

# Package ‘MultiLevelOptimalBayes’

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**Type** Package

**Title** Regularized Bayesian Estimator for Two-Level Latent Variable Models

**Version** 0.0.4.0

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**Description** Implements a regularized Bayesian estimator that optimizes the estimation of between-group coefficients for multilevel latent variable models by minimizing mean squared error (MSE) and balancing variance and bias. The package provides more reliable estimates in scenarios with limited data, offering a robust solution for accurate parameter estimation in two-level latent variable models. It is designed for researchers in psychology, education, and related fields who face challenges in estimating between-group effects under small sample sizes and low intraclass correlation coefficients. The package includes comprehensive S3 methods for result objects: `print()`, `summary()`, `coef()`, `se()`, `vcov()`, `confint()`, `as.data.frame()`, `dim()`, `length()`, `names()`, and `update()` for enhanced usability and integration with standard R workflows. Dashuk et al. (2025a) <[doi:10.1017/psy.2025.10045](https://doi.org/10.1017/psy.2025.10045)> derived the optimal regularized Bayesian estimator; Dashuk et al. (2025b) <[doi:10.1007/s41237-025-00264-7](https://doi.org/10.1007/s41237-025-00264-7)> extended it to the multivariate case; and Luedtke et al. (2008) <[doi:10.1037/a0012869](https://doi.org/10.1037/a0012869)> formalized the two-level latent variable framework.

**Imports** pracma

**License** GPL-3

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as.data.frame.mlob\_result  
*Convert mlob\_result to data frame*

---

## Description

Convert mlob\_result to data frame

## Usage

```
## S3 method for class 'mlob_result'
as.data.frame(x, ...)
```

## Arguments

x                    An object of class mlob\_result  
 ...                  Additional arguments passed to as.data.frame

## Value

A data frame representation of the results

---

coef.mlob\_result      *Extract coefficients from mlob\_result objects*

---

**Description**

Extract coefficients from mlob\_result objects

**Usage**

```
## S3 method for class 'mlob_result'  
coef(object, ...)
```

**Arguments**

object      An object of class mlob\_result  
...      Additional arguments passed to coef

**Value**

A data frame with coefficients

---

confint.mlob\_result      *Extract confidence intervals from mlob\_result objects*

---

**Description**

Extract confidence intervals from mlob\_result objects

**Usage**

```
## S3 method for class 'mlob_result'  
confint(object, parm, level = 0.95, ...)
```

**Arguments**

object      An object of class mlob\_result  
parm      Parameters for which to extract confidence intervals  
level      Confidence level (can be different from the model's default)  
...      Additional arguments passed to confint

**Value**

A matrix with confidence intervals

---

dim.mlob\_result      *Get dimensions of mlob\_result objects*

---

**Description**

Get dimensions of mlob\_result objects

**Usage**

```
## S3 method for class 'mlob_result'  
dim(x)
```

**Arguments**

x                      An object of class mlob\_result

**Value**

A vector with dimensions

---

length.mlob\_result      *Get length of mlob\_result objects*

---

**Description**

Get length of mlob\_result objects

**Usage**

```
## S3 method for class 'mlob_result'  
length(x)
```

**Arguments**

x                      An object of class mlob\_result

**Value**

The number of parameters/coefficients

## Description

Implements a regularized Bayesian approach that optimizes the estimation of between-group coefficients by minimizing Mean Squared Error (MSE), balancing both variance and bias. This method provides more reliable estimates in scenarios with limited data, offering a robust solution for accurate parameter estimation in multilevel models. The package is designed for researchers in psychology, education, and related fields who face challenges in estimating between-group effects in two-level latent variable models, particularly in scenarios with small sample sizes and low intraclass correlation coefficients.

## Usage

```
mlob(  
  formula,  
  data,  
  group,  
  balancing.limit = 0.2,  
  conf.level = 0.95,  
  jackknife = FALSE,  
  punish.coeff = 2,  
  ...  
)
```

## Arguments

formula	an object of class " <a href="#">formula</a> " (or one that can be coerced to that class): a symbolic description of the model to be fitted. Formula specifies the model (e.g., $Y \sim X + C \dots$ ), where Y is the dependent variable, X is the context variable, which is the focus of most applications of the model (always included), and C includes all additional covariates.
data	a data frame (or object converted by <a href="#">as.data.frame</a> to a data frame) containing the variables referenced in the formula. All variables used in the model, including the dependent variable, context variable, covariates, and grouping variable must be present in this data frame.
group	a name of the variable that defines the affiliation of an individual (row) to the specific group.
balancing.limit	a number that represents the threshold of the maximum relative part of the dataset that can be deleted to balance the data. Defaults to 0.2
conf.level	a numeric value representing the confidence level used to calculate confidence intervals for the estimators. Defaults to 0.95, corresponding to a 95% confidence level.

jackknife	logical variable. If TRUE, the jackknife re-sampling method will be applied to calculate the standard error of the between-group and its confidence interval coefficient. Defaults to FALSE.
punish.coeff	a multiplier that punishes the balancing procedure when deleting the whole group. If punish.coeff is equal to 1, no additional punishment is applied for deleting the group. Higher values intensify the penalty. Defaults to 2.
...	additional arguments passed to the function.

## Details

This function also verifies whether the data is balanced (i.e., whether each group contains the same number of individuals). If the data is unbalanced, the balancing procedure comes into effect, and identifies the optimal number of items and groups to delete based on the punishment coefficient. If the amount of data deleted is more than defined by threshold (`balancing.limit`) then results should be interpreted with caution.

The `summary()` function produces output similar to:

Summary of Coefficients:

	Estimate	Std. Error	Lower CI (99			
beta_b	0.4279681	0.7544766	-1.5154349	2.371371	0.5672384	0.57055223
gamma_Petal.Length	0.4679522	0.2582579	-0.1972762	1.133181	1.8119567	0.06999289

For comparison, summary of coefficients from unoptimized analysis (ML):

	Estimate	Std. Error	Lower CI (99			
beta_b	0.6027440	5.424780e+15	-1.397331e+16	1.397331e+16	1.111094e-16	1.00000000
gamma_Petal.Length	0.4679522	2.582579e-01	-1.972762e-01	1.133181e+00	1.811957e+00	0.06999289

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

## Value

A list containing the results of the regularized Bayesian estimation, which includes the model formula, dependent and context variables, and other relevant details from the analysis. The returned object is of class `mlob_result`.

## Methods

The returned object supports the following S3 methods:

- `print(x)` - Display coefficients, standard errors, confidence intervals, Z-values, and p-values
- `summary(x)` - Comprehensive summary with significance stars and comparison to unoptimized ML
- `coef(x)` - Extract coefficients as a data frame
- `se(x)` - Extract standard errors
- `vcov(x)` - Extract variance-covariance matrix (diagonal only)
- `confint(x, parm, level)` - Extract confidence intervals for specified parameters
- `as.data.frame(x)` - Convert results to a data frame format

- `dim(x)` - Return dimensions (number of parameters)
- `length(x)` - Return number of parameters
- `names(x)` - Return parameter names
- `update(x, formula, data, conf.level, balancing.limit, punish.coeff, jackknife)`  
- Update model with new parameters

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### References

- Dashuk, V., Hecht, M., Luedtke, O., Robitzsch, A., & Zitzmann, S. (2025a). [doi:10.1017/psy.2025.10045](https://doi.org/10.1017/psy.2025.10045)
- Dashuk, V., Hecht, M., Luedtke, O., Robitzsch, A., & Zitzmann, S. (2025b). [doi:10.1007/s41237-025002647](https://doi.org/10.1007/s41237-025002647)
- Luedtke, O., Marsh, H. W., Robitzsch, A., Trautwein, U., Asparouhov, T., & Muthen, B. (2008). [doi:10.1037/a0012869](https://doi.org/10.1037/a0012869)

### Examples

```
# Example 1: usage with the iris dataset

result_iris <- mlob(
  Sepal.Length ~ Sepal.Width + Petal.Length,
  data = iris, group = 'Species',
  conf.level = 0.01,
  jackknife = FALSE)

# View summary statistics (similar to summary of a linear model);

summary(result_iris)

# Example 2: usage with highly unbalanced mtcars dataset (adjusted balancing.limit)

result_mtcars <- mlob(
  mpg ~ hp + wt + am + hp:wt + hp:am,
  data = mtcars, group = 'cyl',
  balancing.limit = 0.35)

# View summary statistics

summary(result_mtcars)

#' # Example 3: Using all available S3 methods on slightly unbalanced ChickWeight dataset

result <- mlob(weight ~ Time, data = ChickWeight, group = 'Diet', jackknife = FALSE)

# Display methods
print(result) # Display results
```

```
summary(result)          # Comprehensive summary
coef(result)             # Extract coefficients
se(result)              # Extract standard errors
vcov(result)            # Extract variance-covariance matrix
confint(result)         # Extract confidence intervals
confint(result, "beta_b") # Extract CI for specific parameter
confint(result, level = 0.99) # Extract CI with different confidence level
as.data.frame(result)   # Convert to data frame
dim(result)             # Get dimensions
length(result)         # Get number of parameters
names(result)          # Get parameter names

# Update model with new parameters
update(result, conf.level = 0.99)

# List all available methods
methods(class = "mlob_result")
```

---

names.mlob\_result      *Get names of mlob\_result objects*

---

## Description

Get names of mlob\_result objects

## Usage

```
## S3 method for class 'mlob_result'
names(x)
```

## Arguments

x                      An object of class mlob\_result

## Value

The names of the parameters/coefficients

---

se	<i>Generic function to extract standard errors</i>
----	--

---

**Description**

Generic function to extract standard errors

**Usage**

```
se(object, ...)
```

**Arguments**

object	An object
...	Additional arguments

---

se.mlob_result	<i>Extract standard errors from mlob_result objects</i>
----------------	---

---

**Description**

Extract standard errors from mlob\_result objects

**Usage**

```
## S3 method for class 'mlob_result'  
se(object, ...)
```

**Arguments**

object	An object of class mlob_result
...	Additional arguments passed to se

**Value**

A named vector of standard errors

---

summary.mlob\_result    *Summary method for mlob\_result objects*

---

### Description

Summary method for mlob\_result objects

### Usage

```
## S3 method for class 'mlob_result'  
summary(object, ...)
```

### Arguments

object	An object of class mlob_result
...	Additional arguments passed to summary

---

update.mlob\_result    *Update mlob\_result objects*

---

### Description

Update mlob\_result objects

### Usage

```
## S3 method for class 'mlob_result'  
update(  
  object,  
  formula = NULL,  
  data = NULL,  
  group = NULL,  
  balancing.limit = NULL,  
  conf.level = NULL,  
  jackknife = NULL,  
  punish.coeff = NULL,  
  ...  
)
```

**Arguments**

object	An object of class mlob_result
formula	Updated formula
data	Updated data
group	Updated group variable
balancing.limit	Updated balancing limit (default: 0.2)
conf.level	Updated confidence level (default: 0.95)
jackknife	Updated jackknife setting (default: FALSE)
punish.coeff	Updated punishment coefficient (default: 2)
...	Additional arguments passed to mlob

**Value**

Updated mlob\_result object

---

vcov.mlob\_result      *Extract variances from mlob\_result objects*

---

**Description**

Extract variances from mlob\_result objects

**Usage**

```
## S3 method for class 'mlob_result'
vcov(object, ...)
```

**Arguments**

object	An object of class mlob_result
...	Additional arguments passed to vcov

**Value**

A named vector of variances (squared standard errors)

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