- adj[5,6] <- 0 # complete graph with some edges missing
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
I_G_special(graph, beta)
# compare with BDgraph gnorm()
I_G_BD(graph, beta, diag(p), n_samp = 1e5)

```

local_mean_grad

Compute means and gradients for the Newton-Raphson update for the clique-completion

Description

Compute means and gradients for the Newton-Raphson update for the clique-completion

Usage

```
local_mean_grad(D, tau, cliques, cliques_ann, prec_flag = TRUE)
```

Arguments

D	A real symmetric positive definite p by p matrix
tau	number of missing edges
cliques	list of cliques
cliques_ann	list of clique annotations
prec_flag	compute the full Hessian

Value

the mean and gradient for the update step note this does not take into account the covariance/precision for numerical speed

local_precision	<i>Compute second moment of the log expansion of the determinant (assuming the mean is 0 from Clique_completion)</i>
-----------------	--

Description

Compute second moment of the log expansion of the determinant (assuming the mean is 0 from Clique_completion)

Usage

```
local_precision(D, tau, cliques, cliques_ann)
```

Arguments

D	A real symmetric positive definite p by p matrix
tau	number of missing edges
cliques	list of cliques
cliques_ann	list of clique annotations

Value

the precision matrix

PD_complete	<i>PD-completion</i>
-------------	----------------------

Description

This function returns the PD-completion of a matrix with respect to a graph. The entries of the given matrix corresponding to the missing edges are modified such that the inverse has zeros in the places of missing edges.

Usage

```
PD_complete(graph, D, missing_edges = NULL, tol = 1e-12)
```

Arguments

graph	An igraph object, corresponding to the graph
D	A real symmetric positive definite p by p matrix
missing_edges	optional argument of edges to complete
tol	A tolerance to stop the numerical iterations

Value

A real symmetric positive definite p by p matrix

Examples

```
set.seed(42)
p <- 5
data <- matrix(runif(10*p), ncol = p)
D <- t(data) %*% data
adj <- matrix(0, nrow = p, ncol = p)
adj[1,5] <- adj[1,2] <- adj[2,3] <- adj[3,4] <- adj[4,5] <- 1 # 5-cycle
graph <- igraph::graph_from_adjacency_matrix(adj, mode = c("max"))
(D_tilde <- PD_complete(graph, D))
(round(solve(D_tilde), 6)) # has zeros at the missing edges
```

predict_row	<i>Predict Row # do not export</i>
-------------	------------------------------------

Description

Predict Row # do not export

Usage

```
predict_row(i, j, D)
```

Arguments

i	A number, the row to predict
j	A vector, the columns to predicted
D	A real symmetric positive definite matrix

Value

the predicted values for the vector j

`prime_decomp`*Prime Decomposition*

Description

This function returns the prime components and the minimal separators of a connected graph.

Usage

```
prime_decomp(graph)
```

Arguments

`graph` An igraph object, a connected graph

Value

A list of the prime components and the separators

Examples

```
graph <- igraph::make_graph(edges = c(1,2, 2,4, 2,5, 1,3, 3,5,  
  5,6, 6,7, 5,7, 4,7), n = 7, directed = FALSE)  
prime_decomp(graph)
```

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