

# Package ‘Rfast’

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**Type** Package

**Title** A Collection of Efficient and Extremely Fast R Functions

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**Suggests** philentropy

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**URL** <https://github.com/RfastOfficial/Rfast>

**Description** A collection of fast (utility) functions for data analysis. Column and row wise means, medians, variances, minimums, maximums, many t, F and G-square tests, many regressions (normal, logistic, Poisson), are some of the many fast functions. References: a) Tsagris M., Papadakis M. (2018). Taking R to its limits: 70+ tips. PeerJ Preprints 6:e26605v1 <[doi:10.7287/peerj.preprints.26605v1](https://doi.org/10.7287/peerj.preprints.26605v1)>. b) Tsagris M. and Papadakis M. (2018). Forward regression in R: from the extreme slow to the extreme fast. Journal of Data Science, 16(4): 771–780. <[doi:10.6339/JDS.201810\\_16\(4\).00006](https://doi.org/10.6339/JDS.201810_16(4).00006)>. c) Chatzipantsiou C., Dimitriadis M., Papadakis M. and Tsagris M. (2020). Extremely Efficient Permutation and Bootstrap Hypothesis Tests Using Hypothesis Tests Using R. Journal of Modern Applied Statistical Methods, 18(2), eP2898. <[doi:10.48550/arXiv.1806.10947](https://doi.org/10.48550/arXiv.1806.10947)>. d) Tsagris M., Papadakis M., Alenazi A. and Alzeley O. (2024). Computationally Efficient Outlier Detection for High-Dimensional Data Using the MDP Algorithm. Computation, 12(9): 185. <[doi:10.3390/computation12090185](https://doi.org/10.3390/computation12090185)>. e) Tsagris M. and Papadakis M. (2025). Fast and light-weight energy statistics using the R package Rfast. <[doi:10.48550/arXiv.2501.02849](https://doi.org/10.48550/arXiv.2501.02849)>.

**License** GPL (>= 2.0)

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## Description

A collection of fast (utility) functions for data analysis. Column and row wise means, medians, variances, minimums, maximums, many t, F and G-square tests, many regressions (normal, logistic, Poisson), are some of the many fast functions. References: a) Tsagris M., Papadakis M. (2018). Taking R to its limits: 70+ tips. PeerJ Preprints 6:e26605v1 <doi:10.7287/peerj.preprints.26605v1>. b) Tsagris M. and Papadakis M. (2018). Forward regression in R: from the extreme slow to the extreme fast. Journal of Data Science, 16(4): 771–780. <doi:10.6339/JDS.201810\_16(4).00006>. c) Chatzipantsiou C., Dimitriadis M., Papadakis M. and Tsagris M. (2020). Extremely Efficient Permutation and Bootstrap Hypothesis Tests Using Hypothesis Tests Using R. Journal of Modern Applied Statistical Methods, 18(2), eP2898. <doi:10.48550/arXiv.1806.10947>. d) Tsagris M., Papadakis M., Alenazi A. and Alzeley O. (2024). Computationally Efficient Outlier Detection for High-Dimensional Data Using the MDP Algorithm. Computation, 12(9): 185. <doi:10.3390/computation12090185>. e) Tsagris M. and Papadakis M. (2025). Fast and light-weight energy statistics using the R package Rfast. <doi:10.48550/arXiv.2501.02849>.

## Details

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## Maintainers

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## Note

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---

All k possible combinations from n elements

*All k possible combinations from n elements*

---

**Description**

All k possible combinations from n elements.

**Usage**

```
comb_n(n, k, simplify=TRUE)
```

**Arguments**

n	A positive <b>INTEGER</b> number or a vector with numbers.
k	A positive integer number at most equal to n or at most equal to the length of n, if n is a vector.
simplify	A logical value for return List instead of matrix.

**Value**

A matrix with k columns and rows equal to the number of possible unique combinations of n with k elements. If simplify is set to TRUE then a list with k values where each value has length equal to the number of possible unique combinations of n with k elements.

**Author(s)**

Manos Papadakis and Marios Dimitriadis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com> and Marios Dimitriadis <kmdimitriadis@gmail.com>.

**References**

Nijenhuis A. and Wilf H.S. (1978). Combinatorial Algorithms for Computers and Calculators. Academic Press, NY.

**See Also**

[nth](#), [colMaxs](#), [colMins](#), [colrange](#)

**Examples**

```
comb_n(20, 4)
combn(20, 4)
x <- rnorm(5)
res<-comb_n(x, 3)
```

---

Analysis of covariance

*Analysis of covariance*

---

**Description**

Analysis of covariance

**Usage**

```
ancova1(y, ina, x, logged = FALSE)
```

**Arguments**

y	A numerical vector with the data, the response variable.
ina	A numerical vector with 1s, 2s, 3s and so on indicating the two groups. Be careful, the function is designed to accept numbers greater than zero.
x	A numerical vector whose length is equal to the number of rows of y. This is the covariate.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

Analysis of covariance is performed. No interaction between the factor and the covariate is tested. Only the main effects. The design need not be balanced. The values of ina need not have the same frequency. The sums of squares have been adjusted to accept balanced and unbalanced designs.

**Value**

A matrix with the test statistic and the p-value for the factor variable and the covariate.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

D.C. Montgomery (2001). Design and analysis of experiments (5th Edition). New York: John Wiley & Sons

**See Also**

[ancovas](#), [ftests](#), [ttests](#), [anova1](#)

**Examples**

```
y <- rnorm(90)
ina <- rbinom(90, 2, 0.5) + 1
x <- rnorm(90)
a <- ancova1(y, ina, x)
```

---

Analysis of variance with a count variable  
*Analysis of variance with a count variable*

---

## Description

Analysis of variance with a count variable.

## Usage

```
poisson.anova(y, ina, logged = FALSE)
geom.anova(y, ina, type = 1, logged = FALSE)
quasipoisson.anova(y, ina, logged = FALSE)
```

## Arguments

<code>y</code>	A numerical vector with discrete valued data, i.e. counts.
<code>ina</code>	A numerical vector with discrete numbers starting from 1, i.e. 1, 2, 3, 4,... or a factor variable. This is suppose to be a categorical predictor. If you supply a continuous valued vector the function will obviously provide wrong results.
<code>type</code>	This argument is for the geometric distribution. Type 1 refers to the case where the minimum is zero and type 2 for the case of the minimum being 1.
<code>logged</code>	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

## Details

This is the analysis of variance with Poisson or geometric distributed data. What we do is a log-likelihood ratio test. However, this is exactly the same as Poisson regression with a single predictor variable who happens to be categorical. Needless to say that this is faster function than the `glm` command in R. For the same purpose with a Bernoulli variable use `g2Test`. The `quasipoisson.anova` is when in the `glm` function you specify `family = quasipoisson`. This is suitable for the case of over or under-dispersed data.

## Value

A vector with two values, the difference in the deviances (or the scale difference in the case of quasi poisson) and the relevant p-value. The `quasipoisson.anova` also returns the estimate of the  $\phi$  parameter.

## Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[logistic.cat1](#), [g2Test](#), [poisson.anovas](#), [anova](#), [poisson\\_only](#), [poisson.mle](#)

**Examples**

```
y <- rpois(300, 10)
ina <- rbinom(300, 3, 0.5) + 1
a1 <- poisson.anova(y, ina)
a2 <- glm(y ~ ina, poisson)
```

```
res<-anova(a2, test = "Chisq")
```

```
y <- rgeom(300, 0.7)
res<-geom.anova(y, ina)
```

---

Angular central Gaussian random values simulation

*Angular central Gaussian random values simulation*

---

**Description**

Angular central Gaussian random values simulation.

**Usage**

```
racg(n, sigma, seed = NULL)
```

**Arguments**

n	The sample size, a numerical value.
sigma	The covariance matrix in $R^d$ .
seed	If you want the same to be generated again use a seed for the generator, an integer number.

**Details**

The algorithm uses univariate normal random values and transforms them to multivariate via a spectral decomposition. The vectors are then scaled to have unit length.

**Value**

A matrix with the simulated data.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Tyler D. E. (1987). Statistical analysis for the angular central Gaussian distribution on the sphere. *Biometrika* 74(3): 579-589.

**See Also**

[acg.mle](#), [rmvnorm](#), [rmvlaplace](#), [rmvt](#)

**Examples**

```
s <- cov( iris[, 1:4] )
#x <- racg(100, s)
#res<-acg.mle(x)
#res<-vmf.mle(x) ## the concentration parameter, kappa, is very low, close to zero, as expected.
```

---

ANOVA for two quasi Poisson regression models

*ANOVA for two quasi Poisson regression models*

---

**Description**

ANOVA for two quasi Poisson regression models.

**Usage**

```
anova_quasipois.reg(mod0, mod1, n)
```

**Arguments**

mod0	An object as returned by the "qpois.reg" function. This is the null model.
mod1	An object as returned by the "qpois.reg" function. This is the alternative model.
n	The sample size. This is necessary to calculate the degrees of freedom.

**Details**

This is an ANOVA type significance testing for two quasi Poisson models.

**Value**

A vector with 4 elements, the test statistic value, its associated p-value and the relevant degrees of freedom of the numerator and the denominator.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Papke L. E. & Wooldridge J. (1996). Econometric methods for fractional response variables with an application to 401(K) plan participation rates. *Journal of Applied Econometrics*, 11(6): 619–632.

McCullagh, Peter, and John A. Nelder. *Generalized linear models*. CRC press, USA, 2nd edition, 1989.

**See Also**

[anova\\_qpois.reg](#), [qpois.reg](#), [univglms](#), [quasipoisson.anova](#)

**Examples**

```
y <- rbinom(200, 10, 0.5)
x <- matrix(rnorm(200 * 3), ncol = 3)
a1 <- qpois.reg(x, y)
a0 <- qpois.reg(x[, 1], y)
res<-anova_quasipois.reg(a0, a1, 200)
b1 <- glm(y ~ x, family = quasipoisson)
b0 <- glm(y ~ x[, 1], family = quasipoisson)
res<-anova(b0, b1, test = "F")
c1 <- glm(y ~ x, family = poisson)
c0 <- glm(y ~ x[, 1], family = poisson)
res<-anova(c0, c1, test = "Chisq")
```

---

Apply method to Positive and Negative number

*Apply method to Positive and Negative number*

---

**Description**

Apply method to Positive and Negative number.

**Usage**

```
negative(x,method = "min")
positive(x,method = "min")
positive.negative(x,method = "min")
```

**Arguments**

x	A numerical vector with data.
method	Accept 3 values. "min", "max", "min.max".

**Details**

These functions apply the chosen method to the chosen subset (negative, positive, or both) from the vector and return the result.

**Value**

negative: apply the chosen method to every negative number of the input vector. positive: apply the chosen method to every positive number of the input vector. positive.negative: apply the chosen method to every negative and positive number of the input vector.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[nth](#), [colNth](#), [rownth](#), [sort\\_unique](#), [Round](#)

**Examples**

```
x <- rnorm(1000)

identical(negative(x, "min"), min(x<0))
identical(positive(x, "min"), min(x>0))
identical(positive.negative(x, "min"), c(min(x<0), min(x>0)))

x<-NULL
```

---

Apply to each column a method under condition

*Apply to each column a method under condition*

---

**Description**

Apply to each column a method under condition.

**Usage**

```
apply.condition(x, method = "+", oper = ">", cond.val = 0)
```

**Arguments**

x	An integer matrix.
method	One of: "+", "-", "*", "min", "max".
oper	One of: ">", "<", ">=", "<=".
cond.val	An integer value for the condition.

**Details**

Apply to each col the specified method using the condition.

**Value**

An integer vector with the corresponding values.

**Author(s)**

Manos Papadakis and Michail Tsagris

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

**See Also**

[colsums](#), [colMedians](#), [colVars](#)

**Examples**

```
x <- matrix(rpois(100,6),10, 10)
identical(apply(x,2,function(x){ sum(x[x>0]) }), apply.condition(x,"+", ">", 0))
x<-NULL
```

---

Backward selection regression

*Backward selection regression*

---

**Description**

Backward selection regression.

**Usage**

```
bs.reg(y, x, alpha = 0.05, type = "logistic")
```

**Arguments**

y	A numerical vector with the response variable values. It can either be of 0 and 1 values (Logistic regression) or of integer values 0, 1, 2,... (Poisson regression).
x	A numerical matrix with the candidate variables.
alpha	Threshold (suitable values are in [0,1]) for assessing the significance of p-values. The default value is at 0.05.
type	For the Logistic regression put "logistic" (default value) and for Poisson type "poisson".

**Details**

This function currently implements only the binary Logistic and Poisson regressions. If the sample size is less than the number of variables a notification message will appear and no backward regression will be performed.

**Value**

The output of the algorithm is an S3 object including:

info	A matrix with the non selected variables and their latest test statistics and p-values.
Vars	A vector with the selected variables.

**Author(s)**

Marios Dimitriadis

R implementation and documentation: Marios Dimitriadis <mtsagris@csd.uoc.gr>

**See Also**

[fs.reg](#), [univglms](#), [cor.fsreg](#)

**Examples**

```
y <- rbinom(50, 1, 0.5)
x <- matnorm(50, 10)
res<-bs.reg(y, x)
```

---

BIC (using partial correlation) forward regression  
*BIC (using partial correlation) forward regression*

---

**Description**

BIC (using partial correlation) forward regression.

**Usage**

```
bic.corfsreg(y, x, tol = 2)
```

**Arguments**

y	A numerical vector.
x	A matrix with data, the predictor variables.
tol	If the BIC difference between two successive models is less than the tolerance value, the variable will not enter the model.

**Details**

The forward regression tries one by one the variables using the F-test, basically partial F-test every time for the latest variable. This is the same as testing the significance of the coefficient of this latest entered variable. Alternatively the correlation can be used and in this case the partial correlation coefficient. There is a direct relationship between the t-test statistic and the partial correlation coefficient. Now, instead of having to calculate the test statistic, we calculate the partial correlation coefficient. The largest partial correlation indicates the candidate variable to enter the model. If the BIC of the regression model with that variable included, reduces, less than "tol" from the previous model without this variable, the variable enters.

**Value**

A matrix with two columns, the index of the selected variable(s) and the BIC of each model. The first line is always 0 and the BIC of the model with no predictor variables.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Draper, N.R. and Smith H. (1988). Applied regression analysis. New York, Wiley, 3rd edition.

**See Also**

[cor.fsreg](#), [score.glms](#), [univglms](#), [logistic\\_only](#), [poisson\\_only](#), [regression](#)

**Examples**

```
x <- matnorm( 50, 10 )
y <- rnorm(50)
a1 <- bic.corfsreg(y, x)
a2 <- cor.fsreg(y, x)
x <- NULL
```

---

BIC forward regression with generalised linear models

*BIC forward regression with generalised linear models*

---

**Description**

BIC forward regression with generalised linear models.

**Usage**

```
bic.fs.reg(y, x, tol = 2, type = "logistic")
```

**Arguments**

y	A numerical vector.
x	A matrix with data, the predictor variables.
tol	If the BIC difference between two successive models is less than the tolerance value, the variable will not enter the model.
type	If you have a binary dependent variable, put "logistic". If you have count data, put "poisson".

**Details**

The forward regression tries one by one the variables using the BIC at each step for the latest variable. If the BIC of the regression model with that variable included, is less than "tol" from the previous model without this variable, the variable enters.

**Value**

A matrix with two columns, the index of the selected variable(s) and the BIC of each model.

**Author(s)**

Marios Dimitriadis

R implementation and documentation: Marios Dimitriadis <kmdimitriadis@gmail.com>.

**References**

Draper, N.R. and Smith H. (1988). Applied regression analysis. New York, Wiley, 3rd edition.

**See Also**

[fs.reg](#), [bic.corfsreg](#), [cor.fsreg](#), [score.glm](#)s, [univglm](#)s, [logistic\\_only](#), [poisson\\_only](#), [regression](#)

**Examples**

```
x <- matrix(rnorm(200 * 50), ncol = 50)
## 200 variables, hence 200 univariate regressions are to be fitted
y <- rbinom(200, 1, 0.5)
a <- bic.fs.reg(y, x)
x <- NULL
```

---

Binary search algorithm

*Binary search algorithm*

---

### Description

Search a value in an ordered vector.

### Usage

```
binary_search(x, v, index=FALSE)
```

### Arguments

x	A vector with the data.
v	A value to check if exists in the vector x.
index	A boolean value for choose to return the position inside the vector.

### Details

The functions is written in C++ in order to be as fast as possible.

### Value

Search if the v exists in x. Then returns TRUE/FALSE if the value is been found.

### Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

### See Also

[is\\_element](#)

### Examples

```
x <- sort(rnorm(1000))
v <- x[50]
b <- binary_search(x,v)
b1 <- binary_search(x,v,TRUE)
```

---

Binomial coefficient and its logarithm

*Binomial coefficient and its logarithm*

---

## Description

Binomial coefficient and its logarithm.

## Usage

```
Lchoose(x, k)
Choose(x, k)
```

## Arguments

x	A vector with integer values numbers.
k	A positive non zero at most equal to x.

## Details

The binomial coefficient or its logarithm are evaluated.

## Value

A vector with the answers.

## Author(s)

Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

## See Also

[comb\\_n](#), [Lbeta](#), [Lgamma](#)

## Examples

```
x <- sample(20:30, 100, replace = TRUE)
res<-Choose(x, 4)
res<-Lchoose(x, 4)

x<-NULL
```

---

Bootstrap t-test for 2 independent samples

*Bootstrap t-test for 2 independent samples*

---

### Description

Bootstrap t-test for 2 independent samples.

### Usage

```
boot.ttest2(x, y, B = 999)
```

### Arguments

x	A numerical vector with the data.
y	A numerical vector with the data.
B	The number of bootstrap samples to use.

### Details

Instead of sampling B times from each sample, we sample  $\sqrt{B}$  from each of them and then take all pairs. Each bootstrap sample is independent of each other, hence there is no violation of the theory.

### Value

A vector with the test statistic and the bootstrap p-value.

### Author(s)

Michail Tsagris and Christina Chatzipantsiou

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Christina Chatzipantsiou <chatzipantsiou@gmail.com>.

### References

B.L. Welch (1951). On the comparison of several mean values: an alternative approach. *Biometrika*, 38(3/4), 330-336.

Efron Bradley and Robert J. Tibshirani (1993). *An introduction to the bootstrap*. New York: Chapman & Hall/CRC.

Chatzipantsiou C., Dimitriadis M., Papadakis M. and Tsagris M. (2019). Extremely efficient permutation and bootstrap hypothesis tests using R. To appear in the *Journal of Modern Applied Statistical Methods*.

<https://arxiv.org/ftp/arxiv/papers/1806/1806.10947.pdf>

### See Also

[ttest2](#), [exact.ttest2](#), [ftest](#)

**Examples**

```
tic <- proc.time()
x <- rexp(40, 4)
y <- rbeta(50, 2.5, 7.5)
a <- boot.ttest2(x, y, 9999)
a
```

---

Check if any column or row is fill with values

*Check if any column or row is fill with values*

---

**Description**

Check if any column or row is fill with values.

**Usage**

```
colrow.value(x,value=0)
```

**Arguments**

x	A vector with data.
value	A value to check.

**Details**

Check all the column if any has all its elements equal to argument value. If found, return "TRUE". Otherwise continues with rows. If columns and rows hasn't any value vector then return "FALSE". Even if it returns "FALSE" that doesn't mean the determinant can't be value. It might be but if check before and found any value vector then for sure the determinant it'll be value.

**Value**

A boolean value, "TRUE" if any column OR row is all filled with value. "FALSE" otherwise.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[rowMins](#), [rowFalse](#), [nth](#), [colrange](#), [colMedians](#), [colVars](#), [colSort](#), [rowSort](#), [rowTrue](#)

**Examples**

```
x <- matrix(runif(10*10),10,10)
res<-colrow.value(x)

x<-NULL
```

---

Check if values are integers and convert to integer  
*Check if values are integers and convert to integer*

---

**Description**

Check if values are integers and convert to integer.

**Usage**

```
is_integer(x)
as_integer(x,result.sort = TRUE,init = 1, parallel = FALSE)
```

**Arguments**

x	is_integer: A vector with numeric data. as_integer: A vector with data.
result.sort	A logical value for sorting the result.
init	An integer value to start.
parallel	Run the algorithm in parallel.

**Details**

The behavior of these functions are different than R's built in.

is\_integer: check if all the values are integers in memory. If typeof is double, and the values are integers in range  $-2^{31} : 2^{31}$  then it is better to convert to integer vector for using less memory. Also you can decrease the time complexity.

as\_integer: converts the discrete values to integers.

**Value**

is\_integer: A logical value, TRUE if all values are integers and in range  $-2^{31} : 2^{31}$ . Otherwise FALSE.

as\_integer: By default the function will return the same result with "as.numeric" but the user can change the "init" value not start from 1 like R's. Also the result can be unsorted using "result.sort".

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[as\\_integer](#), [colVars](#), [colmeans](#)

**Examples**

```
x<-runif(10)
y1<-is_integer(x) # y1 is FALSE
x<-as.numeric(rpois(10,10)) # integers but typeof is double
y1<-is_integer(x) # y1 is TRUE so you can convert to integer vector.

as_integer(letters) ## as.numeric(letters) produce errors
x<-y1<-NULL
```

---

Check Namespace and Rd files

*Check Namespace and Rd files*

---

**Description**

Check Namespace/Rd and examples files.

**Usage**

```
checkNamespace(path.namespace,path.rfolder,paths.full = FALSE)
checkAliases(path.man,path.rfolder,paths.full = FALSE)
checkTF(path.man,paths.full = FALSE)
checkExamples(path.man,package,each = 1,print.errors = stderr(),
print.names = FALSE,paths.full = FALSE)
checkUsage(path.man,path.rfolder,paths.full = FALSE)
```

**Arguments**

<code>path.namespace</code>	An full path to the "NAMESPACE" file.
<code>package</code>	A character vector with the name of the package.
<code>path.rfolder</code>	An full path to the directory that contains the "R" files.
<code>path.man</code>	An full path to the directory that contains the "Rd" files.
<code>each</code>	An integer value for running <b>each</b> example.
<code>print.errors</code>	Print the errors to a file. By default it's "stderr()".
<code>print.names</code>	A boolean value (TRUE/FALSE) for printing the names of the files before running the examples.
<code>paths.full</code>	Print or return the full paths.

## Details

**checkNamespace:** reads from the NAMESPACE folder all the export R functions, reads from folder R all the R functions and check if all the functions are export.

**checkAliases:** reads from the man directory all the Rd files, then reads from each file the aliases and check if:

- All the R files has man file or an alias.
- All aliases belongs to functions.
- If there are duplicated aliases.

**checkExamples:** reads from the man directory all the Rd files, then read from each file the examples and then run each of them. If you want to print the errors in any file then set "print.errors=file\_name" or in the standard error "print.errors=stderr()" and then you will see all the errors for every file. Set to argument "package" the name of your package. The argument "print.names" it is very helpful because if any of you function crashes R during running you will never know which one was. So setting it "TRUE", it will print the name of each file before running it's example. It might crash, but you will know which file. **Remember that there is always an error timeout so it might didn't crash the current file but one from the previous.**

**checkTF:** reads from the man directory all the Rd files, then read from each file the examples and checks if any examples has the values "T" and "F" instead "TRUE" and "FALSE". The "T","F" is wrong.

**checkUsage:** reads from the man directory all the Rd files and for each man check if the usage section has the right signature for the functions from the R directory.

**checkTF, checkUsage, checkAliases:** you can choose which files not to read for both R and Rd. You must add in the first line of the file in comment the "attribute" "[dont read]". Then each function will know which file to read or not. For Rd you add "%[dont read]" and for R "#[dont read]". Finally, these functions will return in the result a list of which files had this attribute.

## Value

**checkNamespace:** a vector with the names of missing R files. (Don't use it for now)

**checkAliases:** a list with 4 fields.

- **Missing Man files:** A vector with the names of the missing Rd files or nothing.
- **Missing R files:** A vector with the names of the missing R files or nothing.
- **Duplicate alias:** A vector with the names of the duplicate aliases or nothing.
- **dont read:** A list with 2 fields
  - **R:** A character vector whith the names of the files that had attribute "#[dont read]" or nothing.
  - **Rd:** A character vector whith the names of the files that had attribute "%[dont read]" or nothing.

**checkExamples:** a list with 3 fields

- **Errors:** A character vector with the names of the Rd files that produced an error.

- **Big Examples:** A character vector with the names of the Rd files that has big examples per line.
- **dont read:** A list with 2 fields
  - **R:** A character vector with the names of the files that had attribute "#[dont read]" or nothing.
  - **Rd:** A character vector with the names of the files that had attribute "%[dont read]" or nothing.

**checkTF:** a list with 3 fields

- **TRUE:** A character vector with the names of the Rd files that has "T" or nothing.
- **FALSE:** A character vector with the names of the Rd files that has "F" or nothing.
- **dont read:** A list with 2 fields
  - **R:** A character vector with the names of the files that had attribute "#[dont read]" or nothing.
  - **Rd:** A character vector with the names of the files that had attribute "%[dont read]" or nothing.

**checkUsage:** a list with 3 fields

- **missing functions:** A character vector with the name of the file that is missing and the Rd file that is found or nothing.
- **missmatch functions:** A character vector with the name of the file that has mismatch function and the Rd file that is found or nothing.
- **dont read:** A list with 2 fields
  - **R:** A character vector with the names of the files that had attribute "#[dont read]" or nothing.
  - **Rd:** A character vector with the names of the files that had attribute "%[dont read]" or nothing.
- **hidden functions:** A character vector with the name of the functions that have been declared as hidden.
- **usage lines wider than 90 characters:** A list with the Rd's that have usages that are wider than 90 characters.

#### Author(s)

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

#### See Also

[AddToNamespace](#), [sourceR](#), [sourceRd](#), [read.examples](#)

### Examples

```
#for example: path.namespace="C:\some_file\NAMESPACE"  
#for example: path.rfolder="C:\some_file\R\  
#for example: path.man="C:\some_file\man\  
#system.time( a<-checkNamespace(path.namespace,path.rfolder) )  
#system.time( b<-checkAliases(path.man,path.rfolder) )  
#system.time( b<-checkExamples(path.man) )  
#system.time( b<-checkExamples(path.man,2) )  
#system.time( b<-checkTF(path.man) )  
#system.time( b<-checkTF(path.man,path.rfolder) )
```

---

Check whether a square matrix is symmetric

*Check whether a square matrix is symmetric*

---

### Description

Check whether a square matrix is symmetric.

### Usage

```
is.symmetric(x)
```

### Arguments

x                    A square matrix with data.

### Details

Instead of going through the whole matrix, the function will stop if the first disagreement is met.

### Value

A boolean value, TRUE or FALSE.

### Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

### See Also

[cholesky](#), [cora](#), [cova](#)

**Examples**

```
x <-matrix( rnorm( 100 * 400), ncol = 400 )
s1 <- cor(x)
is.symmetric(s1)
x <- x[1:100, ]
is.symmetric(x)

x<-s1<-NULL
```

---

Chi-square and G-square tests of (unconditional) independence

*Chi-square and G-square tests of (unconditional) independence*

---

**Description**

Chi-square and G-square tests of (unconditional) independence.

**Usage**

```
gchi2Test(x, y, logged = FALSE)
```

**Arguments**

x	A numerical vector or a factor variable with data. The data must be consecutive numbers.
y	A numerical vector or a factor variable with data. The data must be consecutive numbers.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

The function calculates the test statistic of the  $\chi^2$  and the  $G^2$  tests of unconditional independence between x and y. x and y need not be numerical vectors like in [g2Test](#).

**Value**

A matrix with two rows. In each row the X2 or G2 test statistic, its p-value and the degrees of freedom are returned.

**Author(s)**

Manos Papadakis and Michail Tsagris.

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

## References

Tsagris M. (2017). Conditional independence test for categorical data using Poisson log-linear model. *Journal of Data Science*, 15(2): 347–356.

## See Also

[g2Test\\_univariate](#), [g2Test\\_univariate\\_perm](#), [g2Test](#)

## Examples

```
nvalues <- 3
nvars <- 2
nsamples <- 2000
data <- matrix( sample( 0:(nvalues - 1), nvars * nsamples, replace = TRUE ), nsamples, nvars )

res<-gchi2Test(data[, 1], data[, 2])
res<-g2Test_univariate( data, rep(3, 2) ) ## G^2 test
res<-chisq.test(data[, 1], data[, 2]) ## X^2 test from R

data<-NULL
```

---

Cholesky decomposition of a square matrix  
*Cholesky decomposition of a square matrix*

---

## Description

Cholesky decomposition of a square matrix.

## Usage

```
cholesky(x,parallel = FALSE)
```

## Arguments

x	A square positive definite matrix.
parallel	A boolean value for parallel version.

## Details

The Cholesky decomposition of a square positive definite matrix is computed. The use of parallel is suggested for matrices with dimensions of 1000 or more.

## Value

An upper triangular matrix.

**Author(s)**

Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

**See Also**

[is.symmetric](#)

**Examples**

```
x = matrix(rnorm(1000 * 50), ncol = 50)
s = cov(x)
a1 <- cholesky(s)
#a2 <- chol(s)
#all.equal(a1[upper.tri(a1)], a2[upper.tri(a2)])
x <- NULL
s <- NULL
a1 <- NULL
a2 <- NULL
```

---

Circular or angular regression(s)

*Circular or angular regression(s)*

---

**Description**

Regression with circular dependent variable and Euclidean or categorical independent variables.

**Usage**

```
spml.reg(y, x, tol = 1e-07, seb = FALSE, maxiters = 100)
spml.regs(y, x, tol = 1e-07, logged = FALSE, maxiters = 100, parallel = FALSE)
```

**Arguments**

y	The dependent variable, it can be a numerical vector with data expressed in radians or it can be a matrix with two columns, the cosine and the sine of the circular data. The benefit of the matrix is that if the function is to be called multiple times with the same response, there is no need to transform the vector every time into a matrix.
x	The independent variable(s) of the single regression model. Can be Euclidean or categorical (factor variables). For the many regression models, a matrix with continuous variables.
tol	The tolerance value to terminate the Newton-Raphson algorithm.
seb	Do you want the standard error of the estimates to be returned? TRUE or FALSE.

logged	Do you want the logarithm of the p-value be returned? TRUE or FALSE.
maxiters	The maximum number of iterations to implement.
parallel	Do you want the regression models to run in parallel? Default value is FALSE.

### Details

The Newton-Raphson algorithm is fitted in this regression as described in Presnell et al. (1998). For the case of `spml.regs()`, for each column of `x` a circular regression model is fitted and the hypothesis testing of no association between `y` and this variable is performed.

### Value

For the `spml.reg()` a list including:

iters	The number of iterations required until convergence of the EM algorithm.
be	The regression coefficients.
seb	The standard errors of the coefficients.
loglik	The value of the maximised log-likelihood.
seb	The covariance matrix of the beta values.

For the `spml.regs()` a matrix with two columns, the test statistics and their associated (log) p-values.

### Author(s)

Michail Tsagris and Stefanos Fafalios.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Stefanos Fafalios <stefanosfafalios@gmail.com>.

### References

Presnell Brett, Morrison Scott P. and Littell Ramon C. (1998). Projected multivariate linear models for directional data. *Journal of the American Statistical Association*, 93(443): 1068-1077.

### See Also

[spml.mle](#), [iag.mle](#), [acg.mle](#)

### Examples

```
x <- rnorm(100)
z <- cbind(3 + 2 * x, 1 -3 * x)
y <- cbind( rnorm(100,z[,1], 1), rnorm(100, z[,2], 1) )
y <- y / sqrt( rowsums(y^2) )
a1 <- spml.reg(y, x)
y <- atan( y[, 2] / y[, 1] ) + pi * I(y[, 1] < 0)
a2 <- spml.reg(y, x)

x <- matrnorm(100, 5)
a3 <- spml.regs(y, x)
```

---

Circular-linear correlation  
*Circular-linear correlation*

---

**Description**

It calculates the squared correlation between a circular and one or more linear variables.

**Usage**

```
circlin.cor(theta, x)
```

**Arguments**

theta	A circular variable expressed in radians.
x	The linear variable or a matrix containing many linear variables.

**Details**

The squared correlation between a circular and one or more linear variables is calculated.

**Value**

A matrix with as many rows as linear variables including:

R-squared	The value of the squared correlation.
p-value	The p-value of the zero correlation hypothesis testing.

**Author(s)**

Michail Tsagris  
R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Mardia, K. V. and Jupp, P. E. (2000). Directional statistics. Chichester: John Wiley & Sons.

**See Also**

[spml.reg](#)

**Examples**

```
#phi <- rvonmises(50, 2, 20, rads = TRUE)
#x <- 2 * phi + rnorm(50)
#y <- matrix(rnorm(50 * 5), ncol = 5)
#res<-circlin.cor(phi, x)
#res<-circlin.cor(phi, y)
y <- NULL
```

---

Coefficient matrices *Coefficient matrices*

---

## Description

Coefficient matrices.

## Usage

```
coeff(x, method, vector = FALSE)
```

## Arguments

x	A matrix with data. The distances will be calculated between pairs of rows. In the case of <b>vecdist</b> this is a vector. For the <b>haversine</b> distance it must be a matrix with two columns, the first column is the latitude and the second the longitude.
method	See details for the available methods.
vector	For return a vector instead a matrix.

## Details

- bhattacharyya :  $\sum \sqrt{(P_i * Q_i)}$

## Value

A square matrix with the pairwise coefficients.

## Author(s)

Manos Papadakis.

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

## See Also

[dista](#), [Dist](#)

## Examples

```
x <- matrix(rnorm(50 * 10), ncol = 10)
a1 <- coeff(x, "bhattacharyya")
x<-a1<-NULL
```

---

Colum-wise cumulative operations (sum, prod, min, max)  
*Colum-wise cumulative operations (sum, prod, min, max)*

---

**Description**

Colum-wise cumulative operations (sum, prod, min, max).

**Usage**

```
colCumSums(x)
colCumProds(x)
colCumMins(x)
colCumMaxs(x)
```

**Arguments**

x                    A numerical matrix.

**Details**

Cumulative mins, maxs, sums and prods are returned.

**Value**

A matrix with the results. It has one row less than the initial matrix.

**Author(s)**

Manos Papadakis and Michail Tsagris

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

**See Also**

[colsums](#), [colMedians](#), [colVars](#)

**Examples**

```
x <- matnorm(10, 10)
res<-colCumSums(x)
res<-colCumMins(x)
res<-colCumMaxs(x)
res<-colCumProds(x)
```

---

Column and row wise coefficients of variation  
*Column and row wise coefficients of variation*

---

**Description**

Column and row wise coefficients of variation.

**Usage**

```
colcvs(x, ln = FALSE, unbiased = FALSE)
rowcvs(x, ln = FALSE, unbiased = FALSE)
```

**Arguments**

x	A numerical matrix with the data.
ln	If you have log-normally distributed data (or assume you do), then set this to TRUE.
unbiased	A boolean variable indicating whether the unbiased for shpould be returned. This is applicable in case of small samples.

**Details**

The colum-wise coefficients of variation are calculated.

**Value**

A vector with the coefficient of variation for each column or row.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colsums](#), [colVars](#)

**Examples**

```
m <- rnorm(100, 10)
x <- matrix(rnorm(100 * 100, m, 1), ncol = 100)
a1 <- colcvs(x)
a2 <- colcvs(x[1:25, ], unbiased = TRUE)
a3 <- colcvs( exp(x), ln = TRUE)
x <- NULL
```

---

Column and row-wise Any/All  
*Column and row-wise Any*

---

## Description

Column and row-wise Any/All of a matrix.

## Usage

```
colAny(x)
rowAny(x)
colAll(x, parallel = FALSE, cores = 0)
rowAll(x, parallel = FALSE, cores = 0)
```

## Arguments

x	A logical matrix with the data.
parallel	Do you want the computations to take place in parallel? The default value is FALSE.
cores	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

## Details

The functions is written in C++ in order to be as fast as possible.

## Value

A vector where item "i" is true if found Any/All true in column/row "i". Otherwise false.

## Author(s)

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

## See Also

[Median](#), [colMedians](#), [colMeans](#) (built-in R function)

## Examples

```
x <- matrix(as.logical(rbinom(100*100,1,0.5)),100,100)
a<-colAny(x)
#b<-apply(x,2,any)
#all.equal(a,b)

a<-rowAny(x)
#b<-apply(x,1,any)
```

```
#all.equal(a,b)

a<-colAll(x)
#b<-apply(x,2,all)
#all.equal(a,b)

a<-b<-x<-NULL
```

---

Column and row-wise means of a matrix

*Column and row-wise means of a matrix*

---

## Description

Column and row-wise means of a matrix.

## Usage

```
colmeans(x, parallel = FALSE, cores = 0)
## S3 method for class 'matrix'
colmeans(x, parallel = FALSE, cores = 0)
## S3 method for class 'data.frame'
colmeans(x, parallel = FALSE, cores = 0)
rowmeans(x)
colhameans(x, parallel = FALSE)
rowhameans(x)
```

## Arguments

<code>x</code>	A numerical matrix or data.frame with data.
<code>parallel</code>	Do you want to do it in parallel in C++? TRUE or FALSE.
<code>cores</code>	Number of cores to use for parallelism. Valid only when argument <code>parallel</code> is set to TRUE. Default value is 0 and it means the maximum supported cores.

## Value

A vector with the column or row arithmetic or harmonic means.

## Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

## See Also

[colsums](#), [rowsums](#), [colMins](#), [colMedians](#), [colMads](#)

**Examples**

```
x <- matrix(rpois(100 * 100, 10), ncol = 100)
x1 <- colmeans(x)
#x2 <- colMeans(x)
#all.equal(x1, x2)

x1 <- rowmeans(x)
#x2 <- rowMeans(x)
#all.equal(x1, x2)

colhameans(x)
rowhameans(x)

x<-x1<-x2<-NULL
```

---

Column and row-wise medians of a matrix or median of a vector.

*Column and row-wise medians of a matrix or median of a vector*

---

**Description**

Column and row-wise medians of a matrix or median of a vector.

**Usage**

```
colMedians(x, na.rm = FALSE, parallel = FALSE, cores = 0)
rowMedians(x, na.rm = FALSE, parallel = FALSE, cores = 0)
Median(x, na.rm=FALSE)
med(x, na.rm=FALSE)
```

**Arguments**

<code>x</code>	A vector, matrix or data.frame with the data.
<code>parallel</code>	Do you want to do it in parallel in C++? TRUE or FALSE.
<code>na.rm</code>	TRUE or FALSE for remove NAs if exists.
<code>cores</code>	Number of cores to use for parallelism. Valid only when argument <code>parallel</code> is set to TRUE. Default value is 0 and it means the maximum supported cores.

**Details**

The functions is written in C++ in order to be as fast as possible.

**Value**

A vector with the column medians.

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Median](#), [colVars](#), [colMeans](#) (built-in R function)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100 )
a <- apply(x, 2, median)
b1 <- colMedians(x)
all.equal(as.vector(a), b1)

x<-a<-b1<-NULL
```

---

Column and row-wise nth smallest value of a matrix/vector

*Column and row-wise nth smallest value of a matrix/vector*

---

**Description**

Column and row-wise nth smallest value of a matrix/vector.

**Usage**

```
colnth(x,elems, num.of.nths = 1,descending = FALSE,na.rm = FALSE,
index.return = FALSE, parallel = FALSE, cores = 0)
rownth(x,elems, num.of.nths = 1,descending = FALSE,na.rm = FALSE,
index.return = FALSE, parallel = FALSE, cores = 0)
nth(x, k, num.of.nths = 1,descending = FALSE,index.return = FALSE,na.rm = FALSE)
```

**Arguments**

x	A matrix with the data.
elems	An integer vector with the kth smallest number to be returned for each column/row.
k	The kth smallest/biggest number to be returned.
num.of.nths	The number of the returned nth. By default is 1. Not use with argument parallel, for now.
descending	A boolean value (TRUE/FALSE) for descending order (biggest number). By default is ascending (smallest number).
index.return	Return the index of the kth smallest/biggest number.
parallel	Do you want to do it in parallel in C++? TRUE or FALSE only for col-row wise.
na.rm	TRUE or FALSE for remove NAs if exists. Only for function "nth".
cores	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

**Details**

The functions is written in C++ in order to be as fast as possible.

**Value**

For "colnth" , "rownth": A vector with the column/row nth

For "nth": The nth value.

**Author(s)**

Manos Papadakis <papadakm95@gmail.com>

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Median](#), [colMedians](#), [colMeans](#) (buit-in R function)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100 )
elems <- sample(1:100,100,TRUE)
colnth(x,elems)
rownth(x,elems)
x <- rnorm(1000)

nth(x, 500)
#sort(x)[500]

x<-elems<-NULL
```

---

Column and row-wise Order - Sort Indices

*Column and row-wise Order - Sort Indices*

---

**Description**

Column and row-wise Order - Sort Indices.

**Usage**

```
colOrder(x,stable=FALSE,descending=FALSE, parallel = FALSE, cores = 0)
rowOrder(x,stable=FALSE,descending=FALSE, parallel = FALSE, cores = 0)
Order(x,stable=FALSE,descending=FALSE,partial = NULL,parallel = FALSE)
```

**Arguments**

<code>x</code>	A matrix with numbers or a numeric/character vector.
<code>stable</code>	A boolean value for using a stable sorting algorithm.
<code>descending</code>	A boolean value (TRUE/FALSE) for sorting the vector in descending order. By default sorts the vector in ascending.
<code>parallel</code>	A boolean value for parallel version. For Order, this argument is supported on Windows and most of the unix.
<code>partial</code>	A boolean value for partial sorting.
<code>cores</code>	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE column - major ordering. Default value is 0 and it means the maximum supported cores.

**Details**

The function applies "order" in a column or row-wise fashion or Order a vector. If you want the same results as R's, then set "stable=TRUE" because "stable=FALSE" uses a sorting algorithm that it is not stable like R's sort. But it is faster to use the default. This version is faster for large data, more than 300.

**Value**

For "colOrder" and "rowOrder" a matrix with integer numbers. The result is the same as `apply(x, 2, order)` or `apply(x, 1, order)`.

For "Order" sort the vector and returns the indices of each element that it has before the sorting. The result is the same as `order(x)` but for the same exactly results set argument "stable" to "TRUE".

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colsums](#), [coldiffs](#), [colMedians](#), [colprods](#)

**Examples**

```
x <- matrix( runif(10 * 10), ncol = 10 )
res<-colOrder(x)
res<-apply(x, 2, order)
res<-rowOrder(x)
t(apply(x, 1, order))

y <- rnorm(100)
b <- Order(y)
a <- order(y)
all.equal(a,b) ## false because it is not stable
b <- Order(y,stable=TRUE)
```

```
all.equal(a,b) ## true because it is stable  
x<-y<-b<-a<-NULL
```

---

Column and row-wise products

*Column and row-wise products*

---

## Description

Column and row-wise products.

## Usage

```
colprods(x, method = "direct")  
rowprods(x)
```

## Arguments

x	A matrix with numbers.
method	The type of colCumProds to use. For direct multiplication use "direct" or "exp-sumlog" for a more numerically stable, but slower way.

## Details

The product of the numbers in a matrix is returned either column-wise or row-wise.

## Value

A vector with the column or the row products.

## Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

## See Also

[colsums](#), [coldiffs](#), [colMedians](#)

## Examples

```
x <- matrix( runif(100 * 10), ncol = 10 )  
res<-colprods(x)  
res<-rowprods(x)  
  
x<-NULL
```

---

Column and row-wise range of values of a matrix  
*Column and row-wise range of values of a matrix*

---

**Description**

Column and row-wise range of values of a matrix.

**Usage**

```
colrange(x, cont = TRUE, parallel = FALSE, cores = 0)  
rowrange(x, cont = TRUE)
```

**Arguments**

<code>x</code>	A numerical matrix or data.frame with data.
<code>parallel</code>	Execute algorithm in parallel for data.frame.
<code>cont</code>	If the data are continuous, leave this TRUE and it will return the range of values for each variable (column). If the data are integers, categorical, or if you want to find out the number of unique numbers in each column set this to FALSE.
<code>cores</code>	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

**Value**

A vector with the relevant values.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colMins](#), [colMaxs](#), [rowMins](#), [rowMaxs](#), [nth](#), [colMedians](#), [colVars](#), [colSort](#), [rowSort](#)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100 )  
  
a1 <- colrange(x)  
a2 <- apply(x, 2, function(x) diff( range(x)) )  
all.equal(a1, a2)  
  
a1 <- rowrange(x)  
a2 <- apply(x, 1, function(x) diff( range(x)) )  
all.equal(a1, a2)
```

```
x<-a1<-a2<-NULL
```

---

Column and row-wise ranks

*Column and row-wise ranks*

---

### Description

Column and row-wise ranks.

### Usage

```
colRanks(x,method = "average",descending = FALSE,
         stable = FALSE, parallel = FALSE, cores = 0)
rowRanks(x,method = "average",descending = FALSE,
         stable = FALSE, parallel = FALSE, cores = 0)
Rank(x,method = "average",descending = FALSE,stable = FALSE, parallel = FALSE)
```

### Arguments

x	A numerical matrix or data.frame with the data.
parallel	A boolean value for parallel version.
method	a character string for choosing method. Must be one of: <ul style="list-style-type: none"> <li>• average : a permutation with their mean values at each index set of ties</li> <li>• min : a permutation with minimum values at each index set of ties</li> <li>• max : a permutation with maximum values at each index set of ties</li> <li>• first : a permutation with increasing values at each index set of ties</li> <li>• random : a permutation with random values at each index set of ties</li> </ul>
descending	A boolean value (TRUE/FALSE) for sorting the vector in descending order. By default sorts the vector in ascending.
stable	A boolean value (TRUE/FALSE) for choosing a stable sort algorithm. Stable means that discriminates on the same elements. Only for the method "first".
cores	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

### Details

For each column or row of a matrix the ranks are calculated and they are returned.

### Value

A matrix with the column or row-wise ranks.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Rank](#), [correls](#)

**Examples**

```
x <- matnorm(100, 10)
a1 <- colRanks(x)
a2 <- apply(x, 2, rank)
b1 <- rowRanks(x)
b2 <- apply(x, 1, rank)

a1 <- Rank(x[,1])
a1 <- rank(x[,1])

x<-a1<-a2<-b1<-b2<-NULL
```

---

Column and row-wise Shuffle

*Column and row-wise Shuffle*

---

**Description**

Column and row-wise shuffle of a matrix.

**Usage**

```
colShuffle(x)
rowShuffle(x)
```

**Arguments**

x                    A matrix or data.frame with the data.

**Details**

The functions is written in C++ in order to be as fast as possible.

**Value**

A vector with the column/row Shuffle.

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Median](#), [colVars](#), [colMeans](#) (built-in R function)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100 )
colShuffle(x)
rowShuffle(x)

x<-NULL
```

---

Column and row-wise sums of a matrix

*Column and row-wise sums of a matrix*

---

**Description**

Column and row-wise sums of a matrix.

**Usage**

```
colsums(x, indices = NULL, parallel = FALSE, na.rm = FALSE, cores = 0)
rowsums(x, indices = NULL, parallel = FALSE, na.rm = FALSE, cores = 0)
```

**Arguments**

<code>x</code>	A numerical matrix with data.
<code>indices</code>	An integer vector with the indices to sum the columns/rows.
<code>parallel</code>	Do you want to do it in parallel in C++? TRUE or FALSE. Doesn't work with argument "indices".
<code>na.rm</code>	A logical value indicating to remove NAs. The algorithm run in parallel so do not use with option parallel.
<code>cores</code>	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

**Value**

A vector with sums.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colMedians](#), [colmeans](#), [colVars](#)

**Examples**

```
x <- matrix(rpois(500 * 100, 10), ncol = 100)
x1 <- colsums(x)
x2 <- colSums(x)
all.equal(x1, x2)

x1 <- rowsums(x)
x2 <- rowSums(x)
all.equal(x1, x2)

x<-x1<-x2<-NULL
```

---

Column and row-wise tabulate

*Column and row-wise tabulate*

---

**Description**

Column and row-wise tabulate of a matrix.

**Usage**

```
colTabulate(x, max_number = max(x))
rowTabulate(x, max_number = max(x))
```

**Arguments**

x	An integer matrix with the data. The numbers must start from 1, i.e. 1, 2, 3, 4, ... No zeros are allowed. Anything else may cause a crash.
max_number	The maximum value of vector x. If you know which is the max number use this argument for faster results or by default max(x).

**Details**

The functions is written in C++ in order to be as fast as possible.

**Value**

A matrix where in each column the command "tabulate" has been performed. The number of rows of the returned matrix will be equal to the max\_number if given. Otherwise, the functions will find this number.

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colShuffle](#), [colVars](#), [colmeans](#)

**Examples**

```
x <- matrix( rbinom(100 * 100, 4, 0.5), ncol = 100 )
colTabulate(x)
rowTabulate(x)

x<-NULL
```

---

Column and row-wise variances and standard deviations

*Column and row-wise variances and standard deviations of a matrix*

---

**Description**

Column and row-wise variances and standard deviations of a matrix

**Usage**

```
## S3 method for class 'matrix'
colVars(x, std = FALSE, na.rm = FALSE, parallel = FALSE, cores = 0)
## S3 method for class 'data.frame'
colVars(x, std = FALSE, na.rm = FALSE, parallel = FALSE, cores = 0)
colVars(x, std = FALSE, na.rm = FALSE, parallel = FALSE, cores = 0)
rowVars(x, std = FALSE, na.rm = FALSE, parallel = FALSE, cores = 0)
```

**Arguments**

x	A matrix with the data.
std	A boolean variable specifying whether you want the variances (FALSE) or the standard deviations (TRUE) of each column.
na.rm	TRUE or FALSE for remove NAs if exists.
parallel	Should parallel implementations take place in C++? The default value is FALSE.
cores	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

**Details**

We found this on stackoverflow which was created by David Arenburg. We then modified the function to match the sums type formula of the variance, which is faster.

**Value**

A vector with the column variances or standard deviations.

**Author(s)**

Michail Tsagris and Manos Papadakis.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colmeans](#), [colMedians](#), [colrange](#)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100 )
a2 <- colVars(x)
x<-a2<-NULL
```

---

Column and rows-wise mean absolute deviations

*Column and row-wise mean absolute deviations*

---

**Description**

Column and row-wise mean absolute deviations.

**Usage**

```
colMads(x,method = "median",na.rm=FALSE,parallel = FALSE, cores = 0)
rowMads(x,method = "median",na.rm=FALSE,parallel = FALSE, cores = 0)
Mad(x,method = "median",na.rm=FALSE)
```

**Arguments**

<code>x</code>	A vector, matrix or data.frame with the data.
<code>method</code>	A character vector with values "median", for median absolute deviation or "mean", for mean absolute deviation.
<code>na.rm</code>	A logical value TRUE/FALSE to remove NAs.
<code>parallel</code>	A boolean value for parallel version.
<code>cores</code>	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

**Details**

The functions is written in C++ in order to be as fast as possible.

**Value**

A vector with the column-wise mean absolute deviations.

**Author(s)**

Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colMedians](#), [rowMedians](#), [colVars](#), [colmeans](#), [colMeans](#) (built-in R function)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100 )
a <- colMads(x)
```

```
x<-NULL
```

---

Column-wise differences

*Column-wise differences*

---

**Description**

Column-wise differences.

**Usage**

```
coldiffs(x)
```

**Arguments**

x                    A matrix with numbers.

**Details**

This function simply does this function  $x[, -1] - x[, -k]$ , where k is the last column of the matrix x. But it does it a lot faster. That is, 2nd column - 1st column, 3rd column - 2nd column, and so on.

**Value**

A matrix with one column less containing the differences between the successive columns.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Dist](#), [dista](#), [colmeans](#)

**Examples**

```
x <- matrix( rnorm(50 * 10), ncol = 10 )
res<-coldiffs(x)
```

```
x<-NULL
```

---

**Column-wise kurtosis and skewness coefficients***Column-wise kurtosis and skewness coefficients*

---

**Description**

Column-wise kurtosis and skewness coefficients.

**Usage**

```
colkurtosis(x, pvalue = FALSE)
```

```
colskewness(x, pvalue = FALSE)
```

**Arguments**

x	A matrix with the data, where the rows denote the samples and the columns are the variables.
pvalue	If you want a hypothesis test that the skewness or kurtosis are significant set this to TRUE. This checks whether the skewness is significantly different from 0 and whether the kurtosis is significantly different from 3.

**Details**

The skewness and kurtosis coefficients are calculated. For the skewness coefficient we use the sample unbiased version of the standard deviation. For the kurtosis, we do not subtract 3.

**Value**

If "pvalue" is FALSE, a vector with the relevant coefficient. Otherwise a matrix with two columns. The kurtosis or skewness coefficient and the p-value from the hypothesis test that they are significantly different from 3 or 0 respectively.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[skew](#), [skew.test2](#), [colMedians](#), [colmeans](#), [colVars](#), [sftests](#)

**Examples**

```
## 200 variables, hence 200 F-tests will be performed
x = matrix( rnorm(200 * 50), ncol = 50 )
## 200 observations in total
colkurtosis(x)
colskewness(x)
x <- NULL
```

---

Column-wise matching coefficients

*Column-wise matching coefficients*

---

**Description**

Column-wise matching coefficients.

**Usage**

```
match.coefs(x, y = NULL, ina, type = "jacc")
```

**Arguments**

x	A matrix with the data, where the rows denote the samples and the columns are the variables.
y	A second matrix with the data of the second group. If this is NULL (default value) then the argument ina must be supplied. Notice that when you supply the two matrices the procedure is two times faster.
ina	A numerical vector with 1s and 2s indicating the two groups. Be careful, the function is designed to accept only these two numbers. In addition, if your "y" is NULL, you must specify "ina".
type	This denotes the type of matching coefficient to calculate. For the Jaccard index put "jacc". For the simple matching coefficient put "smc" or else both of them will be calculated.

**Details**

Two matrices are given as input and for each column matching coefficients are calculated, either the Jaccard or the simple matching coefficient or both.

**Value**

A matrix with one or two columns, depending on the type you have specified. If you specify "both", there will be two columns, if you specify "jacc" or "smc" then just one column.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[odds](#), [colTabulate](#)

**Examples**

```
x <- matrix(rbinom(400 * 10, 1, 0.5), ncol = 10)
y <- matrix(rbinom(400 * 10, 1, 0.5), ncol = 10)
a <- match.coefs(x, y, type = "both")
x <- NULL
y <- NULL
```

---

Column-wise minimum and maximum

*Column-wise minimum and maximum of a matrix*

---

**Description**

Column-wise minimum and maximum of a matrix.

**Usage**

```
colMins(x, value = FALSE, parallel = FALSE, cores = 0)
colMaxs(x, value = FALSE, parallel = FALSE, cores = 0)
colMinsMaxs(x, parallel = FALSE, cores = 0)
```

**Arguments**

<code>x</code>	A numerical matrix or data.frame with data.
<code>value</code>	If the value is FALSE it returns the indices of the minimum/maximum, otherwise it returns the minimum and maximum values.
<code>parallel</code>	Do you want to do it in parallel in C++? TRUE or FALSE. The parallel will return the minimum/maximum value only. It will never return the indices.
<code>cores</code>	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

**Value**

A vector with the relevant values.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[rowMins](#), [rowMaxs](#), [nth](#), [colrange](#), [colMedians](#), [colVars](#), [colSort](#), [rowSort](#)

**Examples**

```
x <- matrix( rnorm(100 * 200), ncol = 200 )

s1 <- colMins(x)
s2 <- apply(x, 2, min)

s1 <- colMaxs(x)
s2 <- apply(x, 2, max)

s1 <- colMinsMaxs(x)
s2 <- c(apply(x, 2, min), apply(x, 2, max))

x<-s1<-s2<-NULL
```

---

Column-wise MLE of some univariate distributions

*Column-wise MLE of some univariate distributions*

---

**Description**

Column-wise MLE of some univariate distributions.

**Usage**

```
colexpmle(x)
colexp2.mle(x)
colgammamle(x, tol = 1e-07)
colinvgauss.mle(x)
collaplace.mle(x)
collindley.mle(x)
colmaxboltz.mle(x)
colnormal.mle(x)
colpareto.mle(x)
colrayleigh.mle(x)
colvm.mle(x, tol = 1e-07)
colweibull.mle(x, tol = 1e-09, maxiters = 100, parallel = FALSE)
colnormlog.mle(x)
```

**Arguments**

<code>x</code>	A numerical matrix with data. Each column refers to a different vector of observations of the same distribution. For exponential, 2 parameter exponential, Weibull, gamma, inverse Gaussian, Maxwell-Boltzman, Lindley, Rayleigh and Pareto distributions, the numbers must be greater than zero. For the Poisson and geometric distributions, the numbers must be integers, 0, 1, 2,... For the Normal and Laplace distribution the numbers can take any value. The von Mises distribution takes values between 0 and $2\pi$ (radians).
<code>tol</code>	The tolerance value to terminate the Newton-Fisher algorithm.
<code>maxiters</code>	The maximum number of iterations to implement.
<code>parallel</code>	Do you want to calculations to take place in parallel? The default value is FALSE

**Details**

For each column, the same distribution is fitted and its parameter and log-likelihood are computed.

**Value**

A matrix with two, three or five (for the `colnormlog.mle`) columns. The first one or the first two contain the parameter(s) of the distribution and the other columns contain the log-likelihood values.

**Author(s)**

Michail Tsagris and Stefanos Fafalios

R implementation and documentation: Michail Tsagris <[mtsagris@uoc.gr](mailto:mtsagris@uoc.gr)> and Stefanos Fafalios <[stefanosfafalios@gmail.com](mailto:stefanosfafalios@gmail.com)>

**References**

Kalimuthu Krishnamoorthy, Meesook Lee and Wang Xiao (2015). Likelihood ratio tests for comparing several gamma distributions. *Environmetrics*, 26(8):571-583.

N.L. Johnson, S. Kotz and N. Balakrishnan (1994). *Continuous Univariate Distributions, Volume 1* (2nd Edition).

N.L. Johnson, S. Kotz and N. Balakrishnan (1970). *Distributions in statistics: continuous univariate distributions, Volume 2*.

Sharma V. K., Singh S. K., Singh U. and Agiwal V. (2015). The inverse Lindley distribution: a stress-strength reliability model with application to head and neck cancer data. *Journal of Industrial and Production Engineering*, 32(3): 162-173.

**See Also**

[vm.mle](#), [poisson.mle](#), [normal.mle](#), [gammamle](#)

**Examples**

```
x <- matrix(rnorm(1000 * 50), ncol = 50)
a <- colnormal.mle(x)
b <- collaplace.mle(x)
x <- NULL
```

---

Column-wise true/false value

*Column-wise true/false value of a matrix*

---

**Description**

Column-wise true/false value of a matrix.

**Usage**

```
colTrue(x)
colFalse(x)
colTrueFalse(x)
```

**Arguments**

x                    A logical matrix with data.

**Value**

An integer vector where item "i" is the number of the true/false values of "i" column.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[rowMins](#), [rowFalse](#), [nth](#), [colrange](#), [colMedians](#), [colVars](#), [colSort](#), [rowSort](#), [rowTrue](#)

**Examples**

```
x <- matrix(as.logical(rbinom(100*100,1,0.5)),100,100)

s1 <- colTrue(x)

s1 <- colFalse(x)

s1 <- colTrueFalse(x)

x<-s1<-NULL
```

---

Column-wise uniformity Watson test for circular data  
*Column-wise uniformity tests for circular data*

---

**Description**

Column-wise uniformity tests for circular data.

**Usage**

```
colwatsons(u)
```

**Arguments**

**u** A numeric matrix containing the circular data which are expressed in radians. Each column is a different sample.

**Details**

These tests are used to test the hypothesis that the data come from a circular uniform distribution. The Kuiper test is much more time consuming and this is why it not implemented yet. Once we figure out a way to make it fast, we will include it.

**Value**

A matrix with two columns, the value of the test statistic and its associated p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Jammalamadaka, S. Rao and SenGupta, A. (2001). Topics in Circular Statistics, pg. 153-55 (Kuiper's test) & 156-157 (Watson's test).

**See Also**

[watson](#), [vmf.mle](#), [rvonmises](#)

**Examples**

```
#x <- matrix( rvonmises(n = 50 * 10, m = 2, k = 0), ncol = 10 )
#res<-colwatsons(x)
x <- NULL
```

---

Column-wise Yule's Y (coefficient of colligation)  
*Column-wise Yule's Y (coefficient of colligation)*

---

**Description**

Column-wise Yule's Y (coefficient of colligation).

**Usage**

```
col.yule(x, y = NULL, ina)
```

**Arguments**

x	A matrix with 0 and 1. Every column refers to a different sample or variable.
y	A second matrix, of the same dimensions as x, with 0 and 1. Every column refers to a different sample or variable.
ina	If y is NULL, ina must be specified. This is a numeric vector with 1s and 2s, indicating the group of each row.

**Details**

Yule's coefficient of colligation is calculated for every column.

**Value**

A vector with Yule's Y, one for every column of x is returned.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Yule G. Udny (1912). On the Methods of Measuring Association Between Two Attributes. Journal of the Royal Statistical Society, 75(6):579-652.

**See Also**

[yule](#), [odds](#)

**Examples**

```
x <- matrix(rbinom(300 * 10, 1, 0.5), ncol = 10)
ina <- rep(1:2, each = 150)
res<-col.yule( x, ina = ina )
```

---

Convert a dataframe to matrix

*Convert a dataframe to matrix*

---

## Description

Convert a dataframe to matrix.

## Usage

```
data.frame.to_matrix(x,col.names = NULL,row.names = NULL)
```

## Arguments

x	A Numeric matrix with data and NAs.
col.names	A boolean value for keeping the colnames for argument x or a character vector for the new colnames.
row.names	A boolean value for keeping the rownames for argument x or a character vector for the new rownames.

## Details

This functions converts a dataframe to matrix. Even if there are factors, the function converts them into numerical values. Attributes are not allowed for now.

## Value

A matrix wich has the numrical values from the dataframe.

## Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>

## See Also

[Match](#), [is.symmetric](#), [permutation](#)

## Examples

```
res<-data.frame.to_matrix(iris)
```

---

Convert R function to the Rfast's coresponding  
*Convert R function to the Rfast's coresponding*

---

## Description

Convert R function to the Rfast's coresponding.

## Usage

```
as.Rfast.function(Rfunction.name,margin=NULL)
```

## Arguments

`Rfunction.name` An character value with the name of the function.  
`margin` A logical function for return the column-row wise function.

## Details

Given the name of R function, it returns the coresponding function's name from Rfast.

## Value

The coresponding Rfast function.

## Author(s)

Manos Papadakis and Michail Tsagris

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

## See Also

[colsums](#), [colMedians](#), [colVars](#)

## Examples

```
res<-as.Rfast.function("var")
```

---

Correlation based forward regression

*Correlation based forward regression*

---

### Description

Correlation based forward regression.

### Usage

```
cor.fsreg(y, x, ystand = TRUE, xstand = TRUE, threshold = 0.05,
tolb = 2, tolr = 0.02, stopping = "BIC")
```

### Arguments

y	A numerical vector.
x	A matrix with data, the predictor variables.
ystand	If this is TRUE the response variable is centered. The mean is subtracted from every value.
xstand	If this is TRUE the independent variables are standardised.
threshold	The significance level, set to 0.05 by default. Bear in mind that the logarithm of it is used, as the logarithm of the p-values is calculated at every point. This will avoid numerical overflows and small p-values, less than the machine epsilon, being returned as zero.
tolb	If we see only the significance of the variables, many may enter the linear regression model. For this reason, we also use the BIC as a way to validate the inclusion of a candidate variable. If the BIC difference between two successive models is less than the tolerance value, the variable will not enter the model, even if it is statistically significant. Set it to 0 if you do not want this extra check.
tolr	This is an alternative to the BIC change and it uses the adjusted coefficient of determination. If the increase in the adjusted $R^2$ is more than the tolr continue.
stopping	This refers to the type of extra checking to do. If you want the BIC check, set it to "BIC". If you want the adjusted $R^2$ check set this to "ar2". Or, if you want both of them to take place, both of these criteria to be satisfied make this "BICR2".

### Details

The forward regression tries one by one the variables using the F-test, basically partial F-test every time for the latest variable. This is the same as testing the significance of the coefficient of this latest entered variable. Alternatively the correlation can be used and in this case the partial correlation coefficient. There is a direct relationship between the t-test statistic and the partial correlation coefficient. Now, instead of having to calculate the test statistic, we calculate the partial correlation coefficient. Using Fisher's z-transform we get the variance immediately. The partial correlation coefficient, using Fisher's z-transform, and the partial F-test (or the coefficient's t-test statistic) are not identical. They will be identical for large sample sizes though.

**Value**

A matrix with three columns, the index of the selected variables, the logged p-value and the the test statistic value and the BIC or adjusted  $R^2$  of each model. In the case of stopping="BICR2" both of these criteria will be returned.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Draper, N.R. and Smith H. (1988). Applied regression analysis. New York, Wiley, 3rd edition.

**See Also**

[score.glm](#)s, [univglm](#)s, [logistic\\_only](#), [poisson\\_only](#), [regression](#)

**Examples**

```
## 200 variables, hence 200 univariate regressions are to be fitted
x <- matnorm(200, 100)
y <- rnorm(200)
cor.fsreg(y, x)
x <- NULL
```

---

Correlation between pairs of variables

*Correlation between pairs of variables*

---

**Description**

Correlations between pairs of variables.

**Usage**

```
corpairs(x, y, rho = NULL, logged = FALSE, parallel = FALSE)
```

**Arguments**

x	A matrix with real valued data.
y	A matrix with real valued data whose dimensions match those of x.
rho	This can be a vector of assumed correlations (equal to the number of variables or the columns of x or y) to be tested. If this is not the case, leave it NULL and only the correlations will be returned.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)? This is taken into account only if "rho" is a vector.
parallel	Should parallel implementations take place in C++? The default value is FALSE.

**Details**

The paired correlations are calculated. For each column of the matrices `x` and `y` the correlation between them is calculated.

**Value**

A vector of correlations in the case of "rho" being NULL, or a matrix with two extra columns, the test statistic and the (logged) p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Lambert Diane (1992). Zero-Inflated Poisson Regression, with an Application to Defects in Manufacturing. *Technometrics*. 34(1):1-14.

Johnson Norman L., Kotz Samuel and Kemp Adrienne W. (1992). *Univariate Discrete Distributions* (2nd ed.). Wiley

Cohen, A. Clifford (1960). Estimating parameters in a conditional Poisson distribution. *Biometrics*. 16:203-211.

Johnson, Norman L. Kemp, Adrienne W. Kotz, Samuel (2005). *Univariate Discrete Distributions* (third edition). Hoboken, NJ: Wiley-Interscience.

**See Also**

[correls](#), [allbetas](#), [mvbetas](#)

**Examples**

```
x <- matnorm(100, 100)
y <- matnorm(100, 100)
corpairs(x, y)
a <- corpairs(x, y)
x <- NULL
y <- NULL
```

---

Correlations

*Correlation between a vector and a set of variables*

---

### Description

Correlation between a vector and a set of variables.

### Usage

```
correls(y, x, type = "pearson", a = 0.05, rho = 0)
groupcorrels(y, x, type = "pearson", ina)
```

### Arguments

y	A numerical vector.
x	A matrix with the data.
type	The type of correlation you want. "pearson" and "spearman" are the two supported types for the "correls" because their standard error is easily calculated. For the "groupcorrels" you can also put "kendall" because no hypothesis test is performed in that function.
a	The significance level used for the confidence intervals.
rho	The value of the hypothesised correlation to be used in the hypothesis testing.
ina	A factor variable or a numeric variable indicating the group of each observation.

### Details

The functions uses the built-in function "cor" which is very fast and then includes confidence intervals and produces a p-value for the hypothesis test.

### Value

For the "correls" a matrix with 5 column; the correlation, the p-value for the hypothesis test that each of them is equal to "rho", the test statistic and the  $a/2\%$  lower and upper confidence limits.

For the "groupcorrels" a matrix with rows equal to the number of groups and columns equal to the number of columns of x. The matrix contains the correlations only, no statistical hypothesis test is performed.

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

### See Also

[allbetas](#), [univglms](#)

**Examples**

```
x <- matnorm(60, 100 )
y <- rnorm(60)
r <- cor(y, x) ## correlation of y with each of the xs
a <- allbetas(y, x) ## the coefficients of each simple linear regression of y with x
b <- correls(y, x)
ina <- rep(1:2, each = 30)
b2 <- groupcorrels(y, x, ina = ina)
x <- NULL
```

---

Covariance and correlation matrix

*Fast covariance and correlation matrix calculation*

---

**Description**

Fast covariance and correlation matrix calculation.

**Usage**

```
cova(x, center = FALSE, large = FALSE)
```

```
cora(x, large = FALSE)
```

**Arguments**

x	A matrix with data. It has to be matrix, if it is data.frame for example the function does not turn it into a matrix.
center	If you want to center the data prior to applying the cross product of the matrix set this equal to TRUE, otherwise leave it NULL.
large	If you have large matrices, with thousands of rows and or many tens or hundreds of columns set this equal to TRUE in order to use Rfast's <a href="#">Crossprod</a> or <a href="#">Tcrossprod</a> functions. These functions are twice or up to 3 times faster than the corresponding built-in functions.

**Details**

The calculations take place faster than the built-in functions `cor` as the number of variables increases. This is true if the number of variables is high, say from 500 and above. The "cova" on the other hand is always faster. For the "cova" in specific, we have an option to center the data prior to the cross product. This can be more stable if you have many tens of thousands of rows due to numerical issues that can arise.

For the correlation matrix we took the code from here

<https://stackoverflow.com/questions/18964837/fast-correlation-in-r-using-c-and-parallelization/18965892#18965892>

**Value**

The covariance or the correlation matrix.

**Author(s)**

Michail Tsagris and Manos Papadakis <papadakm95@gmail.com>.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colVars](#), [cor](#), [cov](#)

**Examples**

```
x <- matnorm(100, 40)
s1 <- cov(x)
s2 <- cova(x)
all.equal(s1, s2)
x <- NULL
```

---

Cox confidence interval for the ratio of two Poisson variables  
*Cox confidence interval for the ratio of two Poisson variables*

---

**Description**

Cox confidence interval for the ratio of two Poisson variables.

**Usage**

```
cox.poisrat(x, y, alpha = 0.05)
col.coxpoisrat(x, y, alpha = 0.05)
```

**Arguments**

x	A numeric vector or a matrix with count data.
y	A numeric vector or a matrix with count data.
alpha	The 1 - confidence level. The default value is 0.05.

**Details**

Cox confidence interval for the ratio of two Poisson means is calculated.

**Value**

For the `cox.poisrat` a vector with three elements, the ratio and the lower and upper confidence interval limits. For the `col.coxpoisrat` a matrix with three columns, the ratio and the lower and upper confidence interval limits.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Krishnamoorthy K., Peng J. and Zhang D. (2016). Modified large sample confidence intervals for Poisson distributions: Ratio, weighted average, and product of means. *Communications in Statistics-Theory and Methods*, 45(1): 83-97.

**See Also**

[correls](#), [Table](#)

**Examples**

```
x <- rpois(100, 10)
y <- rpois(100, 10)
res<-cox.poisrat(x, y)
```

---

Cross-Validation for the k-NN algorithm  
*Cross-Validation for the k-NN algorithm*

---

**Description**

Cross-Validation for the k-NN algorithm.

**Usage**

```
knn.cv(folds = NULL, nfolds = 10, stratified = FALSE, seed = NULL, y, x, k,
dist.type = "euclidean", type = "C", method = "average", freq.option = 0,
pred.ret = FALSE, mem.eff = FALSE)
```

**Arguments**

<code>folds</code>	A list with the indices of the folds.
<code>nfolds</code>	The number of folds to be used. This is taken into consideration only if "folds" is NULL.

stratified	Do you want the folds to be selected using stratified random sampling? This preserves the analogy of the samples of each group. Make this TRUE if you wish, but only for the classification. If you have regression (type = "R"), do not put this to TRUE as it will cause problems or return wrong results.
seed	If NULL different folds will be created every time. Otherwise set your own seed.
y	A vector of data. The response variable, which can be either continuous or categorical (factor is acceptable).
x	A matrix with the available data, the predictor variables.
k	A vector with the possible numbers of nearest neighbours to be considered.
dist.type	The type of distance to be used, "euclidean" or "manhattan".
type	Do you want to do classification ("C") or regression ("R")?
method	If you do regression (type = "R"), then how should the predicted values be calculated? Choose among the average ("average"), median ("median") or the harmonic mean ("harmonic") of the closest neighbours.
freq.option	If classification (type = "C") and ties occur in the prediction, more than one class have the same number of k nearest neighbours, there are three strategies available. Option 0 selects the first most frequent encountered. Option 1 randomly selects the most frequent value, in the case that there are duplicates.
pred.ret	If you want the predicted values returned set this to TRUE.
mem.eff	Boolean value indicating a conservative or not use of memory. Lower usage of memory/Having this option on will lead to a slight decrease in execution speed and should ideally be on when the amount of memory in demand might be a concern.

### Details

The concept behind k-NN is simple. Suppose we have a matrix with predictor variables and a vector with the response variable (numerical or categorical). When a new vector with observations (predictor variables) is available, its corresponding response value, numerical or categorical, is to be predicted. Instead of using a model, parametric or not, one can use this ad hoc algorithm.

The k smallest distances between the new predictor variables and the existing ones are calculated. In the case of regression, the average, median, or harmonic mean of the corresponding response values of these closest predictor values are calculated. In the case of classification, i.e. categorical response value, a voting rule is applied. The most frequent group (response value) is where the new observation is to be allocated.

This function does the cross-validation procedure to select the optimal k, the optimal number of nearest neighbours. The optimal in terms of some accuracy metric. For the classification it is the percentage of correct classification and for the regression the mean squared error.

### Value

A list including:

preds	If pred.ret is TRUE the predicted values for each fold are returned as elements in a list.
-------	--

**crit** A vector whose length is equal to the number of k and is the accuracy metric for each k. If you want to compute other metrics of accuracy we suggest you choose "pred.ret = TRUE" when running the function and then write a simple function to compute more metrics. See `col.accs()` or `colmses()` in the package **Rfast2**.

### Author(s)

Marios Dimitriadis

R implementation and documentation: Marios Dimitriadis <kmdimitriadis@gmail.com>

### References

Friedman J., Hastie T. and Tibshirani R. (2017). The elements of statistical learning. New York: Springer.

Cover TM and Hart PE (1967). Nearest neighbor pattern classification. IEEE Transactions on Information Theory. 13(1):21-27.

Tsagris Michail, Simon Preston and Andrew T.A. Wood (2016). Improved classification for compositional data using the  $\alpha$ -transformation. Journal of classification 33(2): 243-261.

### See Also

[knn](#), [Dist](#), [dista](#), [dirknn.cv](#)

### Examples

```
x <- as.matrix(iris[, 1:4])
y <- iris[, 5]
mod <- knn.cv(folds = NULL, n folds = 10, stratified = FALSE, seed = NULL, y = y, x = x,
k = c(3, 4), dist.type = "euclidean", type = "C", method = "average",
freq.option = 0, pred.ret = FALSE, mem.eff = FALSE)
```

---

Cross-Validation for the k-NN algorithm using the arc cosinus distance

*Cross-Validation for the k-NN algorithm using the arc cosinus distance*

---

### Description

Cross-Validation for the k-NN algorithm using the arc cosinus distance.

### Usage

```
dirknn.cv(y, x, k = 5:10, type = "C", folds = NULL, n folds = 10,
stratified = TRUE, seed = NULL, parallel = FALSE, pred.ret = FALSE)
```

**Arguments**

y	A vector of data. The response variable, which can be either continuous or categorical (factor is acceptable).
x	A matrix with the available data, the predictor variables.
k	A vector with the possible numbers of nearest neighbours to be considered.
type	If your response variable y is numerical data, then this should be "R" (regression) or "WR" for distance weighted based nearest neighbours. If y is in general categorical set this argument to "C" (classification) or to "WC" for distance weighted based nearest neighbours.
folds	A list with the indices of the folds.
nfolds	The number of folds to be used. This is taken into consideration only if "folds" is NULL.
stratified	Do you want the folds to be selected using stratified random sampling? This preserves the analogy of the samples of each group. Make this TRUE if you wish, but only for the classification. If you have regression (type = "R"), do not put this to TRUE as it will cause problems or return wrong results.
seed	If NULL different folds will be created every time. Otherwise set your own seed.
parallel	Do you want the calculations to take place in parallel? The default value is FALSE.
pred.ret	If you want the predicted values returned set this to TRUE.

**Details**

The concept behind k-NN is simple. Suppose we have a matrix with predictor variables and a vector with the response variable (numerical or categorical). When a new vector with observations (predictor variables) is available, its corresponding response value, numerical or categorical, is to be predicted. Instead of using a model, parametric or not, one can use this ad hoc algorithm.

The k smallest distances between the new predictor variables and the existing ones are calculated. In the case of regression, the average, median, or harmonic mean of the corresponding response values of these closest predictor values are calculated. In the case of classification, i.e. categorical response value, a voting rule is applied. The most frequent group (response value) is where the new observation is to be allocated.

This function does the cross-validation procedure to select the optimal k, the optimal number of nearest neighbours. The optimal in terms of some accuracy metric. For the classification it is the percentage of correct classification and for the regression the mean squared error.

**Value**

A list including:

preds	If pred.ret is TRUE the predicted values for each fold are returned as elements in a list.
crit	A vector whose length is equal to the number of k and is the accuracy metric for each k. For the classification case it is the percentage of correct classification. For the regression case the mean square of prediction error.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

Friedman J., Hastie T. and Tibshirani R. (2017). The elements of statistical learning. New York: Springer.

Cover TM and Hart PE (1967). Nearest neighbor pattern classification. IEEE Transactions on Information Theory. 13(1):21-27.

**See Also**

[dirknn](#), [knn.cv](#), [knn](#)

**Examples**

```
x <- as.matrix(iris[, 1:4])
x <- x / sqrt( Rfast::rowsums(x^2) )
y <- iris[, 5]
mod <- dirknn.cv(y = y, x = x, k = c(3, 4) )
```

---

Deep copy

*Deep copy*

---

**Description**

Deep copy.

**Usage**

```
env.copy(x, all.names=FALSE)
```

**Arguments**

<code>x</code>	An environment object.
<code>all.names</code>	An logical value (TRUE or FALSE). Copy all the hidden variables or not.

**Details**

Deep copy of the environment object.

**Value**

A copy of the first argument.

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colShuffle](#), [colVars](#), [colmeans](#)

**Examples**

```
x <- new.env()
x$imaginary <- NULL
x$real <- NULL

# you can library the package and just press x and R will understand
# and search automatically for a function to print the environment
x

y <- env.copy(x)

x$real <- 10

x$real == y$real # FALSE
```

---

Density of the multivariate normal and t distributions

*Density of the multivariate normal and t distributions*

---

**Description**

Density of the multivariate normal and t distributions.

**Usage**

```
dmvnorm(x, mu, sigma, logged = FALSE)
dmvt(x, mu, sigma, nu, logged = FALSE)
```

**Arguments**

x	A numerical matrix with the data. The rows correspond to observations and the columns to variables.
mu	The mean vector.
sigma	The covariance matrix.
nu	The degrees of freedom for the multivariate t distribution.
logged	Should the logarithm of the density be returned (TRUE) or not (FALSE)?

**Details**

The (log) density of the multivariate normal distribution is calculated for given mean vector and covariance matrix.

**Value**

A numerical vector with the density values calculated at each vector (row of the matrix *x*).

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Kanti V. Mardia, John T. Kent and John M. Bibby (1979). Multivariate analysis. Academic Press, London.

**See Also**

[rmvnorm](#), [rmvt](#), [mvnorm.mle](#), [iag.mle](#)

**Examples**

```
x <- matrnorm(100, 20)
mu <- colmeans(x)
s <- cova(x)
#1 <- dmnorm(x, mu, s)
#2 <- dmvt(x, mu, s, 1)
x <- NULL
```

---

Design Matrix

*Design Matrix*

---

**Description**

Design Matrix.

**Usage**

```
design_matrix(x, ones = TRUE)
```

**Arguments**

<i>x</i>	A character vector or a factor type vector or a dataframe. Do not supply a numerical vector.
<i>ones</i>	A boolean variable specifying whether to include the ones in the design matrix or not. The default value is TRUE.

**Details**

This function implements the R's "model.matrix" function and is used only when the x is a factor/charactervector or Dataframe.

**Value**

Returns the same matrix with model.matrix.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>

**See Also**

[model.matrix](#)

**Examples**

```
a <- design_matrix( iris[, 5] )
b <- model.matrix( ~ iris[,5] ) ## R's built-in function
all.equal(as.vector(a),as.vector(b)) ## true

a<-b<-NULL
```

---

Diagonal Matrix

*Diagonal Matrix*

---

**Description**

Fill the diagonal of a matrix or create a diagonal and initialize it with a specific value.

**Usage**

```
Diag.fill(x,v=0)
Diag.matrix(len,v=0)
```

**Arguments**

x	A matrix with data.
len	Number of columns or rows.
v	Value or vector to initialize the diagonal of a matrix.By default "v=0".

**Value**

Diag.fill returns a diagonal matrix where all the elements in the diagonal are equal to "v".

Diag.matrix returns a diagonal matrix where has dimension "len,len" and all the elements in the diagonal are equal to "v". It is fast for huge matrices with dimensions more than [row,col] = [500,500]

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis &lt;papadakm95@gmail.com&gt;.

**See Also**[rowMins](#), [colFalse](#), [nth](#), [rowrange](#), [rowMedians](#), [rowVars](#), [colSort](#), [rowSort](#), [colTrue](#)**Examples**

```
x <- matrix(rbinom(100*100,1,0.5),100,100)

f <- Diag.fill(x,1)
f <- Diag.fill(x,1:100) ##equals to diag(x)<-1:100
f <- Diag.matrix(100,1) ##equals to diag(1,100,100)
f <- Diag.matrix(100,1:100) ##equals to diag(1:100,100,100)

f<-x<-NULL
```

---

Distance between vectors and a matrix - Sum of all pairwise distances  
in a distance matrix.

*Distance between vectors and a matrix - Sum of all pairwise distances  
in a distance matrix*

---

**Description**

Distance between vectors and a matrix - Sum of all pairwise distances in a distance matrix..

**Usage**

```
dista(xnew, x, type = "euclidean", k = 0, index = FALSE,
      trans = TRUE, square = FALSE, p = 0, result = "matrix", parallel = FALSE)
total.dista(xnew, x, type = "euclidean", k = 0,
            square = FALSE, p = 0, parallel = FALSE)
```

**Arguments**

xnew	A matrix with some data or a vector.
x	A matrix with the data, where rows denotes observations (vectors) and the columns contain the variables.
type	This can be either "euclidean" or "manhattan".
k	Should the k smaller distances or their indices be returned? If k > 0 this will happen.
index	In case k is greater than 0, you have the option to get the indices of the k smallest distances.

trans	Do you want the returned matrix to be transposed? TRUE or FALSE.
square	If you choose "euclidean" or "hellinger" as the method, then you can have the option to return the squared Euclidean distances by setting this argument to TRUE.
p	This is for the the Minkowski, the power of the metric.
parallel	For methods <b>kullback_leibler</b> , <b>jensen_shannon</b> and <b>itakura_saito</b> , you can run the algorithm in parallel.
result	One of the: <ul style="list-style-type: none"> <li>• "matrix" : Return the result as matrix</li> <li>• "vector" : Return the result as vector</li> <li>• "sum" : Return the sum of the result</li> </ul>

## Details

The target of this function is to calculate the distances between xnew and x without having to calculate the whole distance matrix of xnew and x. The latter does extra calculations, which can be avoided.

- euclidean :  $\sum \sqrt{(\sum |P_i - Q_i|^2)}$
- manhattan :  $\sum \sum |P_i - Q_i|$
- minimum :  $\sum \min |P_i - Q_i|$
- maximum :  $\sum \max |P_i - Q_i|$
- minkowski :  $\sum (\sum |P_i - Q_i|^p)^{\frac{1}{p}}$
- bhattacharyya :  $\sum -\ln \sum \sqrt{P_i * Q_i}$
- hellinger :  $\sum 2 * \sqrt{1 - \sum \sqrt{P_i * Q_i}}$
- kullback\_leibler :  $\sum \sum P_i * \log(\frac{P_i}{Q_i})$
- jensen\_shannon :  $\sum 0.5 * (\sum P_i * \log(2 * \frac{P_i}{Q_i} + Q_i) + \sum Q_i * \log(2 * \frac{Q_i}{P_i} + Q_i))$
- canberra :  $\sum \sum \frac{|P_i - Q_i|}{P_i + Q_i}$
- chi\_square  $X^2$  :  $\sum \sum (\frac{(P_i - Q_i)^2}{P_i + Q_i})$
- soergel :  $\sum \frac{\sum |P_i - Q_i|}{\sum \max(P_i, Q_i)}$
- sorensen :  $\sum \frac{\sum |P_i - Q_i|}{\sum (P_i + Q_i)}$
- cosine :  $\sum \frac{\sum (P_i * Q_i)}{\sqrt{(\sum P_i^2) * \sqrt{(\sum Q_i^2)}}$
- wave\_hedges :  $\sum \frac{\sum |P_i - Q_i|}{\max(P_i, Q_i)}$
- motyka :  $\sum \sum \frac{\min(P_i, Q_i)}{(P_i + Q_i)}$
- harmonic\_mean :  $\sum 2 * \frac{\sum P_i * Q_i}{P_i + Q_i}$
- jeffries\_matusita :  $\sum \sqrt{2 - 2 * \sum \sqrt{P_i * Q_i}}$
- gower :  $\sum \frac{1}{d} * \sum |P_i - Q_i|$
- kulczynski :  $\sum \frac{\sum |P_i - Q_i|}{\sum \min(P_i, Q_i)}$
- itakura\_saito :  $\sum \frac{P_i}{Q_i} - \log(\frac{P_i}{Q_i}) - 1$

**Value**

A matrix with the distances of each `xnew` from each vector of `x`. The number of rows of the `xnew` and the number of columns of `xnew` are the dimensions of this matrix.

**Author(s)**

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[mahala](#), [Dist](#), [total.dist](#), [total.dista](#)

**Examples**

```
xnew <- as.matrix( iris[1:10, 1:4] )
x <- as.matrix( iris[-c(1:10), 1:4] )
a <- dista(xnew, x)
b <- as.matrix( dist( rbind(xnew, x) ) )
b <- b[ 1:10, -c(1:10) ]
sum( abs(a - b) )

## see the time
x <- matrix( rnorm(1000 * 4), ncol = 4 )
dista(xnew, x)
as.matrix( dist( rbind(xnew, x) ) )

x<-b<-a<-xnew<-NULL
```

---

Distance matrix - Sum of all pairwise distances in a distance matrix

*Distance matrix - Sum of all pairwise distances in a distance matrix*

---

**Description**

Distance matrix - Sum of all pairwise distances in a distance matrix.

**Usage**

```
Dist(x,method = "euclidean", square = FALSE,p=0,
     result = "matrix" ,vector = FALSE, parallel = FALSE)
total.dist(x, method = "euclidean", square = FALSE, p = 0)
vecdist(x)
```

**Arguments**

x	A matrix with data. The distances will be calculated between pairs of rows. In the case of <b>vecdist</b> this is a vector. For the <b>haversine</b> distance it must be a matrix with two columns, the first column is the latitude and the second the longitude (in radians).
method	See details for the available methods.
square	If you choose "euclidean" or "hellinger" as the method, then you can have the option to return the squared Euclidean distances by setting this argument to TRUE.
p	This is for the Minkowski method, the power of the metric.
vector	For return a vector instead a matrix.
result	One of the: <ul style="list-style-type: none"> <li>• "matrix" : Return the result as matrix.</li> <li>• "vector" : Return the result as vector.</li> <li>• "sum" : Return the sum of the result.</li> </ul>
parallel	For methods <b>euclidean</b> , <b>canberra</b> and <b>minkowski</b> , you can run the algorithm in parallel.

**Details**

The distance matrix is compute with an extra argument for the Euclidean distances. The "kullback\_leibler" refers to the symmetric Kullback-Leibler divergence.

- euclidean :  $\sum \sqrt{(\sum |P_i - Q_i|^2)}$
- manhattan :  $\sum |P_i - Q_i|$
- minimum :  $\sum \min |P_i - Q_i|$
- maximum :  $\sum \max |P_i - Q_i|$
- minkowski :  $(\sum |P_i - Q_i|^p)^{\frac{1}{p}}$
- bhattacharyya :  $-\ln(\sum \sqrt{(P_i * Q_i)})$
- hellinger :  $2 * \sqrt{1 - \sum \sqrt{(P_i * Q_i)}}$
- kullback\_leibler :  $\sum P_i * \log(\frac{P_i}{Q_i})$
- jensen\_shannon :  $0.5 * (\sum P_i * \log(2 * \frac{P_i}{Q_i + Q_i}) + \sum Q_i * \log(2 * \frac{Q_i}{P_i + Q_i}))$
- canberra :  $\sum \frac{|P_i - Q_i|}{P_i + Q_i}$
- chi\_square  $X^2$  :  $\sum (\frac{(P_i - Q_i)^2}{P_i + Q_i})$
- soergel :  $\frac{\sum |P_i - Q_i|}{\sum \max(P_i, Q_i)}$
- sorensen :  $\frac{\sum |P_i - Q_i|}{\sum (P_i + Q_i)}$
- cosine :  $\sum \frac{\sum (P_i * Q_i)}{\sqrt{(\sum P_i^2)} * \sqrt{(\sum Q_i^2)}}$
- wave\_hedges :  $\sum \frac{\sum |P_i - Q_i|}{\max(P_i, Q_i)}$
- motyka :  $\sum \frac{\min(P_i, Q_i)}{(P_i + Q_i)}$

- `harmonic_mean` :  $2 * \frac{\sum P_i * Q_i}{P_i + Q_i}$
- `jeffries_matusita` :  $\sum \sqrt{(2 - 2 * \sum \sqrt{(P_i * Q_i)})}$
- `gower` :  $\sum \frac{1}{d} * \sum |P_i - Q_i|$
- `kulczynski` :  $\sum \frac{\sum |P_i - Q_i|}{\sum \min(P_i, Q_i)}$
- `itakura_saito` :  $\sum \frac{P_i}{Q_i} - \log(\frac{P_i}{Q_i}) - 1$
- `haversine` :  $2 * R * \arcsin(\sqrt{(\sin((lat_2 - lat_1)/2))^2 + \cos(lat_1) * \cos(lat_2) * \sin((lon_2 - lon_1)/2)^2})$

**Value**

A square matrix with the pairwise distances.

**Author(s)**

Manos Papadakis.

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**References**

Mardia K. V., Kent J. T. and Bibby J. M. (1979). *Multivariate Analysis*. Academic Press.

**See Also**

[dista](#), [colMedians](#)

**Examples**

```
x <- matrix(rnorm(50 * 10), ncol = 10)
a1 <- Dist(x)
a2 <- as.matrix( dist(x) )

x<-a1<-a2<-NULL
```

---

Distance variance, covariance and correlation

*Distance variance, covariance and correlation*

---

**Description**

Distance variance, covariance and correlation.

**Usage**

```
dvar(x, bc = FALSE)
dcov(x, y, bc = FALSE)
dcor(x, y, bc = FALSE)
bcdcor(x, y)
```

**Arguments**

x	A numerical matrix or a vector.
y	A numerical matrix or a vector.
bc	If you want the bias-corrected distance correlation set this equal to TRUE.

**Details**

The distance variance of a matrix/vector, the distance covariance or distance correlation of two matrices is calculated. For the `dcov()` and `dcor()`, if `x` and `y` are matrices, they must have the same dimensions. We have optimized the code, using the formulas provided in Szekely and Rizzo (2023), but only for the case that both matrices are of the same dimensionality.

**Value**

The distance covariance or the distance variance.  
For the bias corrected distance correlation its value only.  
For the distance correlation a list including:

<code>dcov</code>	The distance covariance.
<code>dvarX</code>	The distance variance of <code>x</code> .
<code>dvarY</code>	The distance variance of <code>Y</code> .
<code>dcor</code>	The distance correlation.

**Author(s)**

Michail Tsagris and Manos Papadakis.

R implementation and documentation: Michail Tsagris <[mtsagris@uoc.gr](mailto:mtsagris@uoc.gr)> and Manos Papadakis <[papadakm95@gmail.com](mailto:papadakm95@gmail.com)>.

**References**

Szekely G.J., Rizzo M.L. and Bakirov N.K.(2007). Measuring and Testing Independence by Correlation of Distances. *Annals of Statistics*, 35(6):2769–2794.

Szekely G. J. and Rizzo M. L. (2023). *The Energy of Data and Distance Correlation*. Chapman and Hall/CRC.

Tsagris M. and Papadakis M. (2025). Fast and light-weight energy statistics using the R package Rfast. <https://arxiv.org/abs/2501.02849>

**See Also**

[pdcor](#), [dcor.ttest](#), [edist](#)

**Examples**

```
x <- as.matrix(iris[1:50, 1:4])
y <- as.matrix(iris[51:100, 1:4])
res <- dvar(x[, 1])
#dcor(x, y)
```

---

Eigenvalues and eigenvectors in high dimensional principal component analysis

*Eigenvalues in high dimensional principal component analysis*

---

### Description

Eigenvalues in high dimensional ( $n \ll p$ ) principal component analysis.

### Usage

```
hd.eigen(x, center = TRUE, scale = FALSE, k = NULL, vectors = FALSE, large = FALSE)
```

### Arguments

x	A numerical $n \times p$ matrix with data where the rows are the observations and the columns are the variables.
center	Do you want your data centered? TRUE or FALSE.
scale	Do you want each of your variables scaled, i.e. to have unit variance? TRUE or FALSE.
k	If you want a specific number of eigenvalues and eigenvectors set it here, otherwise all eigenvalues (and eigenvectors if requested) will be returned.
vectors	Do you want the eigenvectors be returned? By default this is FALSE.
large	If you have large matrices, with thousands of rows and or many tens or hundreds of columns set this equal to TRUE in order to use Rfast's <a href="#">Crossprod</a> or <a href="#">Tcrossprod</a> functions. These functions are twice or up to 3 times faster than the corresponding built-in functions.

### Details

When  $n \ll p$ , at most the first  $n$  eigenvalues are non zero. Hence, there is no need to calculate the other  $p-n$  zero eigenvalues. When center is TRUE, the eigenvalues of the covariance matrix are calculated. When both the center and scale is TRUE the eigenvalues of the correlation matrix are calculated. One or more eigenvectors (towards the end) will be 0. In general the signs might be the opposite than R's, but this makes no difference. We use the [Crossprod](#) instead of the relevant built-in function. The higher the dimensions of the matrix are the faster this function becomes.

### Value

A list including:

values	A vector with the $n$ (or first $k$ ) eigenvalues. The divisor in the crossprod matrix is $n-1$ and not $n$ .
vectors	A matrix of $p \times n$ or $p \times k$ eigenvectors.

**Author(s)**

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**See Also**

[rmdp](#)

**Examples**

```
x <- matnorm(20, 50)
#a <- hd.eigen(x, FALSE, FALSE)
#b <- prcomp(x, center = FALSE, scale = FALSE)
#a
#b$sdev^2
#x <- NULL
```

---

Empirical and exponential empirical likelihood tests for one sample

*Empirical and exponential empirical likelihood tests for one sample*

---

**Description**

Empirical and exponential empirical likelihood tests for one sample.

**Usage**

```
eel.test1(x, mu, tol = 1e-09, logged = FALSE)
el.test1(x, mu, tol = 1e-07, logged = FALSE)
```

**Arguments**

x	A numerical vector.
mu	The hypothesised mean value.
tol	The tolerance value to stop the iterations of the Newton-Raphson.
logged	Should the logarithm of the p-value be returned? TRUE or FALSE.

**Details**

Exponential empirical likelihood is a non parametric method. In this case we use it as the non parametric alternative to the t-test. Newton-Raphson is used to maximise the log-likelihood ratio test statistic. In the case of no solution, NULL is returned. Despite the function having been written in R, it is pretty fast. As for the empirical likelihood ratio test, there is a condition for the range of possible values of mu. If mu is outside this range it is rejected immediately.

**Value**

<code>iters</code>	The number of iterations required by the Newton-Raphson algorithm. If no convergence occurred this is NULL. This is not returned for the empirical likelihood ratio test.
<code>info</code>	A vector with three elements, the value of the $\lambda$ , the likelihood ratio test statistic and the relevant p-value. If no convergence occurred, the value of the $\lambda$ before is becomes NA, the value of test statistic is $10^5$ and the p-value is 0. No convergence can be interpreted as rejection of the hypothesis test.
<code>p</code>	The estimated probabilities, one for each observation. If no convergence occurred this is NULL.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Owen A. B. (2001). Empirical likelihood. Chapman and Hall/CRC Press.

**See Also**

[fctest](#), [ttest1](#)

**Examples**

```
x <- rnorm(500)
a1 <- eel.test1(x, 0)
a2 <- el.test1(x, 0)
```

---

Empirical and exponential empirical likelihood tests for two samples  
*Empirical and exponential empirical likelihood tests for two samples*

---

**Description**

Empirical and exponential empirical likelihood tests for two samples.

**Usage**

```
eel.test2(x, y, tol = 1e-09, logged = FALSE)
el.test2(x, y, tol = 1e-07, logged = FALSE)
```

**Arguments**

x	A numerical vector.
y	Another numerical vector.
tol	The tolerance value to stop the iterations of the Newton-Raphson.
logged	Should the logarithm of the p-value be returned? TRUE or FALSE.

**Details**

Empirical and exponential empirical likelihood are two non parametric hypothesis testing methods. We can use them as non parametric alternatives to the t-test. Newton-Raphson is used to maximise the log-likelihood ratio test statistic. In the case of no solution, NULL is returned.

**Value**

iters	The number of iterations required by the Newton-Raphson algorithm. If no convergence occurred this is NULL.
info	A vector with three elements, the value of the $\lambda$ , the likelihood ratio test statistic and the relevant p-value. If no convergence occurred, the value of the $\lambda$ before is becomes NA, the value of test statistic is $10^5$ and the p-value is 0. No convergence can be interpreted as rejection of the hypothesis test.
p1	The estimated probabilities, one for each observation for the first sample. If no convergence occurred this is NULL.
p2	The estimated probabilities, one for each observation for the second sample. If no convergence occurred this is NULL.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Owen A. B. (2001). Empirical likelihood. Chapman and Hall/CRC Press.

**See Also**

[ftests](#), [ttests](#), [ttest](#)

**Examples**

```
x <- rnorm(200)
y <- rnorm(300)
eel.test2(x, y)
el.test2(x, y)
```

---

Energy distance between matrices

*Energy distance between matrices*

---

## Description

Energy distance between matrices.

## Usage

```
edist(x, y = NULL)
```

## Arguments

x	A matrix with numbers or a list with matrices.
y	A second matrix with data. The number of columns of x and y must match. The number of rows can be different.

## Details

This calculates the energy distance between two matrices. It will work even for tens of thousands of rows, it will just take some time. See the references for more information. If you have many matrices and want to calculate the distance matrix, then put them in a list and use the function.

## Value

If "x" is matrix, a numerical value, the energy distance. If "x" is list, a matrix with all pairwise distances of the matrices.

## Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

## References

- Szekely G. J. and Rizzo M. L. (2004) Testing for Equal Distributions in High Dimension, InterStat, November (5).
- Szekely G. J. (2000) Technical Report 03-05, E-statistics: Energy of Statistical Samples, Department of Mathematics and Statistics, Bowling Green State University.
- Sejdinovic D., Sriperumbudur B., Gretton A. and Fukumizu, K. (2013). Equivalence of distance-based and RKHS-based statistics in hypothesis testing. *The Annals of Statistics*, 41(5): 2263–2291.
- Szekely G. J. and Rizzo M. L. (2023). *The Energy of Data and Distance Correlation*. Chapman and Hall/CRC.
- Tsagris M. and Papadakis M. (2025). Fast and light-weight energy statistics using the R package Rfast. <https://arxiv.org/abs/2501.02849>

**See Also**

[dcov](#), [Dist](#), [dista](#)

**Examples**

```
x <- as.matrix( iris[1:50, 1:4] )
y <- as.matrix( iris[51:100, 1:4] )
res<-edist(x, y)
z <- as.matrix(iris[101:150, 1:4])
a <- list()
a[[ 1 ]] <- x
a[[ 2 ]] <- y
a[[ 3 ]] <- z
res<-edist(a)

x<-y<-z<-a<-NULL
```

---

Estimation of an AR(1) model

*Estimation of an AR(1) model*

---

**Description**

Estimation of an AR(1) model.

**Usage**

```
ar1(y, method = "cmle")
colar1(y, method = "cmle")
```

**Arguments**

y	For the case of <b>ar1</b> this is a vector of time series. For the case of <b>colar1</b> this is a matrix where weach column represents a time series.
method	This can be either "cmle" for conditional maximum likelihood or "yw" for the Yule-Walker equations.

**Details**

Instead of the classical MLE for the AR(1) model which requires numerical optimisation (Newton-Raphson for example) we estimate the parameters of the AR(1) model using conditional maximum likelihood. This procedure is described in Chapter 17 in Lee (2006). In some, it assumes that the first observation is deterministic and hence conditioning on that observation, there is a closed form solution for the parameters. The second alternative is to use the method of moments and hence the Yule-Walker equations.

**Value**

param For the case of **ar1** this is a vector with three elements, the constant term, the  $\phi$  term (lag coefficient) and the variance. For the case of **colar1** this is a matrix with three columns, each of which carries the same aforementioned elements.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

[http://econ.nsysu.edu.tw/ezfiles/124/1124/img/Chapter17\\_MaximumLikelihoodEstimation.pdf](http://econ.nsysu.edu.tw/ezfiles/124/1124/img/Chapter17_MaximumLikelihoodEstimation.pdf)

**See Also**

[rm.lines](#), [varcomps.mle](#), [rm.anovas](#)

**Examples**

```
y <- as.vector(1h)
ar1(y)
ar(y, FALSE, 1, "ols")

ar1(y, method = "yw")
ar(y, FALSE, 1, "yw")

a1 <- colar1(cbind(y, y) )
b1 <- colar1(cbind(y, y), method = "yw")
```

---

Estimation of the Box-Cox transformation

*Estimation of the Box-Cox transformation*

---

**Description**

Estimation of the Box-Cox transformation.

**Usage**

```
bc(x, low = -1, up = 1)
```

**Arguments**

x A numerical vector with strictly positive values.  
low The lowest value to search for the best  $\lambda$  parameter.  
up The highest value to search for the best  $\lambda$  parameter.

### Details

The functions estimates the best  $\lambda$  in the Box-Cox power transformation.

### Value

The optimal value of  $\lambda$ .

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

### References

Box George E. P. and Cox D. R. (1964). An analysis of transformations. Journal of the Royal Statistical Society, Series B, 26 (2):211-252.

### See Also

[correls](#), [auc](#)

### Examples

```
x <- exp(rnorm(1000))
res<-bc(x)
```

---

Exact t-test for 2 independent samples  
*Exact t-test for 2 independent samples*

---

### Description

Exact t-test for 2 independent samples.

### Usage

```
exact.ttest2(x, y)
```

### Arguments

x	A numerical vector with the data.
y	A numerical vector with the data.

**Details**

This function performs an exact t-test. With few observations, permutation or bootstrap calculation of the p-value is advisable. However, with even fewer observations, one can perform all possible permutations and calculate the exact p-value. This is what this function does. BUT, pay attention, as this works with few samples. If for example each sample contains 15 numbers, you will need a lot of memory (more than 17 GB) for this function to work. the reason is that we create the matrix with all possible permutations first and then perform the two-sample t-test.

**Value**

A vector with the number of permutations, test statistic and the permutation based p-value.

**Author(s)**

Michail Tsagris and Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

**References**

B.L. Welch (1951). On the comparison of several mean values: an alternative approach. *Biometrika*, 38(3/4), 330-336.

**See Also**

[boot.ttest2](#), [ttest2](#), [ftest](#)

**Examples**

```
x <- rnorm(7)
y <- rnorm(7)
res<-exact.ttest2(x, y)
```

---

Exponential empirical likelihood for a one sample mean vector hypothesis testing

*Exponential empirical likelihood for a one sample mean vector hypothesis testing*

---

**Description**

Exponential empirical likelihood for a one sample mean vector hypothesis testing.

**Usage**

```
mv.eeltest1(x, mu, tol = 1e-06)
```

**Arguments**

<code>x</code>	A matrix containing Euclidean data.
<code>mu</code>	The hypothesized mean vector.
<code>tol</code>	The tolerance value used to stop the Newton-Raphson algorithm.

**Details**

Multivariate hypothesis test for a one sample mean vector. This is a non parametric test and it works for univariate and multivariate data. The p-value is currently computed only asymptotically (no bootstrap calibration at the moment).

**Value**

A list including:

<code>p</code>	The estimated probabilities.
<code>lambda</code>	The value of the Lagrangian parameter $\lambda$ .
<code>iters</code>	The number of iterations required by the newton-Raphson algorithm.
<code>info</code>	The value of the log-likelihood ratio test statistic along with its corresponding p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

Jing Bing-Yi and Andrew TA Wood (1996). Exponential empirical likelihood is not Bartlett correctable. *Annals of Statistics* 24(1): 365-369.

Owen A. B. (2001). *Empirical likelihood*. Chapman and Hall/CRC Press.

**See Also**

[james](#), [mv.eeltest2](#)

**Examples**

```
x <- Rfast::rmvnorm(100, numeric(10), diag( rexp(10, 0.5) ) )
res<-mv.eeltest1(x, numeric(10) )
```

---

Exponential empirical likelihood hypothesis testing for two mean vectors

*Exponential empirical likelihood hypothesis testing for two mean vectors*

---

### Description

Exponential empirical likelihood hypothesis testing for two mean vectors.

### Usage

```
mv.eeltest2(y1, y2, tol = 1e-07, R = 0)
```

### Arguments

y1	A matrix containing the Euclidean data of the first group.
y2	A matrix containing the Euclidean data of the second group.
tol	The tolerance level used to terminate the Newton-Raphson algorithm.
R	If R is 0, the classical chi-square distribution is used, if R = 1, the corrected chi-square distribution (James, 1954) is used and if R = 2, the modified F distribution (Krishnamoorthy and Yanping, 2006) is used.

### Details

Exponential empirical likelihood is a non parametric hypothesis testing procedure for one sample. The generalisation to two (or more samples) is via searching for the mean vector that minimises the sum of the two test statistics.

### Value

A list including:

test	The empirical likelihood test statistic value.
modif.test	The modified test statistic, either via the chi-square or the F distribution.
pvalue	The p-value.
iters	The number of iterations required by the newton-Raphson algorithm.
mu	The estimated common mean vector.

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

- Jing Bing-Yi and Andrew TA Wood (1996). Exponential empirical likelihood is not Bartlett correctable. *Annals of Statistics* 24(1): 365-369.
- G.S. James (1954). Tests of Linear Hypotheses in Univariate and Multivariate Analysis when the Ratios of the Population Variances are Unknown. *Biometrika*, 41(1/2): 19-43.
- Krishnamoorthy K. and Yanping Xia (2006). On Selecting Tests for Equality of Two Normal Mean Vectors. *Multivariate Behavioral Research* 41(4): 533-548.
- Owen A. B. (2001). Empirical likelihood. Chapman and Hall/CRC Press.
- Amaral G.J.A., Dryden I.L. and Wood A.T.A. (2007). Pivotal bootstrap methods for k-sample problems in directional statistics and shape analysis. *Journal of the American Statistical Association* 102(478): 695-707.
- Preston S.P. and Wood A.T.A. (2010). Two-Sample Bootstrap Hypothesis Tests for Three-Dimensional Labelled Landmark Data. *Scandinavian Journal of Statistics* 37(4): 568-587.
- Tsagris M., Preston S. and Wood A.T.A. (2017). Nonparametric hypothesis testing for equality of means on the simplex. *Journal of Statistical Computation and Simulation*, 87(2): 406-422.

**See Also**

[james](#), [mv.eeltest1](#)

**Examples**

```
res<-mv.eeltest2( as.matrix(iris[1:25, 1:4]), as.matrix(iris[26:50, 1:4]), R = 0 )
res<-mv.eeltest2( as.matrix(iris[1:25, 1:4]), as.matrix(iris[26:50, 1:4]), R = 1 )
```

---

Fast and general - untyped representation of a factor variable  
*Fast and general representation of a factor variable*

---

**Description**

Fast and general representation of a factor variable.

**Usage**

```
ufactor(x)
## S3 method for class 'ufactor'
x[i]
## S3 method for class 'ufactor'
print(x,...)
```

**Arguments**

x	A vector with data.
i	An integer value/vector which is the index/indices to the element you want to access.
...	Anything the user want.

**Details**

This is a general implementation of factor structure. For access the fields of a "ufactor" use the "\$" operator.

**Value**

An object of class "ufactor". This object holds 2 fields:  
levels: the levels of the variable in his initial type values: the values of the variable in his initial type

**Author(s)**

Manos Papadakis

R implementation and documentation: and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colVars](#), [factor](#)

**Examples**

```
x <- rnorm(10)
R.factor<- as.factor(x)
Rfast.factor <- ufactor(x)

identical(levels(R.factor),Rfast.factor$levels) # TRUE
identical(as.numeric(R.factor),Rfast.factor$values) # TRUE
x<-R.factor<-Rfast.factor<-NULL
```

---

FBED variable selection method using the correlation

*FBED variable selection method using the correlation*

---

**Description**

FBED variable selection method using the correlation.

**Usage**

```
cor.fbed(y, x, ystand = TRUE, xstand = TRUE, alpha = 0.05, K = 0)
```

**Arguments**

y	The response variable, a numeric vector.
x	A matrix with the data, where the rows denote the samples and the columns are the variables.
ystand	If this is TRUE the response variable is centered. The mean is subtracted from every value.

xstand	If this is TRUE the independent variables are standardised.
alpha	The significance level, set to 0.05 by default.
K	The number of times to repeat the process. The default value is 0.

### Details

FBED stands for Forward Backward with Early Dropping. It is a variation of the classical forward selection, where at each step, only the statistically significant variables carry on. The rest are dropped. The process stops when no other variables can be selected. If  $K = 1$ , the process is repeated testing sequentially again all those that have not been selected. If  $K > 1$ , then this is repeated.

In the end, the backward selection is performed to remove any falsely included variables. This backward phase has not been implemented yet.

### Value

A list including:

runtime	The duration of the process.
res	A matrix with the index of the selected variable, their test statistic value and the associated p-value.
info	A matrix with two columns. The cumulative number of variables selected and the number of tests for each value of $K$ .

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

### References

Borboudakis G. and Tsamardinos I. (2019). Forward-backward selection with early dropping. *Journal of Machine Learning Research*, 20(8): 1-39.

### See Also

[cor.fsreg](#), [ompr](#), [correls](#), [fs.reg](#)

### Examples

```
x <- matnorm(100, 100)
y <- rnorm(100)
a <- cor.fbed(y, x)
a
x <- NULL
```

---

Find element

*Find element*

---

### Description

Search a value in an unordered vector.

### Usage

```
is_element(x, key)
```

### Arguments

x	A vector or matrix with the data.
key	A value to check if exists in the vector x.

### Details

Find if the key exists in the vector and return returns TRUE/FALSE if the value is been found. If the vector is unordered it is fast but if the vector is ordered then use `binary_search`. The functions is written in C++ in order to be as fast as possible.

### Value

TRUE/FALSE if the value is been found.

### Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

### See Also

[binary\\_search](#) (built-in R function)

### Examples

```
x <- rnorm(500)
key <- x[50]
b <- is_element(x, key)
```

---

Find the given value in a hash table

*Find the given value in a hash table*

---

## Description

Find the given value in a hash table or list.

## Usage

```
hash.find(x, key)
```

## Arguments

x	A hash table or list.
key	The key for searching the table.

## Details

This function search the given key.

## Value

If the given key exists return its value else returns 0.

## Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>

## See Also

[hash.list](#)

## Examples

```
x <- hash.list(letters, c(1:26))
value <- hash.find(x, "a")
x[["a"]] == value
```

---

Fitted probabilities of the Terry-Bradley model

*Fitted probabilities of the Terry-Bradley model*

---

### Description

Fitted probabilities of the Terry-Bradley model.

### Usage

```
btmprobs(x, tol = 1e-09)
```

### Arguments

x	A numerical square, usually not symmetric, matrix with discrete valued data. Each entry is a frequency, to give an example, the number of wins. $x[i, j]$ is the number of wins of home team $i$ against guest team $j$ . $x[j, i]$ is the number of wins of home team $j$ against guest team $i$ .
tol	The tolerance level to terminate the iterative algorithm.

### Details

It fits a Bradley-Terry model to the given matrix and returns the fitted probabilities only.

### Value

A list including:

iters	The number of iterations required.
probs	A vector with probabilities which sum to 1. This is the probability of win for each item (or team in our hypothetical example).

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

### References

Bradley R.A. and Terry M.E. (1952). Rank Analysis of Incomplete Block Designs: I. The Method of Paired Comparisons. *Biometrika*, 39(3/4):324-345.

Huang Tzu-Kuo, Ruby C. Weng and Chih-Jen Lin (2006). Generalized Bradley-Terry models and multi-class probability estimates. *Journal of Machine Learning Research*, 7:85-115.

Agresti A. (2002). *Categorical Data Analysis* (2nd ed). New York: Wiley.

**See Also**

[g2tests](#), [poisson.anova](#), [anova](#), [poisson\\_only](#), [poisson.mle](#)

**Examples**

```
x <- matrix( rpois(10 * 10, 10), ncol = 10) ## not the best example though
res<-btmprobs(x)
```

---

Fitting a Dirichlet distribution via Newton-Rapshon

*Fitting a Dirichlet distribution via Newton-Rapshon*

---

**Description**

Fitting a Dirichlet distribution via Newton-Rapshon.

**Usage**

```
diri.nr2(x, type = 1, tol = 1e-07)
```

**Arguments**

x	A matrix containing the compositional data. Zeros are not allowed.
type	Type 1 uses a vectorised version of the Newton-Raphson (Minka, 2012). In high dimensions this is to be preferred. If the data are too concentrated, regardless of the dimensions, this is also to be preferred. Type 2 uses the regular Newton-Raphson, with matrix multiplications. In small dimensions this can be considerably faster.
tol	The tolerance level indicating no further increase in the log-likelihood.

**Details**

Maximum likelihood estimation of the parameters of a Dirichlet distribution is performed via Newton-Raphson. Initial values suggested by Minka (2012) are used.

**Value**

A list including:

loglik	The value of the log-likelihood.
param	The estimated parameters.

**Author(s)**

Michail Tsagris and Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

## References

- Minka Thomas (2012). Estimating a Dirichlet distribution. Technical report.
- Ng Kai Wang, Guo-Liang Tian, and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

## See Also

[beta.mle](#)

## Examples

```
x <- matrix( rgamma(100 * 4, c(5, 6, 7, 8), 1), ncol = 4)
x <- x / rowsums(x)
res<-diri.nr2(x)
```

---

Floyd-Warshall algorithm

*Floyd-Warshall algorithm for shortest paths in a directed graph*

---

## Description

Floyd-Warshall algorithm for shortest paths in a directed graph.

## Usage

```
floyd(x)
```

## Arguments

**x** The adjacency matrix of a directed graph. A positive number (including) in  $x[i, j]$  indicates that there is an arrow from  $i$  to  $j$  and it also shows the cost of going from  $i$  to  $j$ . Hence, the algorithm will find not only the shortest path but also the with the smallest cost. A value of NA means that there is no path. Put positive number only, as negative will cause problems.

## Details

The Floyd-Warshall algorithm is designed to find the shortest path (if it exists) between two nodes in a graph.

## Value

A matrix, say  $z$ , with 0 and positive numbers. The elements denote the length of the shortest path between each pair of points. If  $z[i, j]$  is zero it means that there is no cost from  $i$  to  $j$ . If  $z[i, j]$  has a positive value it means that the length of going from  $i$  to  $j$  is equal to that value.

**Author(s)**

John Burkardt (C++ code)

Ported into R and documentation: Manos Papadakis <papadakm95@gmail.com>.

**References**

Floyd, Robert W. (1962). Algorithm 97: Shortest Path. Communications of the ACM. 5(6): 345.

Warshall, Stephen (1962). A theorem on Boolean matrices. Journal of the ACM. 9 (1): 11-12.

<https://en.wikipedia.org/wiki/Floyd>

**See Also**

[colSort](#), [rowSort](#)

**Examples**

```
x <- matrix(NA, 10, 10)
x[sample(1:100, 10)] <- rpois(10, 3)
res<-floyd(x)
```

---

Forward selection with generalised linear regression models

*Variable selection in generalised linear regression models with forward selection*

---

**Description**

Variable selection in generalised linear regression models with forward selection

**Usage**

```
fs.reg(y, ds, sig = 0.05, tol = 2, type = "logistic")
```

**Arguments**

<code>y</code>	The dependent variable. This can either be a binary numeric (0, 1) or a vector with integers (numeric or integer class), count data. The first case is for the binary logistic regression and the second for the Poisson regression.
<code>ds</code>	The dataset; provide a matrix where columns denote the variables and the rows the observations. The variables must be continuous, no categorical variables are accepted.
<code>sig</code>	Significance level for assessing the p-values significance. Default value is 0.05.
<code>tol</code>	The difference between two successive values of the stopping rule. By default this is set to 2. If for example, the BIC difference between two successive models is less than 2, the process stops and the last variable, even though significant does not enter the model.

**type** If you have a binary dependent variable, put "logistic" or "quasibinomial". If you have percentages, values between 0 and 1, including 0 and or 1, use "quasibinomial" as well. If you have count data put "poisson".

### Details

The classical forward regression is implemented. The difference is that we have an extra step of check. Even if a variable is significant, the BIC of the model (with that variable) is calculated. If the decrease from the previous BIC (of the model without this variable) is less than a prespecified by the user value (default is 2) the variable will enter. This way, we guard somehow against over-fitting.

### Value

A matrix with for columns, the selected variables, the logarithm of their p-value, their test statistic and the BIC of the model with these variables included. If no variable is selected, the matrix is empty.

### Author(s)

Marios Dimitriadis

Documentation: Marios Dimitriadis <kmdimitriadis@gmail.com>.

### See Also

[cor.fsreg](#), [logistic\\_only](#), [poisson\\_only](#), [glm\\_logistic](#), [glm\\_poisson](#)

### Examples

```
set.seed(123)

#simulate a dataset with continuous data
x <- matnorm(100, 50)
y <- rpois(100, 10)
a <- fs.reg(y, x, sig = 0.05, tol = 2, type = "poisson")
x <- NULL
```

---

G-square and Chi-square test of conditional independence  
*G-square test of conditional independence*

---

### Description

G-square test of conditional independence with and without permutations.

**Usage**

```
g2Test(data, x, y, cs, dc)
g2Test_perm(data, x, y, cs, dc, nperm)
chi2Test(data, x, y, cs, dc)
```

**Arguments**

data	A numerical matrix with the data. <b>The minimum must be 0, otherwise the function can crash or will produce wrong results.</b> The data must be consecutive numbers.
x	A number between 1 and the number of columns of data. This indicates which variable to take.
y	A number between 1 and the number of columns of data (other than x). This indicates the other variable whose independence with x is to be tested.
cs	A vector with the indices of the variables to condition upon. It must be non zero and between 1 and the number of variables. If you want unconditional independence test see <a href="#">g2Test_univariate</a> and <a href="#">g2Test_univariate_perm</a> . If there is an overlap between x, y and cs you will get 0 as the value of the test statistic.
dc	A numerical value equal to the number of variables (or columns of the data matrix) indicating the number of distinct, unique values (or levels) of each variable. Make sure you give the correct numbers here, otherwise the degrees of freedom will be wrong.
nperm	The number of permutations. The permutations test is slower than without permutations and should be used with small sample sizes or when the contingency tables have zeros. When there are few variables, R's "chisq.test" function is faster, but as the number of variables increase the time difference with R's procedure becomes larger and larger.

**Details**

The functions calculates the test statistic of the  $G^2$  test of conditional independence between x and y conditional on a set of variable(s) cs.

**Value**

A list including:

statistic	The $G^2$ or $chi^2$ test statistic.
df	The degrees of freedom of the test statistic.
x	The row or variable of the data.
y	The column or variable of the data.

**Author(s)**

Giorgos Borboudakis. The permutation version used a C++ code by John Burkardt.

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**References**

Tsamardinos, I., & Borboudakis, G. (2010). Permutation testing improves Bayesian network learning. In Joint European Conference on Machine Learning and Knowledge Discovery in Databases (pp. 322-337). Springer Berlin Heidelberg

**See Also**

[g2Test\\_univariate](#), [g2Test\\_univariate\\_perm](#), [correls](#), [univglms](#)

**Examples**

```
nvalues <- 3
nvars <- 10
nsamples <- 5000
data <- matrix( sample( 0:(nvalues - 1), nvars * nsamples, replace = TRUE ), nsamples, nvars )
dc <- rep(nvalues, nvars)

res<-g2Test( data, 1, 2, 3, c(3, 3, 3) )
res<-g2Test_perm( data, 1, 2, 3, c(3, 3, 3), 1000 )

dc<-data<-NULL
```

---

Gamma regression with a log-link

*Gamma regression with a log-link*

---

**Description**

Gamma regression with a log-link.

**Usage**

```
gammareg(y, x, tol = 1e-07, maxiters = 100)
gammacon(y, tol = 1e-08, maxiters = 50)
```

**Arguments**

y	The dependent variable, a numerical variable with non negative numbers.
x	A matrix or data.frame with the independent variables.
tol	The tolerance value to terminate the Newton-Raphson algorithm.
maxiters	The maximum number of iterations that can take place in the regression.

**Details**

The `gamma.reg` fits a Gamma regression with a log-link. The `gamma.con` fits a Gamma regression with a log link with the intercept only ( `glm(y ~ 1, Gamma(log))` ).

**Value**

A list including:

deviance	The deviance value.
phi	The dispersion parameter ( $\phi$ ) of the regression. This is necessary if you want to perform an F hypothesis test for the significance of one or more independent variables.
be	The regression coefficient(s).
info	The number of iterations, the deviance and the dispersion parameter.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

[gammaregs](#), [normlog.reg](#), [invgauss.reg](#)

**Examples**

```
y <- abs( rnorm(100) )
x <- matrix( rnorm(100 * 2), ncol = 2)
mod <- glm(y ~ x, family = Gamma(log) )
res<-summary(mod)

res<-gammareg(y, x)

mod <- glm(y ~ 1, family = Gamma(log) )
res<-summary(mod)
res<-gammacon(y)
```

---

Gaussian regression with a log-link

*Gaussian regression with a log-link*

---

**Description**

Gaussian regression with a log-link.

**Usage**

```
normlog.reg(y, x, tol = 1e-07, maxiters = 100)
```

**Arguments**

<code>y</code>	The dependent variable, a numerical variable with non negative numbers.
<code>x</code>	A matrix or data.frame with the independent variables.
<code>tol</code>	The tolerance value to terminate the Newton-Raphson algorithm.
<code>maxiters</code>	The maximum number of iterations that can take place in the regression.

**Details**

A Gaussian regression with a log-link is fitted.

**Value**

A list including:

<code>i</code>	The number of iterations required by the Newton-Raphson
<code>loglik</code>	The log-likelihood value.
<code>deviance</code>	The deviance value.
<code>be</code>	The regression coefficients

**Author(s)**

Stefanos Fafalios

R implementation and documentation: Stefanos Fafalios <stefanosfafalios@gmail.com>

**See Also**

[normlog.regs](#), [score.glm](#)s, [prop.regs](#), [allbetas](#)

**Examples**

```
y <- abs( rnorm(100) )
x <- matrix( rnorm(100 * 2), ncol = 2)
a <- normlog.reg(y, x)
b <- glm(y ~ x, family = gaussian(log) )
summary(b)
a
```

---

Generates random values from a normal and puts them in a matrix

*Generates random values from a normal and puts them in a matrix*

---

## Description

Generates random values from a normal and puts them in a matrix.

## Usage

```
matrnorm(n, p, seed = NULL)
```

## Arguments

n	The sample size, the number of rows the matrix will have.
p	The dimensionality of the data, the number of columns of the matrix.
seed	If you want the same to be generated again use a seed for the generator, an integer number.

## Details

How many times did you have to simulated data from a (standard) normal distribution in order to test something? For example, in order to see the speed of [logistic\\_only](#), one needs to generate a matrix with predictor variables. The same is true for other similar functions. In [sftests](#), one would like to examine the type I error of this test under the null hypothesis.

By using the Ziggurat method of generating standard normal variates, this function is really fast when you want to generate big matrices.

## Value

An n x p matrix with data simulated from a standard normal distribution.

## Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

## See Also

[rvmf](#), [Rnorm](#), [rmvnorm](#), [rvonmises](#)

## Examples

```
x <- matrnorm(100, 100)
```

Get specific columns/rows fo a matrix

*Get specific columns/rows fo a matrix*

---

## Description

Get specific columns/rows of a matrix.

## Usage

```
columns(x, indices)
rows(x, indices)
```

## Arguments

x	A matrix with data.
indices	An integer vector with the indices.

## Value

A matrix with the specific columns/rows of argument indices.

## Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

## See Also

[rowMins](#), [rowFalse](#), [nth](#), [colrange](#), [colMedians](#), [colVars](#), [colSort](#), [rowSort](#), [rowTrue](#)

## Examples

```
x <- matrix(runif(100*100),100,100)
indices = sample(1:100,50)
all.equal(x[,indices],columns(x,indices))
all.equal(x[indices,],rows(x,indices))

x<-indices<-NULL
```

---

Hash - Pair function *Hash - Pair function*

---

**Description**

Hash - Pair function.

**Usage**

```
hash.list(key, x)
```

**Arguments**

key	The keys of the given values.
x	The values.

**Details**

This function pairs each item of of key and value make a unique hash table.

**Value**

Returns the hash-list table.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>

**See Also**

[hash.find](#)

**Examples**

```
x <- hash.list(letters,c(1:26))  
x[["a"]]==1
```

---

Hash object	<i>Hash object</i>
-------------	--------------------

---

**Description**

Hash object.

**Usage**

```
Hash(keys=NULL, values=NULL)
Hash.key.multi(x, ..., sep = " ")
## S3 replacement method for class 'Hash'
x[..., sep = " "] <- value
## S3 method for class 'Hash'
x[..., sep = " "]
## S3 method for class 'Hash'
print(x, ...)
## S3 method for class 'Hash'
length(x)
```

**Arguments**

<code>x</code>	A Hash object, using Hash function.
<code>values</code>	A vector with the values you want to store.
<code>value</code>	The values you want to store.
<code>keys</code>	A vector with keys for each values.
<code>sep</code>	A character value using to separate the multiple keys for each value.
<code>...</code>	One or more values for access or find elements.

**Details**

If you want to delete a key just insert the global variable "Rfast:::delete".

Hash: Create Hash object where every key has a value. Specify the type from the beginning (for speed). Use the argument "type" with one of the values "new.env, logical, character, integer, numeric". Hash.key.multi: search if key exists. If the keys are multiple, then use the argument "substr" to search inside each multiple for the specific key.

**Value**

A Hash object.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[hash.list](#), [hash.find](#)

**Examples**

```
x <- Hash(rnorm(10), sample(1:10))

x[1,2,13] <- 0.1234 # insert value using multi key. the same as x["1 2 13"] <- 0.1234
x[1,2,3] <- 15 # insert value using multi key. the same as x["1 2 3"] <- 15

Hash.key.multi(x, "1")
x # print Hash object using S3 generic
#x[1,2,3] <- Rfast::delete # delete multi key. the same as x["1 2 3"] <- NULL
length(x)
```

---

Hash object to a list object

*Hash object to a list object*

---

**Description**

Hash object to a list object.

**Usage**

```
hash2list(x, sorting = FALSE)
```

**Arguments**

<code>x</code>	A hash table with two parts, the keys (number(s) as string) and the key values (a single number).
<code>sorting</code>	This is if you you want the numbers in the keys sorted. The default value is FALSE.

**Details**

For every key, there is a key value. This function creates a list and puts every pair of keys and value in a component of a list.

**Value**

A list whose length is equal to the size of the hash table.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[hash.list](#), [hash.find](#)

**Examples**

```
x=list("1 2 4 3"=2.56,"2.34 1.05"=2)
res<-hash2list(x)
res<-hash2list(x,TRUE)
```

---

High dimensional MCD based detection of outliers

*High dimensional MCD based detection of outliers*

---

**Description**

High dimensional MCD based detection of outliers.

**Usage**

```
rmdp(y, alpha = 0.05, itertime = 100, parallel = FALSE)
```

**Arguments**

<code>y</code>	A matrix with numerical data with more columns ( $p$ ) than rows ( $n$ ), i.e. $n < p$ .
<code>alpha</code>	The significance level, i.e. used to decide whether an observation is said to be considered a possible outlier. The default value is 0.05.
<code>itertime</code>	The number of iterations the algorithm will be ran. The higher the sample size, the larger this number must be. With 50 observations in $R^1000$ maybe this has to be 1000 in order to produce stable results.
<code>parallel</code>	A logical value for parallel version.

**Details**

High dimensional outliers ( $n < p$ ) are detected using a properly constructed MCD. The variances of the variables are used and the determinant is simply their product.

**Value**

A list including: `runtime = runtime`, `dis = dis`, `wei = wei`

<code>runtime</code>	The duration of the process.
<code>dis</code>	The final estimated Mahalanobis type normalised distances.
<code>wei</code>	A boolean variable vector specifying whether an observation is "clean" (TRUE) or a possible outlier (FALSE).
<code>cova</code>	The estimated covatriance matrix.

**Author(s)**

Initial R code: Changliang Zou <nk.chlzou@gmail.com> R code modifications: Michail Tsagris <mtsagris@uoc.gr> C++ implementation: Manos Papadakis <papadakm95@gmail.com> Documentation: Michail Tsagris <mtsagris@uoc.gr> and Changliang Zhou <nk.chlzou@gmail.com>

**References**

Ro K., Zou C., Wang Z. and Yin G. (2015). Outlier detection for high-dimensional data. *Biometrika*, 102(3): 589–599.

Tsagris M., Papadakis M., Alenazi A. and Alzeley O. (2024). Computationally Efficient Outlier Detection for High-Dimensional Data Using the MDP Algorithm. *Computation*, 12(9): 185.

**See Also**

[colmeans](#), [colVars](#), [colMedians](#)

**Examples**

```
x <- matrix(rnorm(30 * 100), ncol = 100)
#a <- rmdp(x, itertime = 5)

x<-a<-NULL
```

---

Hypothesis test for the distance correlation

*Hypothesis test for the distance correlation*

---

**Description**

Hypothesis test for the distance correlation.

**Usage**

```
dcor.ttest(x, y, logged = FALSE)
```

**Arguments**

x	A numerical matrix.
y	A numerical matrix.
logged	Do you want the logarithm of the p-value to be returned? If yes, set this to TRUE.

**Details**

The bias corrected distance correlation is used. The hypothesis test is whether the two matrices are independent or not. Note, that this test is size correct as both the sample size and the dimensionality goes to infinity. It will not have the correct type I error for univariate data or for matrices with just a couple of variables.

**Value**

A vector with 4 elements, the bias corrected distance correlation, the degrees of freedom, the test statistic and its associated p-value.

**Author(s)**

Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

G.J. Szekely, M.L. Rizzo and N. K. Bakirov (2007). Measuring and Testing Independence by Correlation of Distances. *Annals of Statistics*, 35(6): 2769–2794.

Szekely G. J. and Rizzo M. L. (2023). *The Energy of Data and Distance Correlation*. Chapman and Hall/CRC.

**See Also**

[dcov](#), [edist](#)

**Examples**

```
x <- as.matrix(iris[1:50, 1:4])
y <- as.matrix(iris[51:100, 1:4])
#res<-dcor.ttest(x, y)
```

---

Hypothesis test for two means of percentages

*Hypothesis test for two means of percentages*

---

**Description**

Hypothesis test for two means of percentages.

**Usage**

```
percent.ttest(x, y, logged = FALSE)
```

**Arguments**

x	A numerical vector with the percentages of the first sample. Any value between 0 and 1 (inclusive) is allowed.
y	A numerical vector with the percentages of the first sample. Any value between 0 and 1 (inclusive) is allowed.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

This is the [prop.reg](#) but with a single categorical predictor which has two levels only. It is like a t-test for the means of two samples having percentages.

**Value**

A vector with three elements, the phi parameter, the test statistic and its associated p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Papke L. E. & Wooldridge J. (1996). Econometric methods for fractional response variables with an application to 401(K) plan participation rates. *Journal of Applied Econometrics*, 11(6): 619-632.

McCullagh, Peter, and John A. Nelder. *Generalized linear models*. CRC press, USA, 2nd edition, 1989.

**See Also**

[link{percent.ttests}](#), [prop.reg](#), [ttest2](#), [ftest](#)

**Examples**

```
x <- rbeta(100, 3, 1)
y <- rbeta(100, 7.5, 2.5)
res<-percent.ttest(x, y)
```

---

Hypothesis test for von Mises-Fisher distribution over Kent  
distribution

*Hypothesis test for von Mises-Fisher distribution over Kent distribu-  
tion*

---

**Description**

The null hypothesis is whether a von Mises-Fisher distribution fits the data well, and the alternative is that the Kent distribution is more suitable.

**Usage**

```
fish.kent(x, logged = FALSE)
```

**Arguments**

`x` A numeric matrix containing the data as unit vectors in Euclidean coordinates.  
`logged` If you want the logarithm of the p-value to be returned set this to TRUE.

**Details**

Essentially it is a test of rotational symmetry, whether Kent's ovalness parameter (beta) is equal to zero. This works for spherical data only.

**Value**

A vector with two elements, the value of the test statistic and its associated p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Rivest, L. P. (1986). Modified Kent's statistics for testing goodness of fit for the Fisher distribution in small concentrated samples. *Statistics & probability letters*, 4(1): 1-4.

**See Also**

[vmf.mle](#), [iag.mle](#)

**Examples**

```
#x <- rvmf(100, rnorm(3), 15)
#res<-fish.kent(x)
x <- NULL
```

---

Hypothesis testing between two skewness or kurtosis coefficients

*Hypothesis testing between two skewness or kurtosis coefficients*

---

**Description**

Hypothesis testing between two skewness or kurtosis coefficients.

**Usage**

```
skew.test2(x, y)
```

```
kurt.test2(x, y)
```

### Arguments

- x                    A numerical vector with data.
- y                    A numerical vector with data, not necessarily of the same size.

### Details

The skewness of kurtosis coefficients between two samples are being compared.

### Value

A vector with the test statistic and its associated p-value.

### Author(s)

Klio Lakiotaki

R implementation and documentation: Klio Lakiotaki <kliolak@gmail.com>.

### References

<https://en.wikipedia.org/wiki/Skewness>

<https://en.wikipedia.org/wiki/Kurtosis>

### See Also

[skew](#), [colskewness](#), [colmeans](#), [colVars](#), [colMedians](#)

### Examples

```
x <- rgamma(150,1, 4)
y <- rgamma(100, 1, 4)
res<-skew.test2(x, y)
res<-kurt.test2(x, y)
```

---

Index of the columns of a data.frame which are a specific type

*Index of the columns of a data.frame which are a specific type*

---

### Description

Index of the columns of a data.frame which are a specific type.

### Usage

```
which.is(x,method="factor")
```

**Arguments**

`x` A data.frame where some columns are expected to be factor variables.  
`method` A character value about the type. One of, "numeric", "factor", "integer", "logical".

**Details**

The function is written in C++ and this is why it is very fast.

**Value**

A vector with the column indices which are factor variables. If there are no factor variables it will return an empty vector.

**Author(s)**

Manos Papadakis <papadakm95@gmail.com>  
 R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[nth](#), [Match](#)

**Examples**

```
res<-which.is(iris)
```

---

Insert/remove function names in/from the NAMESPACE file

*Insert/remove function names in/from the NAMESPACE file*

---

**Description**

Insert/remove function names in/from the NAMESPACE file.

**Usage**

```
AddToNamespace(path.namespace, path.rfolder, paths.full = FALSE)
RemoveFromNamespace(path.namespace, files.to.remove)
```

**Arguments**

`path.namespace` An full path to the NAMESPACE file.  
`path.rfolder` An full path to the directory the new files to be added are stored.  
`files.to.remove` An character with the names of the functions to be removed from file NAMESPACE.  
`paths.full` Print or return the full paths.

**Details**

**AddToNameSpace:** Reads the files that are exported in NAMESPACE and the functions that are inside rfolder (where R files are) and insert every function that is not exported. For that you must add the attribute "#[export]" above every function you wish to export. Also you can use the attribute "#[export s3]" for exporting S3methods. Finally, if you don't want the program to read a file just add at the top of the file the attribute "#[dont read]".

**RemoveFromNamespace:** Remove every function, from argument "files.to.remove", from NAMESPACE.

**Value**

**AddToNameSpace:**

without export A character vector with the names of the R functions that don't have te "#[export]" attribute.

hidden functions

A character vector with the names of the R functions that are hidden.

**RemoveFromNamespace:** Return the files that could not be removed.

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colShuffle](#), [colVars](#), [colmeans](#)

**Examples**

```
## Not run:
#for example: path.namespace="C:\some_file\NAMESPACE" where is NAMESPACE file
#path.rfolder="C:\some_file\R\" where is R files are
#system.time( a<-AddToNameSpace(path.namespace,path.rfolder) )
#if(length(a)==0){
# print("all the files are inserted")
#}else{
# print("The new files that inserted are: \n")
# a
#}
#system.time( a<-RemoveFromNamespace(path.namespace,c("a","b")) )
#if(length(a)==0){
# print("all the files are inserted")
#}else{
# print("The files thatcould not be deleted are: \n")
# a
#}

## End(Not run)
```

---

Inverse Gaussian regression with a log-link  
*Inverese Gaussian regression with a log-link*

---

**Description**

Inverse Gaussian regression with a log-link.

**Usage**

```
invgauss.reg(y, x, tol = 1e-07, maxiters = 100)
```

**Arguments**

y	The dependent variable, a numerical variable with non negative numbers.
x	A matrix or data.frame with the indendent variables.
tol	The tolerance value to terminate the Newton-Raphson algorithm.
maxiters	The maximum number of iterations that can take place in the regression.

**Details**

An inverse Gaussian regression with a log-link is fitted.

**Value**

A list including:

i	The number of iterations required by the Newton-Raphson
loglik	The log-likelihood value.
deviance	The deviance value.
phi	The dispersion parameter ( $\phi$ ) of the regression. This is necessary if you want to perform an F hypothesis test for the significance of one or more independent variables.
be	The regression coefficients

**Author(s)**

Michail Tsagris

R implementation and documentation: Stefanos Fafalios <mtsagris@uoc.gr>

**References**

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

Zakariya Yahya Algamal and Intisar Ibrahim Allyas (2017). Prediction of blood lead level in maternal and fetal using generalized linear model. International Journal of Advanced Statistics and Probability, 5(2): 65-69.

**See Also**

[invgauss.regs](#), [normlog.reg](#), [score.glm](#)s

**Examples**

```
y <- abs( rnorm(100) )
x <- matrix( rnorm(100 * 2), ncol = 2)
a <- invgauss.reg(y, x)
a
```

---

Inverse of a symmetric positive definite matrix

*Inverse of a symmetric positive definite matrix*

---

**Description**

Inverse of a symmetric positive definite matrix.

**Usage**

```
spdinv(A)
```

**Arguments**

A                    A square positive definite matrix.

**Details**

After calculating the Cholesky decomposition of the matrix we use this upper triangular matrix to invert the original matrix.

**Value**

The inverse of the input matrix.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <[mtsagris@uoc.gr](mailto:mtsagris@uoc.gr)> and Manos Papadakis <[papadakm95@gmail.com](mailto:papadakm95@gmail.com)>.

**References**

[http://econ.nsysu.edu.tw/ezfiles/124/1124/img/Chapter17\\_MaximumLikelihoodEstimation.pdf](http://econ.nsysu.edu.tw/ezfiles/124/1124/img/Chapter17_MaximumLikelihoodEstimation.pdf)

**See Also**

[cholesky](#), [cova](#)

**Examples**

```
s <- cova( as.matrix(iris[, 1:4]) )
res<-spdinv(s)
res<-solve(s)
```

---

Iterator

*Iterator*

---

**Description**

A way to traverse a list, data.frame, matrix or vector.

**Usage**

```
iterator(x,method="ceil",type="vector",by=1)
## S3 method for class 'iterator'
print(x,...)
## S3 replacement method for class 'iterator'
Elem(x) <- value
Elem(x)
Elem(x) <- value
## S3 method for class 'iterator'
Elem(x)
## S3 method for class 'iterator'
x == y
## S3 method for class 'iterator'
x != y
```

**Arguments**

x	A variable with any type, or iterator object.
value	An value depending the method of the iterator.
y	An iterator.
method	Method of the iterator class. One of "ceil","col","row".
type	One of "vector","matrix","data.frame","list".
by	An integer value to iterate through element.
...	Anything the user want.

**Details**

iterator: is an object that helps a programmer to traverse the given object.

print.iterator: print an object of class iterator.

"Elem<-": access to element and change the value.

Elem: access to element.

**Value**

An object of class "iterator". This object holds 4 fields:

copy: deep copy of iterator. end: get iterator tha have access to points to the last element. equals:

equality of iterators nextElem: move iterator to point to the next element using argument "by".

prevElem: move iterator to point to the previous element using argument "by".

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colShuffle](#), [colVars](#), [colmeans](#)

**Examples**

```
y<-rnorm(100)
x<-iterator(y,method="ceil",type="vector",by=1)
```

```
s<-0
while(x != x$end()){
  s <- s + Elem(x)
  x$nextElem()
}
```

```
all.equal(s,sum(y))
```

---

James multivariate version of the t-test

*James multivariate version of the t-test*

---

**Description**

James test for testing the equality of two population mean vectors without assuming equality of the covariance matrices.

**Usage**

```
james(y1, y2, a = 0.05, R = 1)
```

**Arguments**

y1	A matrix containing the Euclidean data of the first group.
y2	A matrix containing the Euclidean data of the second group.
a	The significance level, set to 0.05 by default.
R	If R is 1 the classical James test is returned. If R is 2 the MNV modification is implemented.

**Details**

Multivariate analysis of variance without assuming equality of the covariance matrices. The p-value can be calculated either asymptotically or via bootstrap. The James test (1954) or a modification proposed by Krishnamoorthy and Yanping (2006) is implemented. The James test uses a corrected chi-square distribution, whereas the modified version uses an F distribution.

**Value**

A list including:

note	A message informing the user about the test used.
mesoi	The two mean vectors.
info	The test statistic, the p-value, the correction factor and the corrected critical value of the chi-square distribution if the James test has been used or, the test statistic, the p-value, the critical value and the degrees of freedom (numerator and denominator) of the F distribution if the modified James test has been used.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

G.S. James (1954). Tests of Linear Hypotheses in Univariate and Multivariate Analysis when the Ratios of the Population Variances are Unknown. *Biometrika*, 41(1/2): 19-43

Krishnamoorthy K. and Yanping Xia. On Selecting Tests for Equality of Two Normal Mean Vectors (2006). *Multivariate Behavioral Research* 41(4): 533-548

**See Also**

[mv.eeltest2](#)

**Examples**

```
james( as.matrix(iris[1:25, 1:4]), as.matrix(iris[26:50, 1:4]), R = 1 )  
james( as.matrix(iris[1:25, 1:4]), as.matrix(iris[26:50, 1:4]), R = 2 )
```

---

k nearest neighbours algorithm (k-NN)  
*k nearest neighbours algorithm (k-NN)*

---

### Description

k nearest neighbours algorithm (k-NN).

### Usage

```
knn(xnew, y, x, k, dist.type = "euclidean", type = "C", method = "average",
    freq.option = 0, mem.eff = FALSE)
```

### Arguments

xnew	The new data, new predictor variable values. A matrix with numerical data.
y	A vector with the response variable, whose values for the new data we wish to predict. This can be numerical data, factor or discrete, 0, 1, ... The latter two cases are for classification.
x	The dataset. A matrix with numerical data.
k	The number of nearest neighbours to use. The number can either be a single value or a vector with multiple values.
dist.type	The type of distance to be used. Either <code>"euclidean"</code> or <code>"manhattan"</code> .
type	If your response variable <code>"y"</code> is numerical data, then this should be <code>"R"</code> (regression). If <code>"y"</code> is in general categorical, factor or discrete set this argument to <code>"C"</code> (classification).
method	In case you have regression (type = <code>"R"</code> ) you want a way to summarise the prediction. If you want to take the average of the responses of the k closest observations, type <code>"average"</code> . For the median, type <code>"median"</code> and for the harmonic mean, type <code>"harmonic"</code> .
freq.option	If classification (type = <code>"C"</code> ) and ties occur in the prediction, more than one class has the same number of k nearest neighbours, in which case there are two strategies available: Option 0 selects the first most frequent encountered. Option 1 randomly selects the most frequent value, in the case that there are duplicates.
mem.eff	Boolean value indicating a conservative or not use of memory. Lower usage of memory/Having this option on will lead to a slight decrease in execution speed and should ideally be on when the amount of memory in demand might be a concern.

### Details

The concept behind k-NN is simple. Suppose we have a matrix with predictor variables and a vector with the response variable (numerical or categorical). When a new vector with observations (predictor variables) is available, its corresponding response value, numerical or category is to be predicted. Instead of using a model, parametric or not, one can use this ad hoc algorithm.

The  $k$  smallest distances between the new predictor variables and the existing ones are calculated. In the case of regression, the average, median or harmonic mean of the corresponding response values of these closest predictor values are calculated. In the case of classification, i.e. categorical response value, a voting rule is applied. The most frequent group (response value) is where the new observation is to be allocated.

### Value

A matrix whose number of columns is equal to the size of  $k$ . If in the input you provided there is just one value of  $k$ , then a matrix with one column is returned containing the predicted values. If more than one value was supplied, the matrix will contain the predicted values for every value of  $k$ .

### Author(s)

Marios Dimitriadis

R implementation and documentation: Marios Dimitriadis <kmdimitriadis@gmail.com>

### References

Cover TM and Hart PE (1967). Nearest neighbor pattern classification. IEEE Transactions on Information Theory. 13(1):21-27.

Friedman J., Hastie T. and Tibshirani R. (2017). The elements of statistical learning. New York: Springer.

[http://web.stanford.edu/~hastie/ElemStatLearn/printings/ESLII\\_print12.pdf](http://web.stanford.edu/~hastie/ElemStatLearn/printings/ESLII_print12.pdf)

<http://statlink.tripod.com/id3.html>

### See Also

[knn.cv](#), [dirknn](#), [logistic\\_only](#), [fs.reg](#), [cor.fsreg](#)

### Examples

```
# Simulate a dataset with continuous data
x <- as.matrix(iris[, 1:4])
y <- as.numeric(iris[, 5])
id <- sample(1:150, 120)
mod <- knn(x[-id, ], y[id], x[id, ], k = c(4, 5, 6), type = "C", mem.eff = FALSE)
mod # Predicted values of y for 3 values of k.
res<-table(mod[, 1], y[-id] ) # Confusion matrix for k = 4
res<-table(mod[, 2], y[-id] ) # Confusion matrix for k = 5
res<-table(mod[, 3], y[-id] ) # Confusion matrix for k = 6
```

---

k-NN algorithm using the arc cosinus distance  
*k-NN algorithm using the arc cosinus distance*

---

**Description**

It classifies new observations to some known groups via the k-NN algorithm.

**Usage**

```
dirknn(xnew, x, y, k, type = "C", parallel = FALSE)
```

**Arguments**

xnew	The new data whose membership is to be predicted, a numeric matrix with unit vectors. In case you have one vector only make it a row vector (i.e. matrix with one row).
x	The data, a numeric matrix with unit vectors.
k	The number of nearest neighbours. It can also be a vector with many values.
y	A numerical vector representing the class or label of each vector of x. 1, 2, 3, and so on. It can also be a numerical vector with data in order to perform regression.
type	If your response variable y is numerical data, then this should be "R" (regression) or "WR" for distance weighted based nearest neighbours. If y is in general categorical set this argument to "C" (classification) or to "WC" for distance weighted based nearest neighbours.
parallel	Do you want the calculations to take place in parallel? The default value is FALSE.

**Details**

The standard algorithm is to keep the k nearest observations and see the groups of these observations. The new observation is allocated to the most frequent seen group. The non standard algorithm is to calculate the classical mean or the harmonic mean of the k nearest observations for each group. The new observation is allocated to the group with the smallest mean distance.

If you want regression, the predicted value is calculated as the average of the responses of the k nearest observations.

**Value**

A matrix with the predicted group(s). It has as many columns as the values of k.

**Author(s)**

Stefanos Fafalios

R implementation and documentation: Stefanos Fafalios <stefanosfafalios@gmail.com>

**See Also**

[dirknn.cv](#), [knn](#), [vmf.mle](#), [spml.mle](#)

**Examples**

```
x <- as.matrix(iris[, 1:4])
x <- x/sqrt( rowSums(x^2) )
y<- as.numeric( iris[, 5] )
a <- dirknn(x, x, y, k = 2:10)
```

---

Limited number of eigenvalues and eigenvectors of a symmetric matrix

*Limited number of eigenvalues and eigenvectors of a symmetric matrix*

---

**Description**

Limited number of eigenvalues and eigenvectors of a symmetric matrix.

**Usage**

```
eigen.sym(A, k, vectors = TRUE)
```

**Arguments**

A	A symmetric matrix.
k	The number of eigenvalues and eigenvectors to extract.
vectors	A flag that indicates if the eigenvectors will be returned (default: vectors = True)

**Details**

The function calls the same function from the Armadillo library in C++. It is quite faster than R's built in function "eigen" if the number of eigenvalues and eigenvectors (argument k) is small.

The k largest, in magnitude, eigenvalues are returned. Hence, if the matrix is not positive definite you may get negative eigenvalues as well. So, it is advised to use it with positive definite matrices.

**Value**

A list including:

values	The eigenvalues.
vectors	The eigenvectors.

**Author(s)**

Armadillo library in C++ and Stefanos Fafalios and Manos Papadakis.

R implementation and documentation: Stefanos Fafalios <stefanosfafalios@gmail.com> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**[hd.eigen](#)**Examples**

```
x <- matnorm(500, 100 )
s <- Rfast::cova(x)
res<-eigen.sym(s, 5)
x <- s <- NULL
```

---

Linear models for large scale data

*Linear models for large scale data*

---

**Description**

Linear models for large scale data.

**Usage**

```
lmfit(x, y, w = NULL)
```

**Arguments**

x	The design matrix with the data, where each column refers to a different sample of subjects. You must supply the design matrix, with the column of 1s. This function is the analogue of <code>lm.fit</code> and <code>.lm.fit</code> .
y	A numerical vector or a numerical matrix.
w	An optional numerical vector with weights. Note that if you supply this, the function does not make them sum to 1. So, you should do it.

**Details**

We have simply exploited R's powerful function and managed to do better than `.lm.fit` which is a really powerful function as well. This is a bare bones function as it returns only two things, the coefficients and the residuals. `.lm.fit` returns more and `lm.fit` even more and finally `lm` returns too much. The motivation came from this site <https://m-clark.github.io/docs/fastr.html>. We changed the function a bit.

**Value**

A list including:

be	The beta coefficients.
residuals	The residuals of the linear model(s).

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Draper, N.R. and Smith H. (1988). Applied regression analysis. New York, Wiley, 3rd edition.

**See Also**

[regression](#), [allbetas](#), [correels](#), [mvbetas](#), [cor.fsreg](#)

**Examples**

```
n <- 200 ; p <- 5
X <- matnorm(n, p)
y <- rnorm(n)
a1 <- .lm.fit(X, y)
a2 <- lmfit(X, y)
x <- NULL
```

---

Logistic and Poisson regression models

*Logistic and Poisson regression models*

---

**Description**

Logistic and Poisson regression models.

**Usage**

```
glm_logistic(x, y, full = FALSE, tol = 1e-09, maxiters = 100)
glm_poisson(x, y, full = FALSE, tol = 1e-09)
```

**Arguments**

<code>x</code>	A matrix with the data, where the rows denote the samples (and the two groups) and the columns are the variables. This can be a matrix or a data.frame (with factors).
<code>y</code>	The dependent variable; a numerical vector with two values (0 and 1) for the logistic regression or integer values, 0, 1, 2,... for the Poisson regression.
<code>full</code>	If this is FALSE, the coefficients and the deviance will be returned only. If this is TRUE, more information is returned.
<code>tol</code>	The tolerance value to terminate the Newton-Raphson algorithm.
<code>maxiters</code>	The max number of iterations that can take place in each regression.

**Details**

The function is written in C++ and this is why it is very fast.

**Value**

When full is FALSE a list including:

be	The regression coefficients.
devi	The deviance of the model.

When full is TRUE a list including:

info	The regression coefficients, their standard error, their Wald test statistic and their p-value.
devi	The deviance.

**Author(s)**

Manos Papadakis <papadakm95@gmail.com>

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

[poisson\\_only](#), [logistic\\_only](#), [univglms](#), [regression](#)

**Examples**

```
x <- matrix(rnorm(100 * 3), ncol = 3)
y <- rbinom(100, 1, 0.6) ## binary logistic regression
a1 <- glm_logistic(x, y, full = TRUE)
a2 <- glm(y ~ x, binomial)

x <- matrix(rnorm(100 * 3), ncol = 3)
y <- rpois(100, 10) ## binary logistic regression
b1 <- glm_poisson(x, y, full = TRUE)
b2 <- glm(y ~ x, poisson)

x<-y<-a1<-a2<-b1<-b2<-NULL
```

---

Logistic or Poisson regression with a single categorical predictor

*Logistic or Poisson regression with a single categorical predictor*

---

### Description

Logistic or Poisson regression with a single categorical predictor.

### Usage

```
logistic.cat1(y, x, logged = FALSE)
```

```
poisson.cat1(y, x, logged = FALSE)
```

### Arguments

y	A numerical vector with values 0 or 1.
x	A numerical vector with discrete numbers or a factor variable. This is suppose to be a categorical predictor. If you supply a continuous valued vector the function will obviously provide wrong results. <b>Note:</b> For the "binomial.anova" if this is a numerical vector it must contain strictly positive numbers, i.e. 1, 2, 3, 4, ..., no zeros are allowed.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

### Details

There is a closed form solution for the logistic regression in the case of a single predictor variable. See the references for more information.

### Value

info	A matrix similar to the one produced by the glm command. The estimates, their standard error, the Wald value and the relevant p-value.
devs	For the logistic regression case a vector with the null and the residual deviances, their difference and the significance of this difference.
res	For the Poisson regression case a vector with the log likelihood ratio test statistic value and its significance.

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

### References

Stan Lipovetsky (2015). Analytical closed-form solution for binary logit regression by categorical predictors. *Journal of Applied Statistics*, 42(1): 37–49.

**See Also**

[poisson.anova](#), [poisson.anovas](#), [anova](#), [logistic\\_only](#), [poisson\\_only](#)

**Examples**

```

y <- rbinom(20000, 1, 0.6)
x <- as.factor( rbinom(20000, 3, 0.5) )
a1 <- logistic.cat1(y, x)
#a2 <- glm(y ~ x, binomial)

y <- rpois(20000, 10)
x <- as.factor( rbinom(20000, 3, 0.5) )
a1 <- poisson.cat1(y, x)
#a2 <- glm(y ~ x, poisson)

x<-y<-a1<-a2<-NULL

```

---

Lower and Upper triangular of a matrix

*Lower and Upper triangular of a matrix*

---

**Description**

Lower/upper triangular matrix.

**Usage**

```

lower_tri(x, suma = FALSE, diag = FALSE)
upper_tri(x, suma = FALSE, diag = FALSE)
lower_tri.assign(x, v, diag = FALSE)
upper_tri.assign(x, v, diag = FALSE)

```

**Arguments**

x	A matrix with data <b>or</b> a vector with 2 values which is the dimension of the logical matrix to be returned with the upper or lower triangular filled with "TRUE".
v	A numeric vector for assign to the lower/upper triangular.
suma	A logical value for returning the sum of the upper or lower triangular. By default is "FALSE". Works only <b>if</b> argument "x" is matrix.
diag	A logical value include the diagonal to the result.

**Value**

Get a lower/upper triangular logical matrix with values **TRUE/FALSE**, a vector with the values of a lower/upper triangular, the sum of the upper/lower triangular if suma is set **TRUE** or assign to the lower/upper (only for large matrices) triangular. You can also include diagonal with any operation if argument diag is set to "TRUE".

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[rowMins](#), [colFalse](#), [nth](#), [rowrange](#), [rowMedians](#), [rowVars](#), [colTrue](#)

**Examples**

```
x <- matrix(runif(10*10),10,10)

all.equal(lower_tri(c(10,10)),lower_tri(x))

all.equal(lower_tri(x),x[lower_tri(x)])

#all.equal(upper_tri(c(10,10)),upper_tri(x))

#all.equal(upper_tri(x),x[upper_tri(x)])

#all.equal(lower_tri(c(10,10),diag = TRUE),lower_tri(x,diag = TRUE))

#all.equal(lower_tri(x,diag = TRUE),x[lower_tri(x,diag = TRUE)])

#all.equal(upper_tri(c(10,10),diag = TRUE),upper_tri(x,diag = TRUE))

#all.equal(upper_tri(x,diag = TRUE),x[upper_tri(x,diag = TRUE)])

all.equal(lower_tri.assign(x,diag = TRUE,v=rep(1,1000)),x[lower_tri(x,diag = TRUE)]<-1)

all.equal(upper_tri.assign(x,diag = TRUE,v=rep(1,1000)),x[upper_tri(x,diag = TRUE)]<-1)

x<-NULL
```

---

Mahalanobis distance *Mahalanobis distance*

---

**Description**

Mahalanobis distance.

**Usage**

```
mahala(x, mu, sigma, ischol = FALSE)
```

**Arguments**

<code>x</code>	A matrix with the data, where rows denotes observations (vectors) and the columns contain the variables.
<code>mu</code>	The mean vector.
<code>sigma</code>	The covariance or any square symmetric matrix.
<code>ischol</code>	A boolean variable set to true if the Cholesky decomposition of the covariance matrix is supplied in the argument <code>"sigma"</code> .

**Value**

A vector with the Mahalanobis distances.

**Author(s)**

Matteo Fasiolo <matteo.fasiolo@gmail.com>,  
C++ and R implementation and documentation: Matteo Fasiolo <matteo.fasiolo@gmail.com>.

**See Also**

[dista](#), [colmeans](#)

**Examples**

```
x <- matrix( rnorm(100 * 50), ncol = 50 )
m <- colmeans(x)
s <- cov(x)
#a1 <- mahala(x, m, s)
```

---

Many (and one) area under the curve values  
*Many area under the curve values*

---

**Description**

Many area under the curve values.

**Usage**

```
colaucs(group, preds)
auc(group, preds)
```

**Arguments**

<code>group</code>	A numerical vector with two values, one of which must be strictly 1.
<code>preds</code>	A numerical matrix with scores, probabilities or any other measure. In the case of <code>auc</code> this is a vector.

**Details**

The AUCs are calculated column-wise or just an AUC if the vector function is used.

**Value**

A vector with length equal to the number of columns of the "preds" argument, with the AUC values for each column. If the "auc" function is used then a single number is returned.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[ttests](#), [ttest](#), [ftests](#)

**Examples**

```
## 200 variables, hence 200 AUCs will be calculated
x <- matrix( rnorm(100 * 200), ncol = 200 )
ina <- rbinom(100, 1, 0.6)
colaucs(ina, x)
a <- colaucs(ina, x)
b <- auc(ina, x[, 1])
x <- NULL
```

---

Many 2 sample proportions tests

*Many 2 sample proportions tests*

---

**Description**

It performs very many 2 sample proportions tests.

**Usage**

```
proptests(x1, x2, n1, n2)
```

**Arguments**

x1	A vector with the successes of the one group.
x2	A vector with the successes of the one group.
n1	A vector with the number of trials of the one group.
n2	A vector with the number of trials of the one group.

**Details**

The 2-sample proportions test is performed for each pair of proportions of the two groups.

**Value**

A matrix with the proportions of each group (two columns), the test statistic and the p-value of each test.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

B. L. Welch (1951). On the comparison of several mean values: an alternative approach. *Biometrika*, 38(3/4), 330-336.

**See Also**

[ttests](#), [ftests](#), [colVars](#)

**Examples**

```
## 10000 variables, hence 10000 t-tests will be performed
set.seed(12345)
x1 <- rpois(500, 5)
x2 <- rpois(500, 5)
n1 <- rpois(1000, 40)
n2 <- rpois(1000, 40)
a <- proptests(x1, x2, n1, n2)
mean(a[, 4]<0.05)

x1 <- rbinom(500, 500, 0.6)
x2 <- rbinom(500, 500, 0.6)
b <- proptests(x1, x2, 500, 500)
mean(b[, 4]<0.05)
```

---

Many 2 sample tests    *Many 2 sample tests tests*

---

**Description**

It performs very many 2 sample tests.

**Usage**

```

ttests(x, y = NULL, ina, alternative = "unequal", paired = FALSE,
logged = FALSE, parallel = FALSE)
mcnemars(x, y = NULL, ina, logged = FALSE)
var2tests(x, y = NULL, ina, alternative = "unequal", logged = FALSE)

```

**Arguments**

x	A matrix with the data, where the rows denote the samples and the columns are the variables.
y	A second matrix with the data of the second group. If this is NULL (default value) then the argument ina must be supplied. Notice that when you supply the two matrices the procedure is two times faster.
ina	A numerical vector with 1s and 2s indicating the two groups. Be careful, the function is designed to accept only these two numbers. In addition, if your "y" is NULL, you must specify "ina".
alternative	The type of hypothesis to be checked, "equal", "greater", "less".
paired	If the groups are not independent paired t-tests should be performed and this must be TRUE, otherwise, leave it FALSE. In this case, the two groups must have equal sample sizes, otherwise no test will be performed.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?
parallel	Should parallel implementations take place in C++? The default value is FALSE.

**Details**

For the ttests, if the groups are independent, the Welch's t-test (without assuming equal variances) is performed. Otherwise many paired t-tests are performed. The McNemar's test requires a number of observations, at least 30 would be good in order for the test to have some power and be size correct.

**Value**

A matrix with the test statistic, the degrees of freedom (if the groups are independent) and the p-value (or their logarithm) of each test.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

B. L. Welch (1951). On the comparison of several mean values: an alternative approach. *Biometrika*, 38(3/4), 330-336.

McNemar Q. (1947). Note on the sampling error of the difference between correlated proportions or percentages. *Psychometrika*. 12(2):153-157.

**See Also**

[ftests](#), [anovas](#), [ttest](#)

**Examples**

```
## 1000 variables, hence 1000 t-tests will be performed
x = matnorm(100, 100)
## 100 observations in total
ina = rbinom(100, 1, 0.6) + 1  ## independent samples t-test
ttests(x, ina = ina)
x1 = x[ina == 1, ]
x2 = x[ina == 2, ]
ttests(x1, x2)
x <- NULL
```

---

Many analysis of variance tests with a discrete variable

*Many analysis of variance tests with a discrete variable*

---

**Description**

Many analysis of variance tests with a discrete variable.

**Usage**

```
poisson.anovas(y, ina, logged = FALSE)
quasipoisson.anovas(y, ina, logged = FALSE)
geom.anovas(y, ina, type = 1, logged = FALSE)
```

**Arguments**

<code>y</code>	A numerical matrix with discrete valued data, i.e. counts for the case of the Poisson, or with 0s and 1s for the case of the Bernoulli distribution. Each column represents a variable.
<code>ina</code>	A numerical vector with discrete numbers starting from 1, i.e. 1, 2, 3, 4,... or a factor variable. This is suppose to be a categorical predictor. If you supply a continuous valued vector the function will obviously provide wrong results.
<code>type</code>	This rgument is for the geometric distribution. Type 1 refers to the case where the minimum is zero and type 2 for the case of the minimum being 1.
<code>logged</code>	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

This is the analysis of variance with count data. What we do is many log-likelihood ratio tests. For the quasi Poisson case we scale the difference in the deviances.

**Value**

A matrix with two values, the difference in the deviances (test statistic) and the relevant p-value. For the case of quasi Poisson the estimated  $\phi$  parameter is also returned.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[g2tests](#), [poisson.anova](#), [anova](#), [poisson\\_only](#), [poisson.mle](#)

**Examples**

```
ina <- rbinom(500, 3, 0.5) + 1
## Poisson example
y <- matrix( rpois(500 * 100, 10), ncol= 100 )
a1 <- poisson.anovas(y, ina)
y <- NULL
```

---

Many ANCOVAs

*Many ANCOVAs*

---

**Description**

Many ANCOVAs.

**Usage**

```
ancovas(y, ina, x, logged = FALSE)
```

**Arguments**

y	A matrix with the data, where the rows denote the observations and the columns are the variables.
ina	A numerical vector with 1s, 2s, 3s and so one indicating the two groups. Be careful, the function is desinged to accept numbers greater than zero.
x	A numerical vector whose length is equal to the number of rows of y. This is the covariate.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

Many Analysis of covariance tests are performed. No interaction between the factor and the covariate is tested. Only the main effects. The design need not be balanced. The values of `ina` need not have the same frequency. The sums of squares have been adjusted to accept balanced and unbalanced designs.

**Value**

A matrix with the test statistic and the p-value for the factor variable and the covariate.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

D.C. Montgomery (2001). Design and analysis of experiments (5th Edition). New York: John Wiley & Sons

**See Also**

[ftests](#), [ttests](#), [anovas](#)

**Examples**

```
## 100 variables, hence 100 F-tests will be performed
y <- matrix( rnorm(90 * 100), ncol = 100 )
ina <- rbinom(90, 2, 0.5) + 1
x <- rnorm(90)
a <- ancovas(y, ina, x)

m1 <- lm(y[, 15] ~ factor(ina) + x)
m2 <- lm(y[, 15] ~ x + factor(ina))
res<-anova(m1)
res<-anova(m2)
y <- NULL
a[15, ] ## the same with the m2 model, but not the m1
```

---

Many ANOVAS for count data with Poisson or quasi Poisson models

*Many ANOVAS for count data with Poisson or quasi Poisson models*

---

**Description**

Many ANOVAS for count data with Poisson or quasi Poisson models.

**Usage**

```
colpoisson.anovas(y, x, logged = FALSE)
colquasipoisson.anovas(y, x, logged = FALSE)
```

**Arguments**

y	A numerical vector with the data.
x	A matrix with the data, where the rows denote the samples (and the two groups) and the columns are the variables. This must be a matrix with the categorical variables as numbers, starting from 1. Poisson or quassi Poisson ANOVA takes place for each column.
logged	A boolean variable; it will return the logarithm of the pvalue if set to TRUE.

**Details**

Poisson or quassi Poisson ANOVA takes place at each column.

**Value**

A matrix with the test statistic and the (logged) p-value for each predictor variable. In the case of the quasi Poisson, the  $\phi$  is returned as well.

**Author(s)**

Michail Tsagris and Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

**See Also**

[poisson.anova](#), [boot.ttest2](#), [ttest2](#), [fctest](#)

**Examples**

```
y <- rpois(200, 10)
x <- matrix(rbinom(200 * 10, 3, 0.5), ncol = 10)
```

---

Many exponential regressions

*Many exponential regressions*

---

**Description**

Many exponential regressions.

**Usage**

```
expregs(y, x, di, tol = 1e-09, logged = FALSE)
```

**Arguments**

y	A vector with positive data (including zeros).
x	A numerical matrix with the predictor variables.
di	A vector of size equal to that of y with 0s and 1s indicating censoring or not respectively.
tol	The tolerance value to stop the newton-Raphson iterations. It is set to 1e-09 by default.
logged	A boolean variable; it will return the logarithm of the pvalue if set to TRUE.

**Details**

We have implemented the newton-Raphson in order to avoid unnecessary calculations.

**Value**

A matrix with three columns, the test statistic, its associated (logged) p-value and the BIC of each model.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

[univglms](#), [score.glms](#), [logistic\\_only](#), [poisson\\_only](#), [regression](#)

**Examples**

```
## 200 variables, hence 200 univariate regressions are to be fitted
x <- matnorm(100, 100)
y <- rexp(100, 4)
expregs(y, x, di = rep(1, length(y)))
x <- NULL
```

---

Many F-tests with really huge matrices

*Many F-tests with really huge matrices*

---

### Description

Many F-tests with really huge matrices.

### Usage

```
list.ftests(x, logged = FALSE)
```

### Arguments

x	A list with many big size matrices. Each element of the list contains a matrix. This is the <code>ftests</code> function but with really huge matrices, which cannot be loaded into R as a single matrix.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

### Details

The Welch's F-test (without assuming equal variances) is performed just like in the "ftests" function. The difference is that you have a really huge matrix which you cannot load into R. In the "ftests" function, the argument "ina" denotes the different groups. Here, you "cut" the matrix into smaller ones, each of which denotes a different group and put them in a list.

### Value

A matrix with the test statistic and the p-value of each test.

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

### References

B.L. Welch (1951). On the comparison of several mean values: an alternative approach. *Biometrika*, 38(3/4), 330-336.

### See Also

[ftests](#), [ttests](#)

**Examples**

```
x <- matnorm(300, 500)
ina <- rbinom(300, 2, 0.6) + 1
a <- list()
a[[ 1 ]] <- x[ina == 1, ]
a[[ 2 ]] <- x[ina == 2, ]
a[[ 3 ]] <- x[ina == 3, ]
mod <- list.ftests(a)
z <- NULL
a <- NULL
```

---

Many G-square and Chi-square tests of independence  
*Many G-square tests of independence*

---

**Description**

Many G-square tests of independence with and without permutations.

**Usage**

```
g2tests(data, x, y, dc)
g2tests_perm(data, x, y, dc, nperm)
chi2tests(data, x, y, dc)
```

**Arguments**

data	A numerical matrix with the data. <b>The minimum must be 0, otherwise the function can crash or will produce wrong results.</b> The data must be consecutive numbers.
x	An integer number or a vector of integer numbers showing the other variable(s) to be used for the $G^2$ test of independence.
y	An integer number showing which column of data to be used.
dc	A numerical value equal to the number of variables (or columns of the data matrix) indicating the number of distinct, unique values (or levels) of each variable. Make sure you give the correct numbers here, otherwise the degrees of freedom will be wrong.
nperm	The number of permutations. The permutations test is slower than without permutations and should be used with small sample sizes or when the contingency tables have zeros. When there are few variables, R's "chisq.test" function is faster, but as the number of variables increase the time difference with R's procedure becomes larger and larger.

**Details**

The function does all the pairwise  $G^2$  test of independence and gives the position inside the matrix. The user must build the associations matrix now, similarly to the correlation matrix. See the examples of how to do that. The p-value is not returned, we leave this to the user. See the examples of how to obtain it.

**Value**

A list including:

statistic	The $G^2$ or $\chi^2$ test statistic for each pair of variables.
pvalue	This is returned when you have selected the permutation based $G^2$ test.
x	The row or variable of the data.
y	The column or variable of the data.
df	The degrees of freedom of each test.

**Author(s)**

Giorgos Borboudakis. The permutation version used a C++ code by John Burkardt.

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**References**

Tsagris M. (2017). Conditional independence test for categorical data using Poisson log-linear model. *Journal of Data Science*, 15(2):347-356.

Tsamardinos, I., & Borboudakis, G. (2010). Permutation testing improves Bayesian network learning. In *Joint European Conference on Machine Learning and Knowledge Discovery in Databases* (pp. 322-337). Springer Berlin Heidelberg.

**See Also**

[g2Test](#), [g2Test\\_perm](#), [correls](#), [univglms](#)

**Examples**

```
nvalues <- 3
nvars <- 10
nsamples <- 2000
data <- matrix( sample( 0:(nvalues - 1), nvars * nsamples, replace = TRUE ), nsamples, nvars )
dc <- rep(nvalues, nvars)
a <- g2tests(data = data, x = 2:9, y = 1, dc = dc)
pval <- pchisq(a$statistic, a$df, lower.tail = FALSE) ## p-value
b <- g2tests_perm(data = data, x = 2:9, y = 1, dc = dc, nperm = 1000)
a<-b<-data<-NULL
```

---

Many hypothesis tests for two means of percentages

*Many hypothesis tests for two means of percentages*

---

**Description**

Many hypothesis tests for two means of percentages.

**Usage**

```
percent.ttests(x, y, logged = FALSE)
```

**Arguments**

x	A numerical matrix with the percentages of the first sample. Any value between 0 and 1 (inclusive) is allowed.
y	A numerical matrix with the percentages of the first sample. Any value between 0 and 1 (inclusive) is allowed.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

This is the [prop.reg](#) but with a single categorical predictor which has two levels only. It is like a t-test for the means of two samples having percentages.

**Value**

A matrix with three columns, the phi parameter, the test statistic and its associated p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Papke L. E. & Wooldridge J. (1996). Econometric methods for fractional response variables with an application to 401(K) plan participation rates. *Journal of Applied Econometrics*, 11(6): 619-632.

McCullagh, Peter, and John A. Nelder. *Generalized linear models*. CRC press, USA, 2nd edition, 1989.

**See Also**

[link{percent.ttest}](#), [prop.reg](#), [ttest2](#), [fctest](#)

**Examples**

```
x <- matrix( rbeta(100 * 10, 3, 1), ncol = 10)
y <- matrix( rbeta(50 * 10, 7.5, 2.5), ncol = 10)
res<-percent.ttests(x, y)
```

---

Many moment and maximum likelihood estimations of variance components

*Many moment and maximum likelihood estimations of variance components*

---

**Description**

Many moment and maximum likelihood estimations of variance components.

**Usage**

```
colvarcomps.mom(x, id, parallel = FALSE)
colvarcomps.mle(x, id, ranef = FALSE, tol= 1e-08, maxiters = 100,
parallel = FALSE)
```

**Arguments**

x	A matrix with the data, where each column refers to a different sample of subjects.
id	A numerical vector indicating the subject. You must put consecutive numbers and no zero values. Alternatively this can be a factor variable.
ranef	Do you also want the random effects to be returned? TRUE or FALSE.
tol	The tolerance level to terminate the golden ratio search.
maxiters	The maximum number of iterations to perform.
parallel	Should the computations run in parallel? TRUE or FALSE.

**Details**

Note that the "colvarcomp.mom" works for **balanced designs only**, i.e. for each subject the same number of measurements have been taken. The "colvarcomps.mle" works for unbalanced as well.

The variance components, the variance of the between measurements and the variance of the within are estimated using moment estimators. The "colvarcomps.mom" is the moment analogue of a random effects model which uses likelihood estimation ("colvarcomps.mle"). It is much faster, but can give negative variance of the random effects, in which case it becomes zero.

The maximum likelihood version is a bit slower (try yourselves to see the difference), but statistically speaking is to be preferred when small samples are available. The reason why it is only a little bit slower and not a lot slower as one would imagine is because we are using a closed formula to calculate the two variance components (Demidenko, 2013, pg. 67-69). Yes, there are closed formulas for linear mixed models.

**Value**

For the "colvarcomps.mom": A matrix with 5 columns, The MSE, the estimate of the between variance, the variance components ratio and a 95% confidence for the ratio.

For the "colvarcomps.mle": **If ranef = FALSE** a list with a single component called "info". That is a matrix with 3 columns, The MSE, the estimate of the between variance and the log-likelihood value. **If ranef = TRUE** a list including "info" and an extra component called "ranef" containing the random effects. It is a matrix with the same number of columns as the data. Each column contains the random effects of each variable.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

D.C. Montgomery (2001). Design and analysis of experiments (5th Edition). New York: John Wiley & Sons.

Charles S. Davis (2002). Statistical methods for the analysis of repeated measures. New York: Springer-Verlag.

Demidenko E. (2013). Mixed Models: Theory and Applications with R 2nd Edition). New Jersey: John Wiley & Sons (Excellent book).

**See Also**

[varcomps.mle](#), [colrint.regbx](#)

**Examples**

```
## example taken from Montgomery, page 514-517.
y <- c(98, 97, 99, 96, 91, 90, 93, 92,
96, 95, 97, 95, 95, 96, 99, 98)
y <- matrix(y)
id <- rep(1:4, each = 4)

x <- rmvnorm(100, numeric(20), diag(rexp(20)) )
id <- rep(1:25, each = 4)
n <- 25 ; d <- 4
a <- colvarcomps.mom(x, id)
mean(a[, 4]<0 & a[, 5]>0)
b <- colvarcomps.mle(x, id)
x <- NULL
```

---

Many multi-sample tests

*Many multi-sample tests*

---

### Description

Many multi-sample tests.

### Usage

```
ftests(x, ina, logged = FALSE)
anovas(x, ina, logged = FALSE)
vartests(x, ina, type = "levene", logged = FALSE)
block.anovas(x, treat, block, logged = FALSE)
```

### Arguments

x	A matrix with the data, where the rows denote the observations (and the two groups) and the columns are the variables.
ina	A numerical vector with 1s, 2s, 3s and so on indicating the two groups. Be careful, the function is desinged to accept numbers greater than zero. Alternatively it can be a factor variable.
type	This is for the variances test and can be either "levene" or "bf" corresponding to Levene's or Brown-Forsythe's testing procedure.
treat	In the case of the blocking ANOVA this argument plays the role of the "ina" argument.
block	This item, in the blocking ANOVA denotes the subjects which are the same. Similarly to "ina" a numeric vector with 1s, 2s, 3s and so on.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

### Details

The Welch's F-test (without assuming equal variances) is performed with the "ftests" function. The "anovas" function perform the classical (Fisher's) one-way analysis of variance (ANOVA) which assumes equal variance across the groups.

The "vartests" perform hypothesis test for the equality of the variances in two ways, either via the Levene or via the Brown-Forsythe procedure. Levene's test employs the means, whereas the Brown-Forsythe procedure employs the medians and is therefore more robust to outliers. The "var2tests" implement the classical F test.

The "block.anova" is the ANOVA with blocking, randomised complete block design (RCBD). In this case, for every combination of the block and treatment values, there is only one observation. The mathematics are the same as in the case of two way ANOVA, but the assumptions different and the testing procedure also different. In addition, no interaction is present.

**Value**

A matrix with the test statistic and the p-value of each test.

**Author(s)**

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Welch B.L. (1951). On the comparison of several mean values: an alternative approach. *Biometrika*, 38(3/4), 330-336.

Montgomery D.C. (2001). *Design and analysis of experiments* (5th Edition). New York: John Wiley & Sons.

**See Also**

[ttests](#)

**Examples**

```
x <- matrix( rnorm(300 * 50), ncol = 50 )
## 300 observations in total
ina <- rbinom(300, 3, 0.6) + 1
a1 <- fttests(x, ina)
a2 <- anovas(x, ina)
a3 <- vartests(x, ina)
x <- NULL
```

---

Many multivariate simple linear regressions coefficients

*Many multivariate simple linear regressions coefficients*

---

**Description**

Many multivariate simple linear regressions coefficients.

**Usage**

```
mvbetas(y, x, pvalue = FALSE)
```

**Arguments**

y	A matrix with the data, where rows denotes the observations and the columns contain the dependent variables.
x	A numerical vector with one continuous independent variable only.
pvalue	If you want a hypothesis test that each slope (beta coefficient) is equal to zero set this equal to TRUE. It will also produce all the correlations between y and x.

**Details**

It is a function somehow opposite to the [allbetas](#). Instead of having one y and many xs we have many ys and one x.

**Value**

A matrix with the constant (alpha) and the slope (beta) for each simple linear regression. If the p-value is set to TRUE, the correlation of each y with the x is calculated along with the relevant p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[allbetas](#), [correls](#), [univglms](#)

**Examples**

```
y <- matnorm(100, 100)
x <- rnorm(100)
a <- mvbetas(y, x, pvalue = FALSE)
b <- matrix(nrow = 100, ncol = 2)
z <- cbind(1, x)

a <- mvbetas(y, x)
b[2, ] <- coef( lm.fit( z, y[, 1] ) )
b[2, ] <- coef( lm.fit( z, y[, 2] ) )
x <- NULL
```

---

Many non parametric multi-sample tests  
*Many multi-sample tests*

---

**Description**

Many multi-sample tests.

**Usage**

```
kruskaltests(x, ina, logged = FALSE)
cqtests(x, treat, block, logged = FALSE)
```

**Arguments**

x	A matrix with the data, where the rows denote the samples (and the two groups) and the columns are the variables.
ina	A numerical vector with 1s, 2s, 3s and so on indicating the two groups. Be careful, the function is desinged to accept numbers greater than zero.
treat	In the case of the Cochran's Q test, this argument plays the role of the "ina" argument.
block	This item denotes the subjects which are the same. Similarly to "ina" a numeric vector with 1s, 2s, 3s and so on.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

The "kruskaltests" performs the Kruskal-Wallis non parametric alternative to analysis of variance test. The "cqtests" performs the Cochran's Q test for the equality of more than two groups whose values are strictly binary (0 or 1). This is a generalisation of the McNemar's test in the multi-sample case.

**Value**

A matrix with the test statistic and the p-value of each test.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[block.anovas](#), [ftests](#)

**Examples**

```
x <- matrix( rexp(300 * 200), ncol = 200 )
ina <- rbinom(300, 3, 0.6) + 1
kruskaltests(x, ina)
x <- matrix( rbinom(300 * 200, 1, 0.6), ncol = 200 )
treat <- rep(1:3, each = 100)
block <- rep(1:3, 100)
cqtests(x, treat, block)
x <- NULL
```

---

Many odds ratio tests *Many odds ratio tests*

---

**Description**

It performs very many odds ratio tests.

**Usage**

```
odds(x, y = NULL, ina, logged = FALSE)
```

**Arguments**

x	A matrix with the data, where the rows denote the observations and the columns are the variables. They must be 0s and 1s only.
y	A second matrix with the data of the second group. If this is NULL (default value) then the argument ina must be supplied. Notice that when you supply the two matrices the procedure is two times faster. They must be 0s and 1s only.
ina	A numerical vector with 1s and 2s indicating the two groups. Be careful, the function is designed to accept only these two numbers. In addition, if your "y" is NULL, you must specify "ina".
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

Many odds ratio tests are performed.

**Value**

A matrix with the test statistic and the p-value (or their logarithm) of each test.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Mosteller Frederick (1968). Association and Estimation in Contingency Tables. Journal of the American Statistical Association. 63(321):1-28.

Edwards A.W.F. (1963). The measure of association in a 2x2 table. Journal of the Royal Statistical Society, Series A. 126(1):109-114.

**See Also**

[odds.ratio](#), [g2Test\\_univariate](#)

**Examples**

```
x <- matrix( rbinom(100 * 100, 1, 0.5), ncol = 100 )
ina <- rep(1:2, each = 50)
a <- odds(x, ina = ina)
```

---

Many one sample goodness of fit tests for categorical data

*Many one sample goodness of fit tests for categorical data*

---

**Description**

Many one sample goodness of fit tests for categorical data.

**Usage**

```
cat.goftests(x, props, type = "gsquare", logged = FALSE)
```

**Arguments**

x	A matrix with the data, where the rows denote the samples and the columns are the variables. The data must be integers and be of the form 1, 2, 3, and so on. The minimum must be 1, and not zero.
props	The assumed distribution of the data. A vector or percentages summing to 1.
type	Either Pearson's $\chi^2$ test ("chisquare") is used or the $G^2$ test ("gsquare", default value).
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

Given a matrix of integers, where each column refers to a sample, the values of a categorical variable the function tests whether these values can be assumed to fit a specific distribution.

**Value**

A matrix with the test statistic and the p-value of each test.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[ttests](#), [ttest](#), [ftests](#)

**Examples**

```
x <- matrix( rbinom(300 * 100, 4, 0.6), ncol = 100 ) + 1
props <- dbinom(0:4, 4, 0.6)
## can we assume that each column comes from a distribution whose mass is given by props?
cat.goftests(x, props)
a1 <- cat.goftests(x, props) ## G-square test
a2 <- cat.goftests(x, props, type = "chisq") ## Chi-square test
cor(a1, a2)
mean( abs(a1 - a2) )
x <- NULL
```

---

Many one sample tests *Many one sample tests*

---

**Description**

Many one sample tests.

**Usage**

```
proptest(x, n, p, alternative = "unequal", logged = FALSE)
ttest(x, m, alternative = "unequal", logged = FALSE, conf = NULL)
vartest(x, sigma, alternative = "unequal", logged = FALSE, conf = NULL)
```

**Arguments**

x	A matrix with numerical data. Each column of the matrix corresponds to a sample, or a group. In the case of the "proptest" this is a vector integers ranging from 0 up to n. It is the number of "successes".
n	This is for the "proptest" only and is a vector with integer numbers specifying the number of tries for the proptest. Its size is equal to the size of x.
p	A vector with the assumed probabilities of success in the "proptest". Its size is equal to the number of columns of the matrix x.
m	A vector with the assumed means. Its size is equal to the number of columns of the matrix x.
sigma	A vector with assumed variances. Its size is equal to the number of columns of the matrix x.
alternative	The type of hypothesis to be checked. Equal to ("unequal"), grater than("greater") or less than ("less") the assumed parameter.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?
conf	If you want confidence intervals to be returned specify the confidence level, otherwise leave it NULL.

**Details**

Despite the functions having been written in R, they are very fast.

**Value**

For all tests except for the "sftests" a matrix with two columns, the test statistic and the p-value respectively.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[ftests](#), [ttests](#)

**Examples**

```
R <- 100
## protest
x <- rbinom(R, 50, 0.6)
n <- rep(50, R)
p <- rep(0.6, R)
a1 <- proptest(x, n, p, "unequal", logged = FALSE)
res<-sum( a1[, 2] < 0.05 ) / R

## vartest
x <- matnorm(100, 100)
a2 <- vartest(x, rep(1, R) )
res<-sum( a2[, 2] < 0.05 )

## ttest
a4 <- ttest(x, numeric(R) )
res<-sum(a4[, 2] < 0.05) / R
x <- NULL
```

---

Many random intercepts LMMs for balanced data with a single identical covariate.

*Many random intercepts LMMs for balanced data with a single identical covariate*

---

**Description**

Many random intercepts LMMs for balanced data with a single identical covariate.

**Usage**

```
colrint.regbx(y, x, id)
```

**Arguments**

y	A numerical matrix with the data. The subject values.
x	A numerical vector with the same length as the number of rows of y indicating the fixed predictor variable. Its values are the same for all levels of y. An example of this x is time which is the same for all subjects.
id	A numerical variable with 1, 2, ... indicating the subject.

**Details**

This is a special case of a balanced random intercepts model with a compound symmetric covariance matrix and one single covariate which is constant for all replicates. An example, is time, which is the same for all subjects. Maximum likelihood estimation has been performed. In this case the mathematics exist in a closed formula (Demidenko, 2013, pg. 67-69).

This is the generalisation of `rint.regbx` to matrices. Assume you have many observations, gene expressions over time for example, and you want to calculate the random effects or something else for each expression. Instead of using a "for" loop with `rint.regbx` function we have used `amtrix` operations to make it even faster.

**Value**

A list including:

info	A matrix with the random intercepts variance (between), the variance of the errors (within), the log-likelihood, the deviance (twice the log-likelihood) and the BIC. In the case of "rint.reg" it also includes the number of iterations required by the generalised least squares.
be	The estimated regression coefficients, which in the case of "rint.regbx" are simply two: the constant and the slope (time effect).
ranef	A matrix with random intercepts effects. Each row corresponds to a column in y. Instead of having a matrix with the same number of columns as y we return a transposed matrix.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Eugene Demidenko (2013). *Mixed Models: Theory and Applications with R*, 2nd Edition. New Jersey: Wiley & Sons (excellent book).

**See Also**

`colvarcomps.mle`, `rint.regbx`, `rm.lines`, `varcomps.mom`, `rint.reg`

**Examples**

```
y <- matrix( rnorm(100 * 50), ncol = 50)
id <- rep(1:20, each = 5)
x <- rep(1:10, 10)
a<- colrint.regbx(y, x, id)
```

---

Many regression based tests for single sample repeated measures

*Many regression based tests for single sample repeated measures*

---

**Description**

Many regression based tests for single sample repeated measures.

**Usage**

```
rm.lines(y, x, logged = FALSE)
rm.anovas(y, x, logged = FALSE)
```

**Arguments**

- |        |  |
|--------|--|
| y      | A matrix with the data, where each column refers to a different sample of subjects. For example, the first column is the repeated measurements of a sample of subjects, the second column contains repeated measurements of a second sample of subjects and so on. Within each column, the measurements of each subjects are stacked one upon the other. Say for examples there are n subjects and each of them has been measured d times (in time or at different experimental conditions). We put these in a matrix with just one column. The first d rows are the measurements of subject 1, the next d rows are the measurements of subject 2 and so on. |
| x      | A numerical vector with time (usually) or the the predictor variable. For example the temperature, or the pressure. See the details for more information. Its length is equal to the time points for example, i.e. it must not have the same length as the number of rows of y. For the "rm.lines" this is a continuous variable.<br>For the "rm.anovas" this is treated as a categorical variable, indicating say the type of experimental condition, but no difference between the points is important. Hence, for this function only, x can also be a facto variable.   |
| logged | Should the p-values be returned (FALSE) or their logarithm (TRUE)?   |

**Details**

In order to see whether the repeated measurements are associated with a single covariate, e.g. time we perform many regressions and each time calculate the slope. For each subject, its regression slope with the covariate is calculated. In the end a t-test for the hypothesis that the average slopes is zero is performed. The regression slopes ignore that the measurements are not independent, but

note that the slopes are independent, because they come from different subjects. This is a simple, summary statistics based approach found in Davis (2002), yet it can provide satisfactory results.

The second approach ("rm.anovas") found in Davis (2002) is the usual repeated measures ANOVA. In this case, suppose you have taken measurements on one or more variables from the same group of people. See the example below on how to put such data.

### Value

A matrix with the test statistic (t-test) and its associated p-value.

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

### References

Charles S. Davis (2002). Statistical methods for the analysis of repeated measures. Springer-Verlag, New York.

### See Also

[rint.regbx](#), [rint.reg](#), [varcomps.mle](#)

### Examples

```
y <- c(74.5,81.5,83.6,68.6,73.1,79.4,
75.5,84.6,70.6,87.3,73.0,75.0,
68.9,71.6,55.9,61.9,60.5,61.8,
57.0,61.3,54.1,59.2,56.6,58.8,
78.3,84.9,64.0,62.2,60.1,78.7,
54.0,62.8,63.0,58.0,56.0,51.5,
72.5,68.3,67.8,71.5,65.0,67.7,
80.8,89.9,83.2,83.0,85.7,79.6)
y <- as.matrix(y)
### the first 6 measurements are from subject 1, measurments 7-12 are from subject 2,
## measurements 13-18 are from subject 3 and so on.
x <- c(-10, 25, 37, 50, 65, 80) ## all subjects were measured at the same time points
res<-rm.lines(y, x) ## Is linear trend between the measurements and the temperature?
res<-rm.anovas(y, x) ## Tests whether the means of the individuals are the same
## the temperature is treated as categorical variable here.

## fake example
y <- matnorm(10, 4)
## the y matrix contains 4 repeated measurements for each of the 10 persons.
x <- 1:4
## we stack the measurements of each subject, one under the other in a matrix form.
y1 <- matrix( t(y) )
res<-rm.anovas(y1, x) ## perform the test
z <- matrix( rnorm(20 * 8), ncol = 2) ## same example, but with 2 sets of measurements.
```

```
res<-rm.anovas(z, x)
```

---

Many score based regressions

*Many score based regressions*

---

## Description

Many score based GLM regressions.

## Usage

```
score.glm(y, x, oiko = NULL, logged = FALSE)
score.multinomregs(y, x, logged = FALSE)
score.negbinregs(y, x, type = 1, logged = FALSE)
score.weibregs(y, x, logged = FALSE)
score.betaregs(y, x, logged = FALSE)
score.gamaregs(y, x, logged = FALSE)
score.expregs(y, x, logged = FALSE)
score.invgaussregs(y, x, logged = FALSE)
score.ztpregs(y, x, logged = FALSE)
score.geomregs(y, x, logged = FALSE)
```

## Arguments

- |        |   |
|--------|---|
| y      | A vector with either discrete or binary data for the Poisson, geometric, or negative binomial and binary logistic regressions, respectively. A vector with discrete values or factor values for the multinomial regression. If the vector is binary and choose multinomial regression the function checks and transfers to the binary logistic regression.<br><br>For the Weibull, gamma, inverse Gaussian and exponential regressions they must be strictly positive data, lifetimes or durations for example. For the beta regression they must be numbers between 0 and 1. For the zero truncated Poisson regression (score.ztpregs) they must be integer valued data strictly greater than 0. |
| x      | A matrix with data, the predictor variables.  |
| oiko   | This can be either "poisson" or "binomial". If you are not sure leave it NULL and the function will check internally.   |
| type   | This argument is for the negative binomial distribution. In the negative binomial you can choose which way you prefer. Type 1 is for small sample sizes, whereas type 2 is for larger ones as is faster.  |
| logged | A boolean variable; it will return the logarithm of the pvalue if set to TRUE.  |

## Details

Instead of maximising the log-likelihood via the Newton-Raphson algorithm in order to perform the hypothesis testing that  $\beta_i = 0$  we use the score test. This is dramatically faster as no model needs to be fitted. The first derivative (score) of the log-likelihood is known and in closed form and under the null hypothesis the fitted values are all equal to the mean of the response variable  $y$ . The variance of the score is also known in closed form. The test is not the same as the likelihood ratio test. It is size correct nonetheless but it is a bit less efficient and less powerful. For big sample sizes though (5000 or more) the results are the same. We have seen via simulation studies is that it is size correct to large sample sizes, at least a few thousands. You can try for yourselves and see that even with 500 the results are pretty close. The score test is pretty faster than the classical log-likelihood ratio test.

## Value

A matrix with two columns, the test statistic and its associated p-value. For the Poisson and logistic regression the p-value is derived via the t distribution, whereas for the multinomial regressions via the  $\chi^2$  distribution.

## Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

## References

- Tsagris M., Alenazi A. and Fafalios S. (2020). Computationally efficient univariate filtering for massive data. *Electronic Journal of Applied Statistical Analysis*, 13(2):390-412.
- Hosmer DW. JR, Lemeshow S. and Sturdivant R.X. (2013). *Applied Logistic Regression*. New Jersey, Wiley, 3rd Edition.
- Campbell M.J. (2001). *Statistics at Square Two: Understand Modern Statistical Applications in Medicine*, pg. 112. London, BMJ Books.
- Draper N.R. and Smith H. (1988). *Applied regression analysis*. New York, Wiley, 3rd edition.
- McCullagh Peter, and John A. Nelder. *Generalized linear models*. CRC press, USA, 2nd edition, 1989.
- Agresti Alan (1996). *An introduction to categorical data analysis*. New York: Wiley.
- Joseph M.H. (2011). *Negative Binomial Regression*. Cambridge University Press, 2nd edition.

## See Also

[univglms](#), [logistic\\_only](#), [poisson\\_only](#), [regression](#)

## Examples

```
#x <- matnorm(500, 500)
#y <- rbinom(500, 1, 0.6) ## binary logistic regression
#a2 <- score.glm(y, x)
```

```
#y <- rweibull(500, 2, 3)
#a <- score.weibregs(y, x)
#mean(a[, 2] < 0.05)
#x <- NULL
```

---

Many Shapiro-Francia normality tests

*Many Shapiro-Francia normality tests*

---

## Description

Many Shapiro-Francia normality tests.

## Usage

```
sftests(x, logged = FALSE)
sftest(x, logged = FALSE)
```

## Arguments

x	A matrix with the data, where the rows denote the observations and the columns are the variables. In the case of a single sample, then this must be a vector and "sftest" is to be used.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

## Details

The Shapiro-Francia univariate normality test is performed for each column (variable) of the matrix x.

## Value

A matrix with the squared correlation between the ordered values and the standard normal ordered statistics, the test statistic and the p-value of each test. If the "sftest" has been used, the output is a vector with these three elements.

## Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

## References

Royston J. P. (1983). A simple method for evaluating the Shapiro-Francia W' test of non-normality. *The Statistician*, 32(3): 297-300.

Mbah A. K. & Paothong A. (2015). Shapiro-Francia test compared to other normality test using expected p-value. *Journal of Statistical Computation and Simulation*, 85(15): 3002-3016.

**See Also**

[ttests](#), [ttest](#), [ftests](#)

**Examples**

```
x <- matnorm(200, 100)
sftests(x)
a <- sftests(x)
mean(a[, 3]<0.05)
x <- rnorm(100)
res<-sftest(x)
```

---

Many simple geometric regressions

*Many simple geometric regressions*

---

**Description**

Many simple geometric regressions.

**Usage**

```
geom.regs(y, x, tol = 1e-07, type = 1, logged = FALSE, parallel = FALSE, maxiters = 100)
```

**Arguments**

<code>y</code>	The dependent variable, count data.
<code>x</code>	A matrix with the independent variables.
<code>tol</code>	The tolerance value to terminate the Newton-Raphson algorithm.
<code>type</code>	Type 1 refers to the case where the minimum is zero and type 2 for the case of the minimum being 1.
<code>logged</code>	A boolean variable; it will return the logarithm of the pvalue if set to TRUE.
<code>parallel</code>	Do you want this to be executed in parallel or not. The parallel takes place in C++, and the number of threads is defined by each system's available cores.
<code>maxiters</code>	The max number of iterations that can take place in each regression.

**Details**

Many simple geometric regressions are fitted.

**Value**

A matrix with the test statistic values, their relevant (logged) p-values and the BIC values.

**Author(s)**

Stefanos Fafalios

R implementation and documentation: Stefanos Fafalios <stefanosfafalios@gmail.com>

**See Also**

[poisson\\_only](#), [prop.regs](#), [score.geomregs](#)

**Examples**

```
y <- rgeom(100, 0.6)
x <- matrix( rnorm(100 * 50), ncol = 50)
a <- geom.regs(y, x)
x <- NULL
```

---

Many simple linear mixed model regressions

*Many simple linear mixed model regressions*

---

**Description**

Many simple linear mixed model regressions with random intercepts only.

**Usage**

```
rint.regs(y, x, id, tol = 1e-08, logged = FALSE, parallel = FALSE, maxiters = 100)
```

**Arguments**

<code>y</code>	A numerical vector with the data. The subject values, the clustered data.
<code>x</code>	A numerical matrix with data ,the independent variables.
<code>id</code>	A numerical variable with 1, 2, ... indicating the subject. Unbalanced design is of course welcome.
<code>tol</code>	The tolerance value to terminate the Newton-Raphson algorithm. This is set to $10^{-9}$ by default.
<code>logged</code>	Should the p-values be returned (FALSE) or their logarithm (TRUE)?
<code>parallel</code>	Do you want this to be executed in parallel or not. The parallel takes place in C++, and the number of threads is defined by each system's available cores.
<code>maxiters</code>	The max number of iterations that can take place in each regression.

**Details**

Many linear mixed models with a single covariate are fitted. We use Newton-Raphson as described in Demidenko (2013). The test statistic is the usual F-test. This model allows for random intercepts only.

**Value**

A two-column matrix with the test statistics (Wald statistic) and the associated p-values (or their logarithm).

**Author(s)**

Stefanos Fafalios.

R implementation and documentation: Stefanos Fafalios <stefanosfafalios@gmail.com>.

**References**

Eugene Demidenko (2013). *Mixed Models: Theory and Applications with R*, 2nd Edition. New Jersey: Wiley & Sons (excellent book).

**See Also**

[rint.reg](#), [allbetas.univglms](#), [score.glms](#), [logistic\\_only](#)

**Examples**

```
## not a so good example
y <- rnorm(100)
id <- sample(1:10, 100, replace = TRUE)
x <- matrix(rnorm(100 * 100), ncol = 100)
a <- rint.regs(y, x, id)
x <- NULL
```

---

Many simple linear regressions coefficients

*Simple linear regressions coefficients*

---

**Description**

Simple linear regressions coefficients.

**Usage**

```
allbetas(y, x, pvalue = FALSE, logged = FALSE)
```

**Arguments**

<code>y</code>	A numerical vector with the response variable.
<code>x</code>	A matrix with the data, where rows denotes the observations and the columns contain the independent variables.
<code>pvalue</code>	If you want a hypothesis test that each slope (beta coefficient) is equal to zero set this equal to TRUE. It will also produce all the correlations between y and x.
<code>logged</code>	A boolean variable; it will return the logarithm of the pvalue if set to TRUE.

**Value**

A matrix with the constant (alpha) and the slope (beta) for each simple linear regression. If the p-value is set to TRUE, the correlation of each y with the x is calculated along with the relevant test statistic and its associated p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[mvbetas](#), [correels](#), [univglms](#), [colsums](#), [colVars](#)

**Examples**

```
x <- matrix( rnorm(100 * 50), ncol = 50 )
y <- rnorm(100)
r <- cor(y, x) ## correlation of y with each of the xs
a <- allbetas(y, x) ## the coefficients of each simple linear regression of y with x
x <- NULL
```

---

Many simple multinomial regressions

*Many simple multinomial regressions*

---

**Description**

Many simple multinomial regressions.

**Usage**

```
multinom.regs(y, x, tol = 1e-08, logged = FALSE, parallel = FALSE, maxiters = 100)
```

**Arguments**

y	The dependent variable, either a numerical variable or a factor variable.
x	A matrix with the independent variables.
tol	The tolerance value to terminate the Newton-Raphson algorithm.
logged	A boolean variable; it will return the logarithm of the pvalue if set to TRUE.
parallel	Do you want this to be executed in parallel or not. The parallel takes place in C++, and the number of threads is defined by each system's available cores.
maxiters	The maximum number of iterations that can take place in each regression.

**Details**

Many simple multinomial regressions are fitted.

**Value**

A matrix with the test statistic values, their relevant (logged) p-values and the BIC values.

**Author(s)**

Stefanos Fafalios

R implementation and documentation: Stefanos Fafalios <stefanosfafalios@gmail.com>

**See Also**

[poisson\\_only](#), [prop.regs](#), [score.geomregs](#)

**Examples**

```
y <- rbinom(100, 2, 0.5)
x <- matnorm(100, 100)
a <- multinom.regs(y, x)
x <- NULL
```

---

Many simple regressions for positive valued data

*Many simple regressions for positive valued data*

---

**Description**

Many simple regressions for positive valued data.

**Usage**

```
normlog.regs(y, x, tol = 1e-08, logged = FALSE, parallel = FALSE, maxiters = 100)
gammaregs(y, x, tol = 1e-07, logged = FALSE, maxiters = 100)
invgauss.regs(y, x, tol = 1e-08, logged = FALSE, maxiters = 100)
```

**Arguments**

y	The dependent variable, a numerical variable with non negative numbers for the Gamma and inverse Gaussian regressions. For the Gaussian with a log-link zero values are allowed.
x	A matrix with the independent variables.
tol	The tolerance value to terminate the Newton-Raphson algorithm.
logged	A boolean variable; it will return the logarithm of the pvalue if set to TRUE.
parallel	Do you want this to be executed in parallel or not. The parallel takes place in C++, therefore you do not have the option to set the number of cores.
maxiters	The maximum number of iterations that can take place in each regression.

**Details**

Many simple Gamma, inverse Gaussian or Gaussian regressions with a log-link are fitted.

**Value**

A matrix with the test statistic values and their relevant (logged) p-values.

**Author(s)**

Stefanos Fafalios and Michail Tsagris

R implementation and documentation: Stefanos Fafalios <stefanosfafalios@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>

**References**

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

Zakariya Yahya Algamal and Intisar Ibrahim Allyas (2017). Prediction of blood lead level in maternal and fetal using generalized linear model. International Journal of Advanced Statistics and Probability, 5(2): 65-69.

**See Also**

[normlog.reg](#), [score.glms](#), [prop.regs](#), [allbetas](#)

**Examples**

```
y <- abs( rnorm(100) )
x <- matrnorm(100, 100)
a <- normlog.regs(y, x)
b <- glm(y ~ x[, 1], family = gaussian(log) )
anova(b, test= "F")
a[1, ]
a2 <- gammaregs(y, x)
a3 <- invgauss.regs(y, x)
x <- NULL
```

---

Many tests for the dispersion parameter in Poisson distribution

*Many tests for the dispersion parameter in Poisson distribution*

---

**Description**

Many tests for the dispersion parameter in Poisson distribution.

**Usage**

```
colpoisdisp.tests(y, alternative = "either", logged = FALSE)
colpois.tests(y, logged = FALSE)
```

**Arguments**

<code>y</code>	A numerical matrix with count data, 0, 1,...
<code>alternative</code>	Do you want to test specifically for either over or underspersion ("either"), overdispersion ("over") or underspersion ("under")?
<code>logged</code>	Set to TRUE if you want the logarithm of the p-value.

**Value**

A matrix with two columns, the test statistic and the (logged) p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Yang Zhao, James W. Hardin, and Cheryl L. Addy. (2009). A score test for overdispersion in Poisson regression based on the generalized Poisson-2 model. *Journal of statistical planning and inference* 139(4):1514-1521.

Dimitris Karlis and Evdokia Xekalaki (2000). A Simulation Comparison of Several Procedures for Testing the Poisson Assumption. *Journal of the Royal Statistical Society. Series D (The Statistician)*, 49(3): 355-382.

Bohning, D., Dietz, E., Schaub, R., Schlattmann, P. and Lindsay, B. (1994) The distribution of the likelihood ratio for mixtures of densities from the one-parameter exponential family. *Annals of the Institute of Statistical Mathematics*, 46(): 373-388.

**See Also**

[poisson.mle](#), [negbin.mle](#), [poisson.anova](#), [poisson.anovas](#), [poisson\\_only](#)

**Examples**

```
y <- matrix(rnbinom(100* 50, 10, 0.6), ncol = 50)
a1 <- colpoisdisp.tests(y, "over")
b1 <- colpois.tests(y)

y <- matrix(rpois(100* 50, 10), ncol = 50)
a2 <- colpoisdisp.tests(y, "either")
b2 <- colpois.tests(y)
y <- NULL
```

---

Many two-way ANOVAs    *Many two-way ANOVAs*

---

**Description**

Many two-way ANOVAs.

**Usage**

```
twoway.anovas(y, x1, x2, interact = FALSE, logged = FALSE)
```

**Arguments**

y	A matrix with the data, where the rows denote the observations (and the two groups) and the columns are the variables.
x1	A numerical vector with 1s, 2s, 3s and so on indicating the two groups. Alternatively it can be a factor variable. This is the one factor.
x2	A numerical vector with 1s, 2s, 3s and so on indicating the two groups. Alternatively it can be a factor variable. This is the other factor.
interact	A boolean variable specifying whether you want to test for interaction.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

The classical two-way ANOVA design is performed. Note that the design must be balanced. For every combination of values of the two factors, x1 and x2 the same number of observations must exist. If that's not the case, regression models must be used.

**Value**

A matrix with the test statistic and the p-value of each test.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

D.C. Montgomery (2001). Design and analysis of experiments (5th Edition). New York: John Wiley & Sons.

**See Also**

[ancovas](#), [ftests](#), [ttests](#)

**Examples**

```

y <- as.matrix( rnorm(125) )
x1 <- rep(1:5, 25)
x2 <- rep(1:5, each = 25)
x1 <- factor(x1)
x2 <- factor(x2)
res<-anova( lm(y ~ x1 + x2) )
res<-tway.anovas(y, x1, x2)
res<-anova( lm(y ~ x1*x2) )
res<-tway.anovas(y, x1, x2, interact = TRUE)
y <- matnorm(125, 100)
a1 <- tway.anovas(y, x1, x2)
a2 <- tway.anovas(y, x1, x2, interact = TRUE)
y <- NULL

```

---

Many univariate generalised linear models

*Many univariate generalised linear regressions*

---

**Description**

It performs very many univariate generalised linear regressions.

**Usage**

```
univglms(y, x, oiko = NULL, logged = FALSE)
```

```
univglms2(y, x, oiko = NULL, logged = FALSE)
```

**Arguments**

- |        |   |
|--------|---|
| y      | The dependent variable. It can be a factor or a numerical variable with two values only (binary logistic regression), a discrete valued vector (count data) corresponding to a poisson regression or a numerical vector with continuous values (normal regression).   |
| x      | A matrix with the data, where the rows denote the samples (and the two groups) and the columns are the variables. For the "univglms" only continuous variables are allowed. You are advised to standardise the data before hand to avoid numerical overflow or similar issues. If you see NaN in the outcome, this might be the case. For the "univglms2" categorical variables are allowed and hence this accepts data.frames. In this case, the categorical variables must be given as factor variables, otherwise you might get wrong results. |
| oiko   | This can be either "normal", "poisson", "quasipoisson" or "binomial". If you are not sure leave it NULL and the function will check internally. However, you might have discrete data (e.g. years of age) and want to perform many simple linear regressions. In this case you should specify the family.   |
| logged | A boolean variable; it will return the logarithm of the pvalue if set to TRUE.  |

**Details**

If you specify no family of distributions the function internally checks the type of your data and decides on the type of regression to perform. The function is written in C++ and this is why it is very fast. It can accept thousands of predictor variables. It is useful for univariate screening. We provide no p-value correction (such as *fdr* or *q-values*); this is up to the user.

**Value**

A matrix with the test statistic and the p-value for each predictor variable.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Draper, N.R. and Smith H. (1988). Applied regression analysis. New York, Wiley, 3rd edition.

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

[logistic\\_only](#), [poisson\\_only](#), [allbetas](#), [correels](#), [regression](#)

**Examples**

```
x <- matnorm(100, 50)
y <- rbinom(100, 1, 0.6) ## binary logistic regression
a1 <- univglms(y, x)
a2 <- glm(y ~ x[, 1], binomial)$deviance
a2 <- glm(y ~ 1, binomial)$null.dev - a2
x <- NULL
```

---

Many univariate simple linear regressions

*Many univariate simple linear regressions*

---

**Description**

It performs very many univariate simple linear regressions with or without categorical variables.

**Usage**

```
regression(x, y, poia = NULL, logged = FALSE)
```

**Arguments**

x	A data.frame or a matrix with the data, where the rows denote the samples (and the two groups) and the columns are the variables. A data frame is expected if you have categorical predictor variables. If you only have continuous predictor variables you should use the function <code>allbetas</code> instead as it is faster.
y	The dependent variable; a numerical vector.
poia	If the "x" is a data.frame and you know the indices of the columns which are categorical variables supply it here.
logged	Do you want the logarithm of the p-values be returned? The default value is FALSE.

**Details**

Some parts of the function will be transferred in C++. It can accept thousands of predictor variables. It is useful for univariate screening. We provide no p-value correction (such as `fdr` or `q-values`); this is up to the user.

**Value**

A matrix with two columns, the test statistic value and its corresponding (logged) p-value.

**Author(s)**

Manos Papadakis <papadakm95@gmail.com>

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Draper, N.R. and Smith H. (1988). Applied regression analysis. New York, Wiley, 3rd edition.

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

`univglms`, `allbetas`, `correls`, `univglms`, `mvbetas`

**Examples**

```
y <- rnorm(150)
a <- regression(iris, y)
a
summary(lm(y ~ iris[, 5]) ) ## check the F-test
```

---

Many univariate simple logistic and Poisson regressions  
*Many univariate simple binary logistic regressions*

---

**Description**

It performs very many univariate simple binary logistic regressions.

**Usage**

```
logistic_only(x, y, tol = 1e-09, b_values = FALSE)
poisson_only(x, y, tol = 1e-09, b_values = FALSE)
```

**Arguments**

x	A matrix with the data, where the rows denote the samples (and the two groups) and the columns are the variables. Currently only continuous variables are allowed.
y	The dependent variable; a numerical vector with two values (0 and 1) for the logistic regressions and a vector with many discrete values (count data) for the Poisson regressions.
tol	The tolerance value to terminate the Newton-Raphson algorithm.
b_values	Do you want the values of the coefficients returned? If yes, set this to TRUE.

**Details**

The function is written in C++ and this is why it is very fast. It can accept thousands of predictor variables. It is useful for univariate screening. We provide no p-value correction (such as *fdr* or *q-values*); this is up to the user.

**Value**

A vector with the deviance of each simple binary logistic regression model for each predictor variable.

**Author(s)**

Manos Papadakis <papadakm95@gmail.com>

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

[univglms](#), [score.glm](#)s, [prop.regs](#), [quasi.poisson\\_only](#), [allbetas](#), [correls](#), [regression](#)

**Examples**

```
## 300 variables, hence 300 univariate regressions are to be fitted
x <- matrix( rnorm(100 * 300), ncol = 300 )

## 100 observations in total
y <- rbinom(100, 1, 0.6)  ## binary logistic regression
a1 <- logistic_only(x, y)

a2 <- glm(y ~ x[, 1], binomial)$deviance
a2 <- as.vector(a2)

y <- rpois(100, 10)
a1 <- poisson_only(x, y)

a1 <- x <- NULL
```

---

Many univariate simple quasi poisson regressions

*Many univariate simple poisson regressions*

---

**Description**

It performs very many univariate simple poisson regressions.

**Usage**

```
quasi.poisson_only(x, y, tol = 1e-09, maxiters = 100)
```

**Arguments**

<code>x</code>	A matrix with the data, where the rows denote the samples (and the two groups) and the columns are the variables. Currently only continuous variables are allowed.
<code>y</code>	The dependent variable; a numerical vector with many discrete values (count data).
<code>maxiters</code>	The maximum number of iterations after which the Newton-Raphson algorithm is terminated.
<code>tol</code>	The tolerance value to terminate the Newton-Raphson algorithm.

**Details**

The function is written in C++ and this is why it is very fast. It can accept thousands of predictor variables. It is useful for univariate screening. We provide no p-value correction (such as *fdr* or *q-values*); this is up to the user.

**Value**

A matrix with the deviance and the estimated phi parameter (dispersion parameter) of each simple poisson regression model for each predictor variable.

**Author(s)**

Manos Papadakis <papadakm95@gmail.com> and Stefanos Fafalios <stefanosfafalios@gmail.com>  
R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>, Manos Papadakis <papadakm95@gmail.com> and Stefanos Fafalios <stefanosfafalios@gmail.com>.

**References**

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

[poisson\\_only](#), [univglms](#), [logistic\\_only](#), [allbetas](#), [regression](#)

**Examples**

```
## 200 variables, hence 200 univariate regressions are to be fitted
x <- matrix( rnorm(100 * 200), ncol = 200 )
y <- rpois(100, 10)
poisson_only(x, y)
b1 <- poisson_only(x, y)
b2 <- quasi.poisson_only(x, y)

b1<-b2<-x<-y<-NULL
```

---

Many Welch's F-tests    *Many Welch's F-tests*

---

**Description**

Many Welch's F-tests.

**Usage**

```
colanovas(y, x, logged = FALSE)
```

**Arguments**

y	A numerical vector with the dependent variable.
x	A matrix with the data, where the rows denote the samples (and the two groups) and the columns are the variables. This must be a matrix with the categorical variables as numbers, starting from 1. Welch's F-test is performed for each variable.
logged	A boolean variable; it will return the logarithm of the pvalue if set to TRUE.

**Details**

For each categorical variable in the x matrix Welch's F test is performed. This is the opposite of [ftests](#), where there are many dependent variables and one categorical variable.

**Value**

A matrix with the test statistic and the p-value for each predictor variable.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Draper, N.R. and Smith H. (1988). Applied regression analysis. New York, Wiley, 3rd edition.

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

[regression](#), [ftests](#), [allbetas](#), [correls](#)

**Examples**

```
y <- rnorm(100)
x <- matrix( rbinom(100 * 50, 2, 0.5) + 1 , ncol = 50)
a <- colanovas(y, x)
x <- NULL
```

---

Match

*Match*

---

**Description**

Return the positions of its first argument that matches in its second.

**Usage**

```
Match(x, key=NULL)
```

**Arguments**

x                    A numeric vector.  
key                  The value/vector for searching in vector x. For now let it NULL. **don't use it!**.

**Details**

This function implements the R's `"match"` function. This version basically calculates the `match(x,sort(unique(x)))` for now. Do not use the argument `key!`

**Value**

Returns the position/positions of the given key/keys in the `x` vector.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>

**See Also**

[match](#)

**Examples**

```
y <- rnorm(100)
a <- Match(y)
b <- -50
all.equal(as.vector(a), as.vector(b))
```

---

Matrix multiplication *Matrix multiplication, Cross and Tcross product*

---

**Description**

Matrix multiplication, Cross and Tcross product.

**Usage**

```
mat.mult(x, y)
Crossprod(x,y)
Tcrossprod(x,y)
```

**Arguments**

<code>x</code>	A numerical matrix.
<code>y</code>	A numerical matrix.

**Details**

The functions performs matrix multiplication, croos product and transpose cross product. There are faster(!) than R's function for large matrices. Depending on the computer, maybe higher dimensions are required for the function to make a difference. The function runs in parallel in C++.

**Value**

A matrix, the result of the matrix multiplication.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>

**See Also**

[transpose](#), [colsums](#)

**Examples**

```
x <- matnorm(100, 100)
y <- matnorm(100, 100)
#a <- x %**% y
#b <- mat.mult(x, y) #Always execute in parallel
#b <- Crossprod(x, y) #Always execute in parallel
#b <- Tcrossprod(x, y) #Always execute in parallel
x <- NULL
y <- NULL
b <- NULL
```

---

Matrix with all pairs of t-tests

*Matrix with all pairs of t-tests*

---

**Description**

Matrix with all pairs of t-tests.

**Usage**

```
allttests(x, y = NULL, ina, logged = FALSE)
ttests.pairs(x, logged = FALSE)
```

**Arguments**

x	A numerical matrix with the data.
y	For the case of "all.tests", if you have the second group or sample provide it here, otherwise leave it NULL. For the case of "ttests.pairs" this is not required.
ina	If you have the data in one matrix then provide this indicator variable separating the samples. This numerical vector must contain 1s and 2s only as values. For the case of "ttests.pairs" this is not required.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

The function does all the pairwise t-tests assuming unequal variances (Welch's t-test). The "all.ttests" does all the pairs formed by "cutting" the matrices x and y in two and everything between them. The "ttests.pairs" accepts a matrix x and does all the pairs of t-tests. This is similar to the correlation matrix style.

**Value**

A list including:

stat	A matrix with t-test statistic for each pair of variables.
pvalue	A matrix with the corresponding p-values.
dof	A matrix with the relevant degrees of freedom.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[ttests](#), [ftests](#), [ttest](#), [g2Test\\_univariate](#)

**Examples**

```
x <- as.matrix( iris[1:100, 1:4] )
ina <- as.numeric(iris[1:100, 5])
a <- allttests(x, ina = ina)
b <- ttests.pairs(x) ## less tests
```

---

Matrix with G-square tests of independence

*Matrix with G-square tests of independence*

---

**Description**

Matrix with G-square tests of independence with and without permutations.

**Usage**

```
g2Test_univariate(data, dc)
g2Test_univariate_perm(data, dc, nperm)
chi2Test_univariate(data, dc)
```

**Arguments**

data	A numerical matrix with the data. <b>The minimum must be 0, otherwise the function can crash or will produce wrong results.</b> The data must be consecutive numbers.
dc	A numerical value equal to the number of variables (or columns of the data matrix) indicating the number of distinct, unique values (or levels) of each variable. Make sure you give the correct numbers here, otherwise the degrees of freedom will be wrong.
nperm	The number of permutations. The permutations test is slower than without permutations and should be used with small sample sizes or when the contingency tables have zeros. When there are few variables, R's "chisq.test" function is faster, but as the number of variables increase the time difference with R's procedure becomes larger and larger.

**Details**

The function does all the pairwise  $G^2$  test of independence and gives the position inside the matrix. The user must build the associations matrix now, similarly to the correlation matrix. See the examples of how to do that. The p-value is not returned, we live this to the user. See the examples of how to obtain it.

**Value**

A list including:

statistic	The $G^2$ or $chi^2$ test statistic for each pair of variables.
pvalue	This is returned when you have selected the permutation based $G^2$ test.
x	The row or variable of the data.
y	The column or variable of the data.
df	The degrees of freedom of each test.

**Author(s)**

Giorgos Borboudakis. The permutation version used a C++ code by John Burkardt.  
R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**References**

- Tsagris M. (2017). Conditional independence test for categorical data using Poisson log-linear model. *Journal of Data Science*, 15(2):347-356.
- Tsamardinos, I., & Borboudakis, G. (2010). Permutation testing improves Bayesian network learning. In *Joint European Conference on Machine Learning and Knowledge Discovery in Databases* (pp. 322-337). Springer Berlin Heidelberg

**See Also**

[g2Test](#), [g2Test\\_perm](#), [correls](#), [univglms](#)

## Examples

```
nvalues <- 3
nvars <- 10
nsamples <- 2000
data <- matrix( sample( 0:(nvalues - 1), nvars * nsamples, replace = TRUE ), nsamples, nvars )
dc <- rep(nvalues, nvars)
g2Test_univariate(data = data, dc = dc)
a <- g2Test_univariate(data = data, dc = dc)
pval <- pchisq(a$statistic, a$df, lower.tail = FALSE)

g <- matrix(0, nvars, nvars)
g[ cbind(a$x, a$y) ] <- a$statistic
g <- g + t(g)
diag(g) <- 0
## g ## matrix of G^2 test statistics

g<-a<-dc<-data<-NULL
```

---

Minima and maxima of two vectors/matrices and Column-row wise minima  
and maxima of two matrices

*Minima and maxima of two vectors/matrices and Column-row wise  
minima and maxima of two matrices*

---

## Description

Minima and maxima of two vectors/matrices and Column-row wise minima and maxima of two matrices.

## Usage

```
colPmax(x, y)
colPmin(x, y)
Pmax(x, y, na.rm = FALSE)
Pmin(x, y, na.rm = FALSE)
Pmin_Pmax(x, y, na.rm = FALSE)
```

## Arguments

x	A numerical vector or matrix with numbers.
y	A numerical vector with numbers.
na.rm	TRUE or FALSE for remove NAs if exists.

## Details

The parallel minima or maxima are returned. This are the same as the base functions pmax and pmin.

**Value**

A numerical vector/matrix with numbers, whose length is equal to the length of the initial matrices containing the maximum or minimum between each pair.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Sort](#), [colMins](#), [colMaxs](#), [colMedians](#)

**Examples**

```
x <- matrix(rnorm(100),10,10)
y <- matrix(rnorm(100),10,10)
res<-colPmax(x, y)
res<-colPmin(x, y)
x<-y<-NULL
```

---

Minimum and maximum     *Minimum and maximum of a vector*

---

**Description**

Minimum and maximum of a vector.

**Usage**

```
min_max(x, index=FALSE, percent = FALSE)
```

**Arguments**

x	A numerical vector with data. NAs are handled naturally.
index	A boolean value for the indices of the minimum and the maximum value.
percent	A boolean value for the percent of the positive and negative numbers.

**Value**

A vector with the relevant values, min and max.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[rowMins](#), [rowMaxs](#), [nth](#), [colrange](#), [colMedians](#), [colSort](#), [rowSort](#)

**Examples**

```
x <- rnorm(100 * 500)
s1 <- min_max(x)
s2 <- c(min(x), max(x))
```

---

Minimum and maximum frequencies

*Minimum and maximum frequencies of a vector*

---

**Description**

Minimum and maximum frequencies of a vector.

**Usage**

```
freq.min(x, na.rm = FALSE)
freq.max(x, na.rm = FALSE)
```

**Arguments**

<code>x</code>	A numerical/integer vector with data but without NAs.
<code>na.rm</code>	TRUE or FALSE for remove NAs if exists.

**Details**

Those functions are the same with `max(table(x))` or `min(table(x))` but with one exception. `freq.min` and `freq.max` will return also which value has the minimum/maximum frequency. More Efficient than `max(table(x))` or `min(table(x))`.

**Value**

A vector with 2 values, the value with minimum/maximum frequency and the frequency.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com> and Marios Dimitriadis <kmdimitriadis@gmail.com>.

**See Also**

[rowMins](#), [rowMaxs](#), [nth](#), [colrange](#), [colMedians](#), [colSort](#), [rowSort](#)

**Examples**

```
x <- rnorm(100)
f1 <- freq.min(x)
f2 <- freq.max(x)
# f1r <- min(table(x))
# f2r <- max(table(x))
# f1[2]==f1r ## the frequencies are the same
# f2[2]==f2r ## the frequencies are the same
```

---

MLE for multivariate discrete data

*MLE for multivariate discrete data*

---

**Description**

MLE for multivariate discrete data.

**Usage**

```
multinom.mle(x)
dirimultinom.mle(x, tol = 1e-07)
colpoisson.mle(x)
colgeom.mle(x, type = 1)
```

**Arguments**

<code>x</code>	A matrix with discrete valued non negative data.
<code>tol</code>	the tolerance level to terminate the Newton-Raphson algorithm for the Dirichlet multinomial distribution.
<code>type</code>	This is for the geometric distribution only. Type 1 refers to the case where the minimum is zero and type 2 for the case of the minimum being 1.

**Details**

For the Poisson and geometric distributions we simply fit independent Poisson and geometric distributions respectively.

**Value**

A list including:

<code>loglik</code>	A vector with the value of the maximised log-likelihood.
<code>param</code>	A vector of the parameters.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Johnson Norman L., Kotz Samuel and Balakrishnan (1997). Discrete Multivariate Distributions. Wiley

Minka Thomas (2012). Estimating a Dirichlet distribution. Technical report.

**See Also**

[poisson.mle](#), [zip.mle](#), [ztp.mle](#), [negbin.mle](#), [poisson.nb](#)

**Examples**

```
x <- t( rmultinom(1000, 20, c(0.4, 0.5, 0.1) ) )
res<-multinom.mle(x)
res<-colpoisson.mle(x)
x <- NULL
```

---

MLE of (hyper-)spherical distributions

*MLE of (hyper-)spherical distributions*

---

**Description**

MLE of (hyper-)spherical distributions.

**Usage**

```
vmf.mle(x, tol = 1e-07)
multivmf.mle(x, ina, tol = 1e-07, ell = FALSE)
acg.mle(x, tol = 1e-07)
iag.mle(x, tol = 1e-07)
```

**Arguments**

x	A matrix with directional data, i.e. unit vectors.
ina	A numerical vector with discrete numbers starting from 1, i.e. 1, 2, 3, 4,... or a factor variable. Each number denotes a sample or group. If you supply a continuous valued vector the function will obviously provide wrong results.
ell	This is for the multivmf.mle only. Do you want the log-likelihood returned? The default value is TRUE.
tol	The tolerance value at which to terminate the iterations.

**Details**

For the von Mises-Fisher, the normalised mean is the mean direction. For the concentration parameter, a Newton-Raphson is implemented. For the angular central Gaussian distribution there is a constraint on the estimated covariance matrix; its trace is equal to the number of variables. An iterative algorithm takes place and convergence is guaranteed. Newton-Raphson for the projected normal distribution, on the sphere, is implemented as well. Finally, the von Mises-Fisher distribution for groups of data is also implemented.

**Value**

For the von Mises-Fisher a list including:

loglik	The maximum log-likelihood value.
mu	The mean direction.
kappa	The concentration parameter.

For the multi von Mises-Fisher a list including:

loglik	A vector with the maximum log-likelihood values if ell is set to TRUE. Otherwise NULL is returned.
mi	A matrix with the group mean directions.
ki	A vector with the group concentration parameters.

For the angular central Gaussian a list including:

iter	The number of iterations required by the algorithm to converge to the solution.
cova	The estimated covariance matrix.

For the spherical projected normal a list including:

iters	The number of iteration required by the Newton-Raphson.
mesi	A matrix with two rows. The first row is the mean direction and the second is the mean vector. The first comes from the second by normalising to have unit length.
param	A vector with the elements, the norm of mean vector, the log-likelihood and the log-likelihood of the spherical uniform distribution. The third value helps in case you want to do a log-likelihood ratio test for uniformity.

**Author(s)**

Michail Tsagris R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

- Mardia, K. V. and Jupp, P. E. (2000). Directional statistics. Chichester: John Wiley & Sons.
- Sra, S. (2012). A short note on parameter approximation for von Mises-Fisher distributions: and a fast implementation of  $Is(x)$ . Computational Statistics, 27(1): 177–190.
- Tyler D. E. (1987). Statistical analysis for the angular central Gaussian distribution on the sphere. Biometrika 74(3): 579-589.

Paine P.J., Preston S.P., Tsagris M and Wood A.T.A. (2017). An Elliptically Symmetric Angular Gaussian Distribution. *Statistics and Computing* (To appear).

### See Also

[racg](#), [vm.mle](#), [rvmf](#)

### Examples

```
m <- c(0, 0, 0, 0)
s <- cov(iris[, 1:4])
#x <- racg(100, s)
#mod <- acg.mle(x)
#res<-cov2cor(mod$cova) ## estimated covariance matrix turned into a correlation matrix
#res<-cov2cor(s) ## true covariance matrix turned into a correlation matrix
#res<-vmf.mle(x)
#x <- rbind( rvmf(100,rnorm(4), 10), rvmf(100,rnorm(4), 20) )
#a <- multivmf.mle(x, rep(1:2, each = 100) )
```

---

MLE of continuous univariate distributions defined on the positive  
line

*MLE of continuous univariate distributions defined on the positive line*

---

### Description

MLE of continuous univariate distributions defined on the positive line.

### Usage

```
gammamle(x, tol = 1e-09)
chisq.mle(x, tol = 1e-09)
weibull.mle(x, tol = 1e-09, maxiters = 100)
lomax.mle(x, tol = 1e-09)
foldnorm.mle(x, tol = 1e-09)
betaprime.mle(x, tol = 1e-09)
logcauchy.mle(x, tol = 1e-09)
loglogistic.mle(x, tol = 1e-09)
halfnorm.mle(x)
invgauss.mle(x)
lognorm.mle(x)
pareto.mle(x)
expmle(x)
exp2.mle(x)
maxboltz.mle(x)
rayleigh.mle(x)
normlog.mle(x)
lindley.mle(x)
```

**Arguments**

<code>x</code>	A vector with positive valued data (zeros are not allowed).
<code>tol</code>	The tolerance level up to which the maximisation stops; set to 1e-09 by default.
<code>maxiters</code>	The maximum number of iterations the Newton-Raphson will perform.

**Details**

Instead of maximising the log-likelihood via a numerical optimiser we have used a Newton-Raphson algorithm which is faster. See wikipedia for the equations to be solved. For the t distribution we need the degrees of freedom and estimate the location and scatter parameters. If you want to fit an inverse gamma distribution simply do "gamma.mle(1/x)". The log-likelihood and the parameters are for the inverse gamma.

The "normlog.mle" is simply the normal distribution where all values are positive. Note, this is not log-normal. It is the normal with a log link. Similarly to the inverse gaussian distribution where the mean is an exponentiated. This comes from the GLM theory.

**Value**

Usually a list with three elements, but this is not for all cases.

<code>iters</code>	The number of iterations required for the Newton-Raphson to converge.
<code>loglik</code>	The value of the maximised log-likelihood.
<code>param</code>	The vector of the parameters.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Kalimuthu Krishnamoorthy, Meesook Lee and Wang Xiao (2015). Likelihood ratio tests for comparing several gamma distributions. *Environmetrics*, 26(8):571-583.

N.L. Johnson, S. Kotz and N. Balakrishnan (1994). *Continuous Univariate Distributions*, Volume 1 (2nd Edition).

N.L. Johnson, S. Kotz and N. Balakrishnan (1970). *Distributions in statistics: continuous univariate distributions*, Volume 2.

Tsagris M., Beneki C. and Hassani H. (2014). On the folded normal distribution. *Mathematics*, 2(1):12-28.

Sharma V. K., Singh S. K., Singh U. and Agiwal V. (2015). The inverse Lindley distribution: a stress-strength reliability model with application to head and neck cancer data. *Journal of Industrial and Production Engineering*, 32(3): 162-173.

You can also check the relevant wikipedia pages for these distributions.

**See Also**

[zip.mle](#), [normal.mle](#), [beta.mle](#)

**Examples**

```
x <- rgamma(100, 3, 4)
for (i in 1:20) gammamle(x)
## for (i in 1:20) fitdistr(x,"gamma")
#a <- glm(x ~ 1, gaussian(log) )
res<-normlog.mle(x)
```

---

MLE of continuous univariate distributions defined on the real line

*MLE of continuous univariate distributions defined on the real line*

---

**Description**

MLE of continuous univariate distributions defined on the real line.

**Usage**

```
normal.mle(x)
gumbel.mle(x, tol = 1e-09)
cauchy.mle(x, tol = 1e-09)
logistic.mle(x, tol = 1e-07)
ct.mle(x, tol = 1e-09)
tmle(x, v = 5, tol = 1e-08)
wigner.mle(x, tol = 1e-09)
laplace.mle(x)
```

**Arguments**

x	A numerical vector with data.
v	The degrees of freedom of the t distribution.
tol	The tolerance level up to which the maximisation stops set to 1e-09 by default.

**Details**

Instead of maximising the log-likelihood via a numerical optimiser we have used a Newton-Raphson algorithm which is faster. See wikipedia for the equation to be solved. For the t distribution we need the degrees of freedom and estimate the location and scatter parameters.

The Cauchy is the t distribution with 1 degree of freedom. If you want to fit such a distribution used the `cauchy.mle` and not the `t.mle` with 1 degree of freedom as it's faster. The Laplace distribution is also called double exponential distribution.

The `wigner.mle` refers to the wigner semicircle distribution.

**Value**

Usually a list with three elements, but this is not for all cases.

<code>iters</code>	The number of iterations required for the Newton-Raphson to converge.
<code>loglik</code>	The value of the maximised log-likelihood.
<code>param</code>	The vector of the parameters.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Johnson, Norman L. Kemp, Adrianne W. Kotz, Samuel (2005). Univariate Discrete Distributions (third edition). Hoboken, NJ: Wiley-Interscience.

[https://en.wikipedia.org/wiki/Wigner\\_semicircle\\_distribution](https://en.wikipedia.org/wiki/Wigner_semicircle_distribution)

**See Also**

[zip.mle](#), [gammamle](#), [vm.mle](#)

**Examples**

```
x <- rt(1000,10)
a <- ct.mle(x)
res<-tmle(x, v = a$nu)
res<-cauchy.mle(x)
res<-normal.mle(x)
res<-logistic.mle(x)
res<-gumbel.mle(x)
```

---

MLE of count data (univariate discrete distributions)

*MLE of count data*

---

**Description**

MLE of count data.

**Usage**

```

zip.mle(x, tol = 1e-09)
ztp.mle(x, tol = 1e-09)
negbin.mle(x, type = 1, tol = 1e-09)
binom.mle(x, N = NULL, tol = 1e-07)
borel.mle(x)
geom.mle(x, type = 1)
logseries.mle(x, tol = 1e-09)
poisson.mle(x)
betageom.mle(x, tol = 1e-07)
betabinom.mle(x, N, tol = 1e-07)

```

**Arguments**

x	A vector with discrete valued data.
type	This argument is for the negative binomial and the geometric distribution. In the negative binomial you can choose which way your prefer. Type 1 is for small sample sizes, whereas type 2 is for larger ones as is faster. For the geometric it is related to its two forms. Type 1 refers to the case where the minimum is zero and type 2 for the case of the minimum being 1.
N	This is for the binomial distribution only, specifying the total number of successes. If NULL, it is sestimated by the data. It can also be a vector of successes.
tol	The tolerance level up to which the maximisation stops set to 1e-09 by default.

**Details**

Instead of maximising the log-likelihood via a numerical optimiser we used a Newton-Raphson algorithm which is faster.

See wikipedia for the equation to be solved in the case of the zero inflated distribution. [https://en.wikipedia.org/wiki/Zero-inflated\\_model](https://en.wikipedia.org/wiki/Zero-inflated_model). In order to avoid negative values we have used link functions, log for the  $\lambda$  and logit for the  $\pi$  as suggested by Lambert (1992). As for the zero truncated Poisson see [https://en.wikipedia.org/wiki/Zero-truncated\\_Poisson\\_distribution](https://en.wikipedia.org/wiki/Zero-truncated_Poisson_distribution).

zip.mle is for the zero inflated Poisson, whereas ztp.mle is for the zero truncated Poisson distribution.

**Value**

The following list is not inclusive of all cases. Different functions have different names. In general a list including:

mess	This is for the negbin.mle only. If there is no reason to use the negative binomial distribution a message will appear, otherwise this is NULL.
iters	The number of iterations required for the Newton-Raphson to converge.
loglik	The value of the maximised log-likelihood.
prob	The probability parameter of the distribution. In some distributions this argument might have a different name. For example, param in the zero inflated Poisson.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Lambert Diane (1992). Zero-Inflated Poisson Regression, with an Application to Defects in Manufacturing. *Technometrics*. 34 (1): 1-14

Johnson Norman L., Kotz Samuel and Kemp Adrienne W. (1992). *Univariate Discrete Distributions* (2nd ed.). Wiley

**See Also**

[poisson\\_only](#), [colrange](#)

**Examples**

```
x <- rpois(100, 2)
res<-zip.mle(x)
res<-poisson.mle(x)
## small difference in the two log-likelihoods as expected.
```

```
x <- rpois(100, 10)
x[x == 0 ] <- 1
res<-ztp.mle(x)
res<-poisson.mle(x)
## significant difference in the two log-likelihoods.
```

```
x <- rnbinom(100, 10, 0.6)
res<-poisson.mle(x)
res<-negbin.mle(x)
```

---

MLE of distributions defined in the (0, 1) interval

*MLE of distributions defined in the (0, 1) interval*

---

**Description**

MLE of distributions defined in the (0, 1) interval.

**Usage**

```
beta.mle(x, tol = 1e-09)
ibeta.mle(x, tol = 1e-09)
logitnorm.mle(x)
hsecant01.mle(x, tol = 1e-09)
```

**Arguments**

x	A numerical vector with proportions, i.e. numbers in (0, 1) (zeros and ones are not allowed).
tol	The tolerance level up to which the maximisation stops.

**Details**

Maximum likelihood estimation of the parameters of the beta distribution is performed via Newton-Raphson. The distributions and hence the functions does not accept zeros. "logitnorm.mle" fits the logistic normal, hence no newton-Raphson is required and the "hypersecant01.mle" uses the golden ratio search as is it faster than the Newton-Raphson (less calculations)

**Value**

A list including:

iters	The number of iterations required by the Newton-Raphson.
loglik	The value of the log-likelihood.
param	The estimated parameters. In the case of "hypersecant01.mle" this is called "theta" as there is only one parameter.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

**See Also**

[diri.nr2](#),

**Examples**

```
x <- rbeta(100, 1, 4)
res<-beta.mle(x)
res<-hsecant01.mle(x)
res<-logitnorm.mle(x)

x[sample(1:100, 5)] <- 0
res<-ibeta.mle(x)
```

---

MLE of some circular distributions

*MLE of some circular distributions*

---

### Description

MLE of some circular distributions.

### Usage

```
vm.mle(x, tol = 1e-09)
spml.mle(x, tol = 1e-09, maxiters = 100)
wrapcauchy.mle(x, tol = 1e-09)
```

### Arguments

<code>x</code>	A numerical vector with the circular data. They must be expressed in radians. For the "spml.mle" this can also be a matrix with two columns, the cosinus and the sinus of the circular data.
<code>tol</code>	The tolerance level to stop the iterative process of finding the MLEs.
<code>maxiters</code>	The maximum number of iterations to implement.

### Details

The parameters of the von Mises, the bivariate angular Gaussian and wrapped Cauchy distributions are estimated. For the Wrapped Cauchy, the iterative procedure described by Kent and Tyler (1988) is used. As for the von Mises distribution, we use a Newton-Raphson to estimate the concentration parameter. The angular Gaussian is described, in the regression setting in Presnell et al. (1998).

### Value

A list including:

<code>iters</code>	The iterations required until convergence. This is returned in the wrapped Cauchy distribution only.
<code>loglik</code>	The value of the maximised log-likelihood.
<code>param</code>	A vector consisting of the estimates of the two parameters, the mean direction for both distributions and the concentration parameter kappa and the rho for the von Mises and wrapped Cauchy respectively.
<code>gamma</code>	The norm of the mean vector of the angular Gaussian distribution.
<code>mu</code>	The mean vector of the angular Gaussian distribution.

### Author(s)

Michail Tsagris and Stefanos Fafalios

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Stefanos Fafalios <stefanosfafalios@gmail.com>

## References

- Mardia K. V. and Jupp P. E. (2000). Directional statistics. Chichester: John Wiley & Sons.
- Sra S. (2012). A short note on parameter approximation for von Mises-Fisher distributions: and a fast implementation of  $Is(x)$ . Computational Statistics, 27(1): 177-190.
- Presnell Brett, Morrison Scott P. and Littell Ramon C. (1998). Projected multivariate linear models for directional data. Journal of the American Statistical Association, 93(443): 1068-1077.
- Kent J. and Tyler D. (1988). Maximum likelihood estimation for the wrapped Cauchy distribution. Journal of Applied Statistics, 15(2): 247–254.

## See Also

[vmf.mle](#), [rvonmises](#), [rvmf](#)

## Examples

```
y <- rcauchy(100, 3, 1)
x <- y
res<-vm.mle(x)
res<-spml.mle(x)
res<-wrapcauchy.mle(x)
x <- NULL
```

---

MLE of the inverted Dirichlet distribution  
*MLE of the inverted Dirichlet distribution*

---

## Description

MLE of the inverted Dirichlet distribution.

## Usage

```
invdir.mle(x, tol = 1e-07)
```

## Arguments

x	A matrix with strictly positive data (no zeros are allowed).
tol	The tolerance level up to which the maximisation stops.

## Details

Maximum likelihood estimation of the parameters of the inverted is performed via Newton-Raphson. We took the initial values suggested by Bdiri T. and Bouguila N. (2012) and modified them a bit.

**Value**

A list including:

<code>iters</code>	The number of iterations required by the Newton Raphson.
<code>loglik</code>	The value of the log-likelihood.
<code>param</code>	The estimated parameters.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

**References**

Bdiri T. and Bouguila N. (2012). Positive vectors clustering using inverted Dirichlet finite mixture models. *Expert Systems with Applications*, 39(2): 1869-1882.

**See Also**

[diri.nr2](#), [multinom.mle](#)

**Examples**

```
x <- as.matrix(iris[, 1:4])
for(i in 1:10) invdir.mle(x)
res<-invdir.mle(x)
```

---

MLE of the multivariate (log-) normal distribution

*MLE of the multivariate (log-) normal distribution*

---

**Description**

MLE of the multivariate (log-) normal distribution.

**Usage**

```
mvnorm.mle(x)
mvlnorm.mle(x)
```

**Arguments**

`x` A matrix with numerical data.

**Details**

The mean vector, covariance matrix and the value of the log-likelihood of the multivariate normal or log-normal distribution is calculated. For the log-normal distribution we also provide the expected value and the covariance matrix.

**Value**

A list including:

<code>loglik</code>	The log-likelihood multivariate distribution.
<code>mu</code>	The mean vector.
<code>sigma</code>	The covariance matrix.
<code>m</code>	The expected mean vector of the multivariate log-normal distribution.
<code>s</code>	The expected covariance matrix of the multivariate log-normal distribution.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Kotz, S., Balakrishnan, N., & Johnson, N. L. (2004). Continuous multivariate distributions, Volume 1: Models and applications (Vol. 1). John Wiley & Sons.

<http://isi.cbs.nl/iamamember/CD2/pdf/329.PDF>

[https://en.wikipedia.org/wiki/Log-normal\\_distribution#Multivariate\\_log-normal](https://en.wikipedia.org/wiki/Log-normal_distribution#Multivariate_log-normal)

**See Also**

[multinom.mle](#), [dmvnorm](#), [gaussian.nb](#)

**Examples**

```
x <- matrnorm(100, 4)
res<-mvnorm.mle(x)
x <- NULL
```

MLE of the multivariate  $t$  distribution

*MLE of the multivariate  $t$  distribution*

---

### Description

MLE of the multivariate  $t$  distribution.

### Usage

```
mvt.mle(x, v = 5, tol = 1e-07)
```

### Arguments

<code>x</code>	A matrix with numerical data.
<code>v</code>	The degrees of freedom. Must be a positive number, greater than zero.
<code>tol</code>	The tolerance value to terminate the EM algorithm.

### Details

The location vector, scatter matrix and the value of the log-likelihood is calculated.

### Value

A list including:

<code>iters</code>	The number of iterations required for the EM algorithm to converge.
<code>loglik</code>	The value of the maximised log-likelihood.
<code>location</code>	The location vector.
<code>scatter</code>	The scatter matrix.

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

### References

Nadarajah S. and Kotz S. (2008). Estimation methods for the multivariate  $t$  distribution. *Acta Applicandae Mathematicae*, 102(1):99-118.

### See Also

[mvnorm.mle](#), [dmvnorm](#), [gaussian.nb](#)

**Examples**

```
x <- matnorm(100, 4)
#res<-mvnorm.mle(x)
#res<-mvt.mle(x, v = 5)
#res<-mvt.mle(x, v = 100)
```

---

MLE of the ordinal model without covariates

*MLE of the ordinal model without covariates*

---

**Description**

MLE of the ordinal model without covariates.

**Usage**

```
ordinal.mle(y, link = "logit")
```

**Arguments**

y	A numerical vector with values 1, 2, 3,..., not zeros, or an ordered factor.
link	This can either be "logit" or "probit". It is the link function to be used.

**Details**

Maximum likelihood of the ordinal model (proportional odds) is implemented. See for example the "polr" command in R or the examples.

**Value**

A list including:

loglik	The log-likelihood of the model.
a	The intercepts (threshold coefficients) of the model.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**References**

Agresti, A. (2002) Categorical Data. Second edition. Wiley.

**See Also**

[beta.mle](#), [diri.nr2](#)

**Examples**

```
y <- factor( rbinom(100,3,0.5), ordered = TRUE )
res<-ordinal.mle(y)
res<-ordinal.mle(y, link = "probit")
```

---

MLE of the tobit model

*MLE of the tobit model*

---

**Description**

MLE of the tobit model.

**Usage**

```
tobit.mle(y, tol = 1e-09)
```

**Arguments**

y	A vector with positive valued data and zero values. If there are no zero values, a simple normal model is fitted in the end.
tol	The tolerance level up to which the maximisation stops; set to 1e-09 by default.

**Details**

The tobit model is useful for (univariate) positive data with left censoring at zero. There is the assumption of a latent variable. The values of that variable which are positive coincide with the observed values. If some values are negative, they are left censored and the observed values are zero. Instead of maximising the log-likelihood via a numerical optimiser we have used a Newton-Raphson algorithm which is faster.

**Value**

A list with three elements including

iters	The number of iterations required for the Newton-Raphson to converge.
loglik	The value of the maximised log-likelihood.
param	The vector of the parameters.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

## References

Tobin James (1958). Estimation of relationships for limited dependent variables. *Econometrica*. 26(1):24–36.

[https://en.wikipedia.org/wiki/Tobit\\_model](https://en.wikipedia.org/wiki/Tobit_model)

## See Also

[gammamle](#), [normal.mle](#)

## Examples

```
x <- rnorm(300, 3, 5)
x[ x < 0 ] <- 0 ## left censoring. Values below zero become zero
for (i in 1:50) tobit.mle(x)
```

---

Moment and maximum likelihood estimation of variance components

*Moment and maximum likelihood estimation of variance components*

---

## Description

Moment and maximum likelihood estimation of variance components.

## Usage

```
rint.mle(x, ina, ranef = FALSE, tol = 1e-09, maxiters = 100)
varcomps.mom(x, ina)
varcomps.mle(x, ina, tol = 1e-09)
```

## Arguments

<code>x</code>	A numerical vector with the data.
<code>ranef</code>	Should the random effects be returned as well? The default value is FALSE.
<code>ina</code>	A numerical vector with 1s, 2s, 3s and so one indicating the two groups. Be careful, the function is designed to accept numbers greater than zero. Alternatively it can be a factor variable.
<code>tol</code>	The tolerance level to terminate the golden ratio search. the default value is $10^{-9}$ .
<code>maxiters</code>	The maximum number of iterations Newton-Raphson will implement.

### Details

Note that the "varcomps.mle" and "varcomp.mom" work for **balanced designs only**, i.e. for each subject the same number of measurements have been taken. The "rint.mle" works for both the balanced and unbalanced designs.

The variance components, the variance of the between measurements and the variance of the within are estimated using moment estimators. The "colvarcomsp.mom" is the moment analogue of a random effects model which uses likelihood estimation ("colvarcomps.mle"). It is much faster, but can give negative variance of the random effects, in which case it becomes zero.

The maximum likelihood version is a bit slower (try yourselves to see the difference), but statistically speaking is to be preferred when small samples are available. The reason why it is only a little bit slower and not a lot slower as one would imagine is because we are using a closed formula to calculate the two variance components (Demidenko, 2013, pg. 67-69). Yes, there are closed formulas for linear mixed models.

### Value

For the "varcomps.mom": A vector with 5 elements, The MSE, the estimate of the between variance, the variance components ratio and a 95% confidence for the ratio.

For the "varcomps.mle": a list with a single component called "info". That is a matrix with 3 columns, The MSE, the estimate of the between variance and the log-likelihood value. **If ranef = TRUE** a list including "info" and an extra component called "ranef" containing the random effects. It is a matrix with the same number of columns as the data. Each column contains the random effects of each variable.

### Author(s)

Michail Tsagris and Manos Papadakis.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

### References

Montgomery D.C. (2001). Design and analysis of experiments (5th Edition). New York: John Wiley & Sons.

Davis C.S. (2002). Statistical methods for the analysis of repeated measures. New York: Springer-Verlag.

Demidenko E. (2013). Mixed Models: Theory and Applications with R 2nd Edition). New Jersey: John Wiley & Sons (Excellent book).

### See Also

[colvarcomps.mle](#), [rint.reg](#), [rint.regbx](#)

**Examples**

```
## example from Montgomery, pages 514-517
x <- c(98,97,99,96,91,90,93,92,96,95,97,95,95,96,99,98)
ina <- rep(1:4, each = 4)
res<-varcomps.mom(x, ina)
res<-varcomps.mle(x, ina)
```

---

Multi-sample tests for vectors

*Multi-sample tests for vectors*

---

**Description**

Multi-sample tests for vectors.

**Usage**

```
ftest(x, ina, logged = FALSE)
anova1(x, ina, logged = FALSE)
kruskaltest(x, ina, logged = FALSE)
var2test(x, y, alternative = "unequal", logged = FALSE)
mcnemar(x, y, logged = FALSE)
tttest2(x, y, alternative = "unequal", paired = FALSE, logged = FALSE)
cqtest(x, treat, block, logged = FALSE)
block.anova(x, treat, block, logged = FALSE)
twoway.anova(y, x1, x2, interact = FALSE, logged = FALSE)
```

**Arguments**

x	A numerical vector with the data.
y	A numerical vector with the data.
ina	A numerical vector with 1s, 2s, 3s and so on indicating the two groups. Be careful, the function is designed to accept numbers greater than zero. Alternatively it can be a factor variable.
paired	This is for the two sample t-test only and is TRUE or FALSE specifying whether the two samples are paired or not.
alternative	This can either be "unequal", "greater" or "less".
treat	In the case of the blocking ANOVA and Cochran's Q test, this argument plays the role of the "ina" argument.
block	This item (in the blocking ANOVA and Cochran's Q test) denotes the subjects which are the same. Similarly to "ina" a numeric vector with 1s, 2s, 3s and so on.
x1	The first factor in the two way ANOVA.
x2	The second factor in the two way ANOVA. The order is not important.
interact	Should interaction in the two way ANOVA be included? The default value is FALSE (no interaction).
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

## Details

The Welch's F-test (without assuming equal variances) is performed with the "ftest" function. The "anova" function perform the classical (Fisher's) one-way analysis of variance (ANOVA) which assumes equal variance across the groups. The "kruskaltest" performs the Kruskal-Wallis non parametric alternative to analysis of variance test. The "var2tests" implement the classical F test for the equality of two sample variances. The "cqtest" performs the Cochran's Q test for the equality of more than two groups whose values are strictly binary (0 or 1). This is a generalisation of the McNemar's test in the multi-sample case. The "block.anova" is the ANOVA with blocking, randomised complete block design (RCBD). In this case, for every combination of the block and treatment values, there is only one observation. The mathematics are the same as in the case of "twoway.anova", but the assumptions different and the testing procedure also different. In addition, no interaction is present.

## Value

A vector with the test statistic and the p-value of each test. For the case of t-test, an extra column with the degrees of freedom is given. For the two way ANOVA there can be either 2 or three F test statistics and hence the same number of p-values.

## Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

## References

B.L. Welch (1951). On the comparison of several mean values: an alternative approach. *Biometrika*, 38(3/4), 330-336.

D.C. Montgomery (2001). *Design and analysis of experiments* (5th Edition). New York: John Wiley & Sons.

McNemar Q. (1947). Note on the sampling error of the difference between correlated proportions or percentages. *Psychometrika*. 12(2):153-157.

## See Also

[ttests](#), [ftests](#)

## Examples

```
x <- rnorm(200)
ina <- rbinom(200, 3, 0.5) + 1
res<-anova1(x, ina)
res<-ftest(x, ina)
ina <- rbinom(200, 1, 0.5) + 1
x1 <- x[ ina == 1 ] ; x2 <- x[ ina == 2 ]
res<-ttest2(x1, x2)
res<-var2test(x1, x2)
```

```
## RCBD example 4.1 from Montgomery (2001), page 131-132
x <- c(9.3, 9.4, 9.2, 9.7, 9.4, 9.3, 9.4, 9.6, 9.6, 9.8, 9.5, 10,
10, 9.9, 9.7, 10.2)
tr <- rep(1:4, 4)
bl <- rep(1:4, each = 4)
res<-block.anova(x, tr, bl)
```

---

Multinomial regression

*Multinomial regression*

---

### Description

Multinomial regression.

### Usage

```
multinom.reg(y, x, tol = 1e-07, maxiters = 50)
```

### Arguments

y	The response variable. A numerical or a factor type vector.
x	A matrix or a data.frame with the predictor variables.
tol	This tolerance value to terminate the Newton-Raphson algorithm.
maxiters	The maximum number of iterations Newton-Raphson will perform.

### Value

A list including:

iters	The number of iterations required by the Newton-Raphson.
loglik	The value of the maximised log-likelihood.
be	A matrix with the estimated regression coefficients.

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

### References

Bohning, D. (1992). Multinomial logistic regression algorithm. *Annals of the Institute of Statistical Mathematics*, 44(1): 197-200.

### See Also

[glm\\_logistic](#), [score.multinomregs](#) [logistic\\_only](#)

**Examples**

```
y <- iris[, 5]
x <- matnorm(150, 3)
res <- multinom.reg(y, x)
```

---

Multivariate kurtosis *Multivariate kurtosis*

---

**Description**

Multivariate kurtosis.

**Usage**

```
mvkurtosis(x)
```

**Arguments**

x                    A numerical matrix.

**Details**

The multivariate kurtosis is calculated.

**Value**

A number, the multivariate kurtosis.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

K. V. Mardia (1970). Measures of Multivariate Skewness and Kurtosis with Applications *Biometrika*, 57(3):519-530.

**See Also**

[colskewness](#), [skew.test2](#), [colmeans](#), [colVars](#), [colMedians](#)

**Examples**

```
x <- as.matrix(iris[, 1:4])
#res<-mvkurtosis(x)
```

---

Multivariate Laplace random values simulation

*Multivariate Laplace random values simulation*

---

## Description

Multivariate Laplace random values simulation.

## Usage

```
rmvlaplace(n, lam, mu, G, seed = NULL)
```

## Arguments

n	The sample size, a numerical value.
lam	The the parameter of the exponential distribution, a positive number.
mu	The mean vector.
G	A $d \times d$ covariance matrix with determinant 1.
seed	If you want the same to be generated again use a seed for the generator, an integer number.

## Details

The algorithm uses univariate normal random values and transforms them to multivariate via a spectral decomposition.

## Value

A matrix with the simulated data.

## Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

## References

Eltoft T., Kim T., and Lee T.W. (2006). On the multivariate laplace distribution. Signal Processing Letters, IEEE, 13(5):300-303.

## See Also

[rmvnorm](#), [racg](#), [rmvt](#)

**Examples**

```
m <- colmeans( as.matrix( iris[, 1:4] ) )
s <- cov(iris[,1:4])
s <- s / det(s)^0.25
lam <- 3
x <- rmvlaplace(100, lam, m, s)
```

---

Multivariate normal and t random values simulation

*Multivariate normal and t random values simulation*

---

**Description**

Multivariate normal and t random values simulation.

**Usage**

```
rmvnorm(n, mu, sigma, seed = NULL)
rmvt(n, mu, sigma, v, seed = NULL)
```

**Arguments**

n	The sample size, a numerical value.
mu	The mean vector in $R^d$ .
sigma	The covariance matrix in $R^d$ .
v	The degrees of freedom.
seed	If you want the same to be generated again use a seed for the generator, an integer number.

**Details**

The algorithm uses univariate normal random values and transforms them to multivariate via a spectral decomposition. It is faster than the command "rmvnorm" available from MASS, and it allows for singular covariance matrices.

**Value**

A matrix with the simulated data.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

**See Also**

[racg](#), [rmvlaplace](#), [rmvt](#)

**Examples**

```
x <- as.matrix(iris[, 1:4])
m <- colmeans(x)
s <- cov(x)
y <- rmvnorm(1000, m, s)
res<-colmeans(y)
res<-cov(y)
y <- NULL
```

---

Naive Bayes classifiers

*Naive Bayes classifiers*

---

**Description**

Gaussian, Poisson, geometric and multinomial naive Bayes classifiers.

**Usage**

```
gaussian.nb(xnew = NULL, x, ina, parallel = FALSE)
poisson.nb(xnew, x, ina)
multinom.nb(xnew, x, ina)
geom.nb(xnew, x, ina, type = 1)
gammanb(xnew = NULL, x, ina, tol = 1e-07)
```

**Arguments**

<code>xnew</code>	A numerical matrix with new predictor variables whose group is to be predicted. For the Gaussian naive Bayes, this is set to NUUL, as you might want just the model and not to predict the membership of new observations. For the Gaussian case this contains any numbers, but for the multinomial and Poisson cases, the matrix must contain integer valued numbers only.
<code>x</code>	A numerical matrix with the observed predictor variable values. For the Gaussian case this contains any numbers, but for the multinomial and Poisson cases, the matrix must contain integer valued numbers only.
<code>ina</code>	A numerical vector with strictly positive numbers, i.e. 1,2,3 indicating the groups of the dataset. Alternatively this can be a factor variable.
<code>type</code>	Type 1 refers to the case where the minimum is zero and type 2 for the case of the minimum being 1. This is for the geometric distribution. This argument is for the geometric distribution. Type 1 refers to the case where the minimum is zero and type 2 for the case of the minimum being 1.
<code>tol</code>	The tolerance value to terminate the Newton-Raphson algorithm in the gamma distribution.
<code>parallel</code>	If you want parallel computations set this equal to TRUE.

**Value**

For the Poisson and Multinomial naive Bayes classifiers the estimated group, a numerical vector with 1, 2, 3 and so on. For the Gaussian naive Bayes classifier a list including:

<code>mu</code>	A matrix with the mean vector of each group based on the dataset.
<code>sigma</code>	A matrix with the variance of each group and variable based on the dataset.
<code>ni</code>	The sample size of each group in the dataset.
<code>est</code>	The estimated group of the <code>xnew</code> observations. It returns a numerical value back regardless of the target variable being numerical as well or factor. Hence, it is suggested that you do <code>"as.numeric(target)"</code> in order to see what is the predicted class of the new data.

For the Gamma classifier a list including:

<code>a</code>	A matrix with the shape parameters.
<code>b</code>	A matrix with the scale parameters.
<code>est</code>	The estimated group of the <code>xnew</code> observations. It returns a numerical value back regardless of the target variable being numerical as well or factor. Hence, it is suggested that you do <code>"as.numeric(target)"</code> in order to see what is the predicted class of the new data.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[gaussiannb.pred](#), [colmeans](#), [colVars](#)

**Examples**

```
x <- as.matrix(iris[, 1:4])
a <- gaussian.nb(x, x, iris[, 5])
x1 <- matrix( rpois(100 * 4, 5), ncol = 4)
x2 <- matrix( rpois(50 * 4, 10), ncol = 4)
x <- rbind(x1, x2)
ina <- c( rep(1, 100), rep(2, 50) )
res<-poisson.nb(x, x, ina)
res<-geom.nb(x, x, ina)
res<-multinom.nb(x, x, ina)
```

---

Natural Logarithm each element of a matrix  
*Natural Logarithm each element of a matrix*

---

**Description**

Natural Logarithm each element of a matrix.

**Usage**

```
Log(x, na.rm = FALSE)
```

**Arguments**

x	A matrix with data.
na.rm	A boolean value (TRUE/FALSE) for removing NA.

**Details**

The argument must be a matrix. For vector the time was the same as R's "log" function so we did not add it.

**Value**

A matrix where each element is the natural logarithm of the given argument.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Lbeta](#), [Lchoose](#), [Choose](#)

**Examples**

```
x <-matrix( runif( 100 * 100), ncol = 100 )
a <- log(x)
b <- Log(x)
all.equal(a, b) # true

x<-a<-b<-NULL
```

---

Natural logarithm of the beta function

*Natural logarithm of the beta function*

---

**Description**

Natural logarithm of the beta function.

**Usage**

Lbeta(x, y)

**Arguments**

x	A numerical matrix, or a vector or just a number with positive numbers in either case.
y	A numerical matrix, or a vector or just a number with positive numbers in either case. The dimensions of y must match those of x.

**Details**

The function is faster than R's lbeta when the dimensions of x any are large. If you have only two numbers, then lbeta is faster. But if you have for example two vectors of 1000 values each, Lbeta becomes two times faster than lbeta.

**Value**

The matrix, vector or number with the resulting values.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**References**

Abramowitz, M. and Stegun, I. A. (1972) Handbook of Mathematical Functions. New York: Dover. [https://en.wikipedia.org/wiki/Abramowitz\\_and\\_Stegun](https://en.wikipedia.org/wiki/Abramowitz_and_Stegun) provides links to the full text which is in public domain. Chapter 6: Gamma and Related Functions.

**See Also**

[Lgamma](#), [beta.mle](#), [diri.nr2](#)

**Examples**

```
x <- rexp(1000)
y <- rexp(1000)
a1 <- Lbeta(x, y)

x<-y<-a1<-NULL
```

---

Natural logarithm of the gamma function and its derivatives

*Natural logarithm of the gamma function and its derivatives*

---

**Description**

Natural logarithm of the gamma function and its derivatives.

**Usage**

```
Lgamma(x)
Digamma(x)
Trigamma(x)
```

**Arguments**

x                    A numerical matrix or vector with positive numbers in either case.

**Details**

We have spotted that the time savings come when there are more than 50 elements, with vector or matrix.

**Value**

The matrix or the vector with the resulting values.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**References**

Abramowitz, M. and Stegun, I. A. (1972) Handbook of Mathematical Functions. New York: Dover. [https://en.wikipedia.org/wiki/Abramowitz\\_and\\_Stegun](https://en.wikipedia.org/wiki/Abramowitz_and_Stegun) provides links to the full text which is in public domain. Chapter 6: Gamma and Related Functions.

**See Also**

[beta.mle](#), [diri.nr2](#)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100 )
a1 <- Lgamma(x)
a2 <- lgamma(x)
all.equal(as.vector(a1), as.vector(a2))

a1 <- Digamma(x)
a2 <- digamma(x)
all.equal(as.vector(a1), as.vector(a2))

x<-a1<-a2<-NULL
```

---

Norm of a matrix	<i>Norm of a matrix</i>
------------------	-------------------------

---

**Description**

Norm of a matrix.

**Usage**

```
Norm(x, type = "F")
```

**Arguments**

x	A matrix with numbers.
type	The type of norm to be calculated. The default is "F" standing for Frobenius norm ("f" in R's norm). The other options are "C" standing for the one norm ("o" in R's norm), "R" for the identity norm ("I" in R's norm) and "M" for the maximum modulus among elements of a matrix ("M" in R's norm)

**Value**

A number, the norm of the matrix.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Dist](#), [dista](#), [colmeans](#)

**Examples**

```
x <- matrix( rnorm(10 * 10), ncol = 10 )
res<-Norm(x, "F")
res<-norm(x, "F")
res<-Norm(x, "M")
res<-norm(x, "M")
```

---

Number of equal columns between two matrices

*Number of equal columns between two matrices*

---

**Description**

Number of equal columns between two matrices.

**Usage**

```
mat.mat(x, y)
```

**Arguments**

x	A numerical matrix. See details for more information. It must have the same number of rows as y.
y	A numerical matrix. See details for more information. It must have the same number of rows as x.

**Details**

The function takes each column of x and checks the number of times it matches a column of y. In the example below, we take the first 3 columns of iris as the x matrix. The y matrix is the whole of iris. We will see how many times, each column of x appears in the y matrix. The answer is 1 for each column.

**Value**

A numerical vector of size equal to the number of columns of x.

**Author(s)**

Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Match](#), [colmeans](#), [colMedians](#)

**Examples**

```
x <- as.matrix(iris[, 1:3])
y <- iris
y[, 5] <- as.numeric(y[, 5])
y <- as.matrix(y)
res<-mat.mat(x, y)

x<-y<-NULL
```

---

Odds ratio and relative risk

*Odds ratio and relative risk*

---

**Description**

Odds ratio and relative risk.

**Usage**

```
odds.ratio(x, a = 0.05, logged = FALSE)
rel.risk(x, a = 0.05, logged = FALSE)
```

**Arguments**

x	A 2 x 2 matrix or a vector with 4 elements. In the case of the vector make sure it corresponds to the correct table.
a	The significance level, set to 0.05 by default.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

The odds ratio and the confidence interval are calculated.

**Value**

A list including:

res	The estimated odds ratio and the p-value for the null hypothesis test that it is equal to 1.
ci	The (1-a)% confidence interval for the true value of the odds ratio.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

Mosteller Frederick (1968). Association and Estimation in Contingency Tables. Journal of the American Statistical Association. 63(321):1-28.

Edwards A.W.F. (1963). The measure of association in a 2x2 table. Journal of the Royal Statistical Society, Series A. 126(1):109-114.

**See Also**

[odds](#), [g2Test](#)

**Examples**

```
x <- rpois(4, 30)+2
res<-odds.ratio(x)
res<-odds.ratio( matrix(x, ncol = 2) )
```

---

One and many Gini coefficients

*One and many Gini coefficients*

---

**Description**

Many Gini coefficients.

**Usage**

```
gini(x)
ginis(x)
```

**Arguments**

`x` Either a vector or a matrix with non negative data. The rows are observations and the columns denote the variables.

**Details**

We have implemented the fast version of the Gini coefficient. See [wikipedia](#) for more details.

**Value**

A value with the Gini coefficient or a vector with the Gini coefficient, one for each variable.

**Author(s)**

Michail Tsagris.

R implementation and documentation: Michail Tsagris <[mtsagris@uoc.gr](mailto:mtsagris@uoc.gr)> and Manos Papadakis <[papadakm95@gmail.com](mailto:papadakm95@gmail.com)>.

**See Also**

[colskewness](#), [colmeans](#), [corpairs](#)

**Examples**

```
x <- matrix( rpois(300 * 100, 100), ncol = 100 )
a <- gini(x)
```

---

One sample t-test for a vector

*One sample t-test for a vector*

---

**Description**

One sample t-test for a vector.

**Usage**

```
ttest1(x, m, alternative = "unequal", logged = FALSE, conf = NULL)
```

**Arguments**

x	A numerical vector with the data.
m	The mean value under the null hypothesis.
alternative	The alternative hypothesis, "unequal", "greater" or "less".
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?
conf	If you want a confidence interval supply the confidence level.

**Details**

The usual one sample t-test is implemented, only faster.

**Value**

A list including:

res	A two valued vector with the test statistic and its (logged) p-value.
ci	In the case you supplied a number in the input argument "conf" the relevant confidence interval will be returned as well.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**See Also**

[ttest](#), [anova1](#), [ttests](#)

**Examples**

```
x = rnorm(500)
res<-t.test(x, mu = 0)
res<-ttest1(x, 0, conf = 0.95)
```

---

Operations between two matrices or matrix and vector

*Operations between two matrices or matrix and vector*

---

**Description**

Operations between two matrices or matrix and vector.

**Usage**

```
XopY.sum(x, y = NULL, oper = "*")
eachrow(x,y,oper = "*",method = NULL)
eachcol.apply(x,y,indices = NULL,oper = "*",apply = "sum", parallel = FALSE)
```

**Arguments**

x	A numerical matrix.
y	A second numerical matrix for "XopY.sum" whose dimensions must match the ones of x, or vector for "eachrow","eachcol.apply" whose length must match with the rows of x.
oper	The operation to be performed, either "*", "/", "+", "-" or "==".
method	A character value for choosing option to apply in the result. Options: 1) sum 2) max 3) min Does not work for oper=="=".
indices	An integer vector with indices to specific columns. Only for "eachcol.apply".
apply	A character value with the function to be applied in the columns of the matrix. Only for "eachcol.apply". Options: 1) sum 2) median 3) max 4) min
parallel	A boolean value for parallel version.

**Details**

XopY.sum: sum(X op Y) where op can be on of "+,-,\*,/".

eachrow: X op Y **by row** or **FUNCTION**(X op Y) where "x" is matrix, "y" is vector with length as much as the columns of x and "op" is one of "+,-,\*,/,"=="", and "FUNCTION" is a specific method for applying in the result matrix (see argument method).

eachcol.apply: **FUNCTION**(X op Y) **by column** where "x" is matrix, "y" is vector with length as much as the rows of x, "op" is one of "+,-,\*,/" and "FUNCTION" is a specific method (see argument apply).

**NOTE:** Arguments "method" does not work for oper="==" and this operation works only in "eachrow".

### Value

XopY.sum: sum(X op Y) where "op" can be on of "+,-,\*,/".

eachrow: operation by row between a matrix and a vector."op" can be on of "+,-,\*,/". If "suma=TRUE" then returns the sum of this operation.

eachcol.apply: operation by column between a matrix and a vector and applied a specific function."op" can be on of "+,-,\*,/".

### Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

### See Also

[Dist](#), [dista](#), [colmeans](#), [Diag.fill](#), [colMads](#), [rowMads](#)

### Examples

```
x <- matrix( rnorm(5 * 5), ncol = 5 )
y <- matrix( rnorm(5 * 5), ncol = 5 )
res<-XopY.sum(x, y, oper = "*" )
y <- x[,1]
res<-eachrow(x,y)

all.equal(eachcol.apply(x,y),colsums(x*y))

x<-y<-NULL
```

---

Orthogonal matching pursuit variable selection

*Orthogonal matching pursuit variable selection*

---

### Description

Orthogonal matching pursuit variable selection.

### Usage

```
ompr(y, x, ystand = TRUE, xstand = TRUE, method = "BIC", tol = 2 )
omp(y, x, xstand = TRUE, tol = qchisq(0.95, 1) + log( length(y) ), type = "logistic" )
```

**Arguments**

y	The response variable, a numeric vector. For "ompr" this is a continuous variable. For "omp" this can be either a vector with discrete (count) data, 0 and 1, non negative values, strictly positive or proportions including 0 and 1.
x	A matrix with the data, where the rows denote the observations and the columns are the variables.
ystand	If this is TRUE the response variable is centered. The mean is subtracted from every value.
xstand	If this is TRUE the independent variables are standardised.
method	You can choose between the change in the BIC ("BIC"), the adjusted $R^2$ ("ar2"), the SSE ("SSE") or the classical p-value based ("pvalue").
tol	The tolerance value to terminate the algorithm. This is the change in the criterion value between two successive steps. For "ompr" the default value is 2 because the default method is "BIC". For "omp" the default value is the 95% quantile of the $\chi^2$ distribution with 1 degree of freedom plus the logarithm of the sample size.
type	This denotes the parametric model to be used each time. It depends upon the nature of y. The possible values are "logistic", "poisson", "quasipoisson", "quasibinomial", "normlog", "gamma", "weibull", "mv" (for multivariate response variable) or "multinomial".

**Value**

For "ompr" a list including:

runtime	The runtime of the algorithm.
info	A matrix with two columns. The selected variable(s) and the criterion value at every step.

For "omp" a list including:

runtime	The runtime of the algorithm.
phi	The $\phi$ parameter. In the cases of "quasipoisson", "quasibinomial" and "normlog" this is useful. For all other cases this is NULL.
info	A matrix with two columns. The selected variable(s) and the criterion value at every step.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

Pati Y. C., Rezaifar R. & Krishnaprasad P. S. (1993). Orthogonal matching pursuit: Recursive function approximation with applications to wavelet decomposition. In Signals, Systems and Computers. 1993 Conference Record of The Twenty-Seventh Asilomar Conference on. IEEE.

Mazin Abdulrasool Hameed (2012). Comparative analysis of orthogonal matching pursuit and least angle regression. MSc thesis, Michigan State University. <https://www.google.gr/url?sa=t&rct=j&q=&esrc=s&source=web&>

Lozano A., Swirszcz G., & Abe N. (2011). Group orthogonal matching pursuit for logistic regression. In Proceedings of the Fourteenth International Conference on Artificial Intelligence and Statistics.

The  $\gamma$ -OMP algorithm for feature selection with application to gene expression data. IEEE/ACM Transactions on Computational Biology and Bioinformatics (Accepted for publication) <https://arxiv.org/pdf/2004.00281.pdf>

**See Also**

[cor.fbed](#), [cor.fsreg](#), [correls](#), [fs.reg](#)

**Examples**

```
x <- matnorm(200, 100)
y <- rnorm(200)
a <- ompr(y, x)
a
x <- NULL
```

---

Outer function

*Outer function*

---

**Description**

The outer function.

**Usage**

```
Outer(x, y, oper = "*")
```

**Arguments**

x	A numerical vector.
y	A numerical vector.
oper	The available options are "*" (multiplication), "/" (division), "+" (sum), "-" (subtraction), "^" (power raise), and "

**Details**

The function is the same as R's "outer", but works with vectors only and probably has less capabilities, but faster.

**Value**

A matrix with all the combinations.

**Author(s)**

Manos Papadakis and Michail Tsagris

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

**See Also**

[mat.mult](#), [vecdist](#)

**Examples**

```
x <- rnorm(10)
y <- rnorm(10)
res<-Outer(x, y)
```

---

Partial distance correlation

*Partial distance correlation*

---

**Description**

Partial distance correlation.

**Usage**

```
pdcor(x, y, z)
```

**Arguments**

x	A numerical matrix.
y	A numerical matrix.
z	A numerical matrix.

**Details**

The partial distance correlation between x and y conditioning on z is computed.

**Value**

The partial distance correlation

**Author(s)**

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

Szekely G.J. and Rizzo M.L. (2014). Partial Distance Correlation with Methods for Dissimilarities. *Annals of Statistics*, 42(6): 2382–2412.

Szekely G. J. and Rizzo M. L. (2023). *The Energy of Data and Distance Correlation*. Chapman and Hall/CRC.

Tsagris M. and Papadakis M. (2025). Fast and light-weight energy statistics using the R package Rfast. <https://arxiv.org/abs/2501.02849>

**See Also**

[dcov](#), [dcor.ttest](#)

**Examples**

```
x <- as.matrix(iris[1:50, 1:4])
y <- as.matrix(iris[51:100, 1:4])
z <- as.matrix(iris[101:150, 1:4])
#pdcor(x, y, z)
x <- y <- NULL
```

---

Permutation

*Permutation*

---

**Description**

Permute the given vector.

**Usage**

```
permutation(x, nperm = gamma(length(x)+1))
permutation.next(x, nperm = gamma(length(x)+1))
permutation.prev(x, nperm = gamma(length(x)+1))
bincomb(n)
```

**Arguments**

x	A numeric vector with data.
nperm	An integer value for returning specific number of combinations. By default is set to all combinations. Must be between $0 \leq nperm \leq \gamma(\text{length}(x)+1)$
n	An integer value for the length of the binary number.

**Details**

This function implements "Permutation", which means all the possible combinations. In the permutation.next and permutation.prev if there aren't possible combinations it returns the same vector. "Binary Combinations" for "bincomb", means all the possible combinations for the binary number with length "n".

**Value**

Returns a matrix with all possible combinations of the given vector or a matrix row with one possible combinations.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>

**See Also**

[combn](#), [comb\\_n](#)

**Examples**

```
y <- rnorm(3)
b <- permutation(y)
b <- permutation.next(y)
b <- permutation.prev(y)
g <- bincomb(3)
```

---

Permutation based p-value for the Pearson correlation coefficient

*Permutation based p-value for the Pearson correlation coefficient*

---

**Description**

Permutation based p-value for the Pearson correlation coefficient.

**Usage**

```
permcov(x, y, R = 999)
```

**Arguments**

x	A numerical vector with the first variable.
y	A numerical vector with the second variable.
R	The number of permutations to be conducted; set to 999 by default.

**Details**

This is a very low computational calculation of the p-value. Try it yourselves.

**Value**

A vector consisting of two values, the Pearson correlation and the permutation based p-value.

**Author(s)**

Marios Dimitriadis and Michail Tsagris

R implementation and documentation: Marios Dimitriadis and Michail Tsagris <kmdimitriadis@gmail.com> and <mtsagris@csd.uoc.gr>

**References**

Chatzipantsiou C., Dimitriadis M., Papadakis M. and Tsagris M. (2019). Extremely efficient permutation and bootstrap hypothesis tests using R. To appear in the Journal of Modern Applied Statistical Methods.

<https://arxiv.org/ftp/arxiv/papers/1806/1806.10947.pdf>

**See Also**

[pc.skel](#)

**Examples**

```
x <- iris[, 1]
y <- iris[, 2]
permcors(x, y, R = 499)
```

---

Polyserial correlation

*Polyserial correlation*

---

**Description**

Polyserial correlation.

**Usage**

```
poly.cors(x, y)
```

**Arguments**

x	The continuous variable.
y	The ordinal variable, a numeric vector with numbers starting from 1.

**Details**

The polyserial correlation between a continuous and an ordinal variable is calculated. The function is not super fast, yet is faster than other implementations we found.

**Value**

A list including:

est	A vector with the polyserial correlation and its estimated variance.
test	A vector with the test statistic and its associated p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Olsson U., Drasgow F. and Dorans N. J. (1982). The polyserial correlation coefficient. *Psychometrika*, 47(3):337-347.

**See Also**

[correls](#), [Table](#)

**Examples**

```
x <- rnorm(100)
y <- rpois(100, 10) + 1
res<-poly.cor(x, y)
```

---

Pooled covariance matrix

*Pooled covariance matrix*

---

**Description**

Pooled covariance matrix.

**Usage**

```
pooled.cov(x, ina)
```

**Arguments**

x	A matrix with continuous data.
ina	A numerical vector indicating the groups. <b>The numbers must be consecutive and start from 1.</b>

**Details**

The spatial median is at first computed (if not supplied) and then the covariance matrix.

**Value**

The spatial sign covariance matrix.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

**References**

Durre A, Vogel D. and D.E. Tyler D.E.(2014). The spatial sign covariance matrix with unknown location. *Journal of Multivariate Analysis*, 130: 107-117. <http://arxiv.org/pdf/1307.5706v2.pdf>

**See Also**

[spat.med](#), [spatmed.reg](#)

**Examples**

```
res<-sscov( as.matrix(iris[, 1:4]) )
```

---

Prediction with some naive Bayes classifiers

*Prediction with some naive Bayes classifiers*

---

**Description**

Prediction with some naive Bayes classifiers.

**Usage**

```
gaussiannb.pred(xnew, m, s, ni)  
poissonnb.pred(xnew, m)  
multinomnb.pred(xnew, m)  
gammanb.pred(xnew, a, b)  
geomnb.pred(xnew, prob)
```

**Arguments**

xnew	A numerical matrix with new predictor variables whose group is to be predicted. For the Gaussian case this contains any numbers, but for the multinomial and Poisson cases, the matrix must contain integer valued numbers only.
m	A matrix with the group means. Each row corresponds to a group.
s	A matrix with the group colum-wise variances. Each row corresponds to a group.
ni	A vector with the frequencies of each group.
a	A vector with the shape parameters of each group.
b	A vector with the scale parameters of each group.
prob	A vector with the sprobability parameters of each group.

**Value**

A numerical vector with 1, 2, ... denoting the predicted group.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[gaussian.nb](#), [colpoisson.mle colVars](#)

**Examples**

```
ina <- sample(1:150, 100)
x <- as.matrix(iris[, 1:4])
id <- as.numeric(iris[, 5])
a <- gaussian.nb(xnew = NULL, x[ina, ], id[ina])
est <- gaussianb.pred(x[-ina, ], a$mu, a$sigma, a$ni)
res<-table(id[-ina], est)
```

---

Quasi binomial regression for proportions

*Quasi binomial regression for proportions*

---

**Description**

Quasi binomial regression for proportions.

**Usage**

```
prop.reg(y, x, varb = "quasi", tol = 1e-09, maxiters = 100)
prop.regs(y, x, varb = "quasi", tol = 1e-09, logged = FALSE, maxiters = 100)
```

**Arguments**

y	A numerical vector proportions. 0s and 1s are allowed.
x	For the "prop.reg" a matrix with data, the predictor variables. This can be a matrix or a data frame. For the "prop.regs" this must be a numerical matrix, where each columns denotes a variable.
tol	The tolerance value to terminate the Newton-Raphson algorithm. This is set to $10^{-9}$ by default.
varb	The type of estimate to be used in order to estimate the covariance matrix of the regression coefficients. There are two options, either "quasi" (default value) or "glm". See the references for more information.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?
maxiters	The maximum number of iterations before the Newton-Raphson is terminated automatically.

**Details**

We are using the Newton-Raphson, but unlike R's built-in function "glm" we do no checks and no extra calculations, or whatever. Simply the model. The "prop.regs" is to be used for very many univariate regressions. The "x" is a matrix in this case and the significance of each variable (column of the matrix) is tested. The function accepts binary responses as well (0 or 1).

**Value**

For the "prop.reg" function a list including:

iters	The number of iterations required by the Newton-Raphson.
varb	The covariance matrix of the regression coefficients.
phi	The phi parameter is returned if the input argument "varb" was set to "glm", otherwise this is NULL.
info	A table similar to the one produced by "glm" with the estimated regression coefficients, their standard error, Wald test statistic and p-values.

For the "prop.regs" a two-column matrix with the test statistics (Wald statistic) and the associated p-values (or their loggarithm).

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

- Papke L. E. & Wooldridge J. (1996). Econometric methods for fractional response variables with an application to 401(K) plan participation rates. *Journal of Applied Econometrics*, 11(6): 619–632.
- McCullagh, Peter, and John A. Nelder. *Generalized linear models*. CRC press, USA, 2nd edition, 1989.

**See Also**

[anova\\_propreg](#), [univglms](#), [score.glms](#), [logistic\\_only](#)

**Examples**

```
y <- rbeta(100, 1, 4)
x <- matrix(rnorm(100 * 3), ncol = 3)
a <- prop.reg(y, x)
y <- rbeta(100, 1, 4)
x <- matrix(rnorm(400 * 100), ncol = 400)
b <- prop.regs(y, x)
res<-mean(b[, 2] < 0.05)
```

---

Quasi Poisson regression for count data

*Quasi Poisson regression*

---

**Description**

Quasi Poisson regression.

**Usage**

```
qpois.reg(x, y, full = FALSE, tol = 1e-09, maxiters = 100)
qpois.regs(x, y, tol = 1e-09, logged = FALSE)
```

**Arguments**

<code>x</code>	For the "qpois.reg" a matrix with data, the predictor variables. This can be a matrix or a data frame. For the "qpois.regs" this must be a numerical matrix, where each columns denotes a variable.
<code>y</code>	A numerical vector with positive discrete data.
<code>full</code>	If this is FALSE, the coefficients, the deviance and the estimated phi parameter will be returned only. If this is TRUE, more information is returned.
<code>tol</code>	The tolerance value to terminate the Newton-Raphson algorithm. This is set to $10^{-9}$ by default.
<code>logged</code>	Should the p-values be returned (FALSE) or their logarithm (TRUE)?
<code>maxiters</code>	The maximum number of iterations before the Newton-Raphson is terminated automatically.

**Details**

We are using the Newton-Raphson, but unlike R's built-in function "glm" we do no checks and no extra calculations, or whatever. Simply the model, unless the user requests for the Wald tests of the coefficients. The "qpois.regs" is to be used for very many univariate regressions. The "x" is a matrix in this case and the significance of each variable (column of the matrix) is tested.

**Value**

For the "prop.reg" a list including: When full is FALSE

be	The regression coefficients.
devi	The deviance of the model.
varb	The covariance matrix of the beta coefficients.
phi	The phi parameter, the estimate of dispersion.

When full is TRUE, the additional item is:

info	The regression coefficients, their standard error, their Wald test statistic and their p-value.
------	---

For the "prop.regs" a two-column matrix with the test statistics (Wald statistic) and the associated p-values (or their loggarithm).

**Author(s)**

Manos Papadakis and Marios Dimitriadis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com> and Marios Dimitriadis <kmdimitriadis@gmail.com>.

**References**

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

[prop.reg.univglms](#), [score.glms](#), [poisson\\_only](#)

**Examples**

```
y <- rbinom(100, 10, 0.6)
x <- matrix(rnorm(100*3), ncol = 3)
mod1 <- glm(y ~ x, quasipoisson)
res<-summary(mod1)
res<-qpois.reg(x, y, full = TRUE)
res<-qpois.regs(x, y)
```

---

 Random intercepts linear mixed models

*Random intercepts linear mixed models*


---

### Description

Random intercepts linear mixed models (for balanced data with a single identical covariate).

### Usage

```
rint.reg(y, x, id ,tol = 1e-08, ranef = FALSE, maxiters = 100)
rint.regbx(y, x, id)
```

### Arguments

y	A numerical vector with the data. The subject values.
x	For the case of "rint.reg" this can be a vector or a numerical matrix with data. In the case of "rint.regbx" this is a numerical vector with the same length as y indicating the fixed predictor variable. Its values are the same for all levels of y. An example of this x is time which is the same for all subjects.
id	A numerical variable with 1, 2, ... indicating the subject.
tol	The tolerance level to terminate the generalised elast squares algorithm.
ranef	If you want to obtain the random effects (random intercepts) set this equal to TRUE.
maxiters	The max number of iterations that can take place in a regression.

### Details

Random intercepts linear mixed models with compound covariance structure is fitted in both functions. The "rint.reg" allows any numerical matrix, with balanced or unbalanced data. See Demidenko (2013, pg. 65-67) for more information.

The "rint.regbx" is a special case of a balanced random intercepts model with a compound symmetric covariance matrix and one single covariate which is constant for all replicates. An example, is time, which is the same for all subjects. Maximum likelihood estimation has been performed. In this case the mathematics exist in a closed formula (Demidenko, 2013, pg. 67-69).

### Value

A list including:

info	A vector with the random intercepts variance (between), the variance of the errors (within), the log-likelihood, the deviance (twice the log-likelihood) and the BIC. In the case of "rint.reg" it also includes the number of iterations required by the generalised least squares.
be	The estimated regression coefficients, which in the case of "rint.regbx" are simply two: the constant and the slope (time effect).
ranef	The random intercepts effects.

**Author(s)**

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Eugene Demidenko (2013). *Mixed Models: Theory and Applications with R*, 2nd Edition. New Jersey: Wiley & Sons (excellent book).

**See Also**

[rm.lines](#), [varcomps.mom](#), [colvarcomps.mom](#)

**Examples**

```
y <- rnorm(100)
x <- rnorm(10)
x <- rep(x, 10)
id <- rep(1:10, each = 10)
for (i in 1:20) a <- rint.reg(y, x, id)
```

---

Random values simulation from a von Mises distribution

*Random values simulation from a von Mises distribution*

---

**Description**

It generates random vectors following the von Mises distribution. The data can be spherical or hyper-spherical.

**Usage**

```
rvonmises(n, m, k, rads = TRUE)
```

**Arguments**

n	The sample size.
m	The mean angle expressed in radians or degrees.
k	The concentration parameter. If k is zero the sample will be generated from the uniform distribution over $(0, 2\pi)$ .
rads	If the mean angle is expressed in radians, this should be TRUE and FALSE otherwise. The simulated data will be expressed in radians or degrees depending on what the mean angle is expressed.

**Details**

The mean direction is transformed to the Euclidean coordinates (i.e. unit vector) and then the `fvmf` function is employed. It uses a rejection sampling as suggested by Andrew Wood in 1994. I have mentioned the description of the algorithm as I found it in Dhillon and Sra in 2003. Finally, the data are transformed to radians or degrees.

**Value**

A vector with the simulated data.

**Author(s)**

Michail Tsagris and Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm85@gmail.com>

**References**

Wood, A. T. (1994). Simulation of the von Mises Fisher distribution. *Communications in statistics-simulation and computation*, 23(1): 157-164.

Dhillon, I. S., & Sra, S. (2003). Modeling data using directional distributions. Technical Report TR-03-06, Department of Computer Sciences, The University of Texas at Austin. <http://citeseerx.ist.psu.edu/viewdoc/download?>

**See Also**

[vm.mle](#), [rvmf](#)

**Examples**

```
#x <- rvonmises(1000, 2, 25, rads = TRUE)
#res<-vm.mle(x)
```

---

Reading the files of a directory

*Reading the files of a directory*

---

**Description**

Reading the files of a directory.

**Usage**

```
read.examples(path.man,paths.full = FALSE)
read.directory(path.directory)
```

**Arguments**

`path.man`            The full path to the directory with the Rd files in it. For example: `"C:\Users\username\Documents\R\Rfas"`  
`paths.full`         Print or return the full paths.  
`path.directory`    The full path to the directory.

**Details**

For function `"read.examples"`: Takes as an argument a full path to the directory of the Rd files. If you don't want the program to read any file add at the top of the file the attribute `"%[dont read]"`.

**Value**

For function `"read.examples"`: a list with 2 fields

`examples`            A character vector with the examples of each Rd file.  
`files`                A character vector with the name of the file that each examples belongs.  
`long_lines`         A character vector with the name of the file that has large examples.

You can choose which files not to read for both R and Rd. You must add in the first line of the file in comment the "attribute" `"%[dont read]"`. Finally, that function wil return in the result a list of which files had this attribute.

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[AddToNamespace](#), [sourceR](#), [sourceRd](#), [checkRd](#), [checkExamples](#)

**Examples**

```
# for example: path.man="C:\some_file\man\"
# system.time( read.examples(path.man) )
# system.time( read.examples(path.man,dont.read=c("somef_1.Rd",...,"somef_n.Rd") ) )
```

---

Repeated measures anova

*Repeated measures anova*

---

**Description**

Repeated measures anova.

**Usage**

```
rm.anova(y, logged = FALSE)
```

**Arguments**

<code>y</code>	A matrix with the data, where each column refers to a different measurement. The rows denote the subjects.
<code>logged</code>	Should the p-values be returned (FALSE) or their logarithm (TRUE)?

**Details**

Found in Davis (2002) is the usual repeated measures ANOVA. In this case, suppose you have taken measurements on one or more variables from the same group of people. See the example below on how to put such data.

**Value**

A vector with the test statistic (t-test) and its associated p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Charles S. Davis (2002). Statistical methods for the analysis of repeated measures. Springer-Verlag, New York.

**See Also**

[rm.anovas](#), [rint.reg](#), [varcomps.mle](#)

**Examples**

```
y <- c(74.5,81.5,83.6,68.6,73.1,79.4,
75.5,84.6,70.6,87.3,73.0,75.0,
68.9,71.6,55.9,61.9,60.5,61.8,
57.0,61.3,54.1,59.2,56.6,58.8,
78.3,84.9,64.0,62.2,60.1,78.7,
54.0,62.8,63.0,58.0,56.0,51.5,
72.5,68.3,67.8,71.5,65.0,67.7,
80.8,89.9,83.2,83.0,85.7,79.6)
y <- matrix(y, ncol = 6, byrow = TRUE)
res<-rm.anova(y)
```

---

Replicate columns/rows

*Replicate columns/rows*

---

### Description

Replicate columns/rows.

### Usage

```
rep_col(x,n)
rep_row(x,n)
```

### Arguments

x	A vector with data.
n	Number of new columns/rows.

### Value

A matrix where each column/row is equal to "x".

### Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

### See Also

[rowMins](#), [rowFalse](#), [nth](#), [colrange](#), [colMedians](#), [colVars](#), [colSort](#), [rowSort](#), [rowTrue](#)

### Examples

```
x <- runif(10)
all.equal(rep_col(x,10),matrix(x,nrow=length(x),ncol=10))
all.equal(rep_row(x,10),matrix(x,ncol=length(x),nrow=10,byrow=TRUE))
```

---

**Representation of Stack***Representation of Stack*

---

**Description**

Representation of Stack.

**Usage**

```
Stack(x, type=NULL)
```

**Arguments**

x	Any type that could be convert to vector or an integer value.
type	A type for the Stack, "integer", "numeric" or any other that accepts one argument.

**Details**

Stack is an abstract data type - data structure based on the principle of last in first out. To access the 3 fields, use operator "\$".

**Value**

An object of class "Stack". This object holds 3 fields:

pop: remove the first element (from the top). top: access the first element (from the top). push: add an element to the top of the Stack.

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colShuffle](#), [colVars](#), [colmeans](#)

**Examples**

```
x<-Stack(10,type=integer)

x$push(5)
x$push(10)
x$top() == 10
x$pop()
x$top() == 5

y<-rnorm(10)
```

```
x<-Stack(x)

x$push(5) # length increased to 11
x$top() # access the last element that pushed, 5
x$pop() # pop the last element that pushed
```

---

Round each element of a matrix/vector

*Round each element of a matrix/vector*

---

### Description

Round each element of a matrix/vector.

### Usage

```
Round(x,digit=0,na.rm = FALSE)
```

### Arguments

x	A numeric matrix/vector with data or NA. NOT integer values.
digit	An integer value for 0...N-1 where N is the number of the digits. By default is 0.
na.rm	TRUE or FALSE for remove NAs if exists.

### Details

Round is a very fast C++ implementation. Especially for large data. It handles NA.

### Value

A vector/matrix where each element is been rounded in the given digit.

### Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

### See Also

[Lchoose](#), [Log](#), [Choose](#)

**Examples**

```
x <-matrix( rnorm( 50 * 10), ncol = 10 )
a <- Round(x,5)
b <- round(x,5)
all.equal(a,b) #true
x <-rnorm( 1000)
a <- Round(x,5)
b <- round(x,5)
all.equal(a,b) # true
```

---

Row - Wise matrix/vector count the frequency of a value

*Row - Wise matrix/vector count the frequency of a value*

---

**Description**

Row - Wise matrix/vector count the frequency of a value.

**Usage**

```
count_value(x, value)
colCountValues(x, values, parallel = FALSE, cores = 0)
rowCountValues(x, values, parallel = FALSE, cores = 0)
```

**Arguments**

x	A vector with the data (numeric or character) or a numeric matrix.
value	The value, numeric or character, to check its frequency in the vector "x".
values	a vector with the values to check its frequency in the matrix "x" by row or column.
parallel	Do you want to do it in parallel in C++? TRUE or FALSE. Works with every other argument.
cores	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

**Details**

The functions is written in C++ in order to be as fast as possible. The "x" and "value" must have the same type. The type can be numeric or character.

**Value**

The frequency of a value/values in a vector in linear time or by row/column in a matrix.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Median](#), [binary\\_search](#), [Order](#), [nth](#)

**Examples**

```
x <- rnorm(100)
value <- x[50]
count_value(x,value)
y <- sample(letters,replace=TRUE)
value <- "r"
count_value(y,value)
values <- sample(x,100,replace=TRUE)
x <- matrix(x,100,100)
res<-colCountValues(x,values)
res<-rowCountValues(x,values)
x<-value<-values<-y<-NULL
```

---

Row-wise minimum and maximum

*Row-wise minimum and maximum of a matrix*

---

**Description**

Row-wise minimum and maximum of a matrix.

**Usage**

```
rowMins(x, value = FALSE)
rowMaxs(x, value = FALSE)
rowMinsMaxs(x)
```

**Arguments**

x	A numerical matrix with data.
value	If the value is FALSE it returns the indices of the minimum/maximum, otherwise it returns the minimum and maximum values.

**Value**

A vector with the relevant values.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colMins](#), [colMaxs](#), [nth](#), [rowrange](#) [colMedians](#), [colVars](#), [colSort](#), [rowSort](#)

**Examples**

```
x <- matrix( rnorm(10 * 10), ncol = 10 )

s1 <- rowMins(x)
#s2 <- apply(x, 1, min)

s1 <- rowMaxs(x)
#s2 <- apply(x, 1, max)

#s1 <- c(apply(x, 1, min), apply(x, 1, max) )
s2 <- rowMinsMaxs(x)

x<-s1<-s2<-NULL
```

---

Row-wise true value     *Row-wise true value of a matrix*

---

**Description**

Row-wise true value of a matrix.

**Usage**

```
rowTrue(x)
rowFalse(x)
rowTrueFalse(x)
```

**Arguments**

x                    A logical matrix with data.

**Value**

An integer vector where item "i" is the number of the true/false values of "i" row.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[rowMins](#), [colFalse](#), [nth](#), [rowrange](#), [rowMedians](#), [rowVars](#), [colTrue](#)

**Examples**

```
x <- matrix(as.logical(rbinom(100*100,1,0.5)),100,100)
s1 <- rowTrue(x)
s1 <- rowFalse(x)
s1 <- rowTrueFalse(x)
x<-s1<-NULL
```

---

Search for variables with zero range in a matrix

*Search for variables with zero range in a matrix*

---

**Description**

Search for variables with zero range in a matrix.

**Usage**

```
check_data(x, ina = NULL)
```

**Arguments**

<code>x</code>	A matrix or a data.frame with the data, where rows denotes the observations and the columns contain the dependent variables.
<code>ina</code>	If your data are grouped, for example there is a factor or numerical variable indicating the groups of the data supply it here, otherwise leave it NULL.

**Details**

The function identifies the variables with zero range, instead of a zero variance as this is faster. It will work with matrices and data.frames.

**Value**

A numerical vector of length zero if no zero ranged variable exists, or of length at least one with the index (or indices) of the variable(s) that need attention or need to be removed.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colrange](#), [colVars](#)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100 )
res<-check_data(x)

## some variables have a constant value
x[, c(1,10, 50, 70)] <- 1
res<-check_data(x)
id <- rep(1:4, each = 25 )
x[1:25, 2] <- 0
res<-check_data(x) ## did not use the id variable
res<-check_data(x, id) ## see now
x <- NULL
```

---

Significance testing for the coefficients of Quasi binomial or the quasi Poisson regression

*Significance testing for the coefficients of Quasi binomial or the quasi Poisson regression*

---

**Description**

Significance testing for the coefficients of Quasi binomial or the quasi Poisson regression.

**Usage**

```
anova_propreg(mod, poia = NULL)
anova_qpois.reg(mod, poia = NULL)
```

**Arguments**

<code>mod</code>	An object as returned by the "prop.reg" or the "qpois.reg" function.
<code>poia</code>	If you want to test the significance of a single coefficient this must be a number. In this case, the "prop.reg" or the "qpois.reg" function contains this information. If you want more coefficients to be testes simultaneously, e.g. for a categorical predictor, then this must contain the positions of the coefficients. If you want to see if all coefficients are zero, like an overall F-test, leave this NULL.

**Details**

Even though the name of this function starts with anova it is not an ANOVA type significance testing, but a Wald type.

**Value**

A vector with three elements, the test statistic value, its associated p-value and the relevant degrees of freedom.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**References**

Papke L. E. & Wooldridge J. (1996). Econometric methods for fractional response variables with an application to 401(K) plan participation rates. *Journal of Applied Econometrics*, 11(6): 619-632.

McCullagh, Peter, and John A. Nelder. *Generalized linear models*. CRC press, USA, 2nd edition, 1989.

**See Also**

[prop.reg](#), [qpois.reg](#), [univglms](#), [score.glms](#), [logistic\\_only](#)

**Examples**

```
y <- rbeta(1000, 1, 4)
x <- matrix(rnorm(1000 * 3), ncol = 3)
a <- prop.reg(y, x)
## all coefficients are tested
res<-anova_propreg(a)
## the first predictor variable is tested
res<-anova_propreg(a, 2)
a ## this information is already included in the model output
## the first and the second predictor variables are tested
res<-anova_propreg(a, 2:3)
```

---

Simulation of random values from a Bingham distribution  
*Simulating from a Bingham distribution*

---

**Description**

Simulation from a Bingham distribution using the code suggested by Kent et al. (2013).

**Usage**

```
rbing(n, lam)
```

**Arguments**

n	Sample size.
lam	Eigenvalues of the diagonal symmetric matrix of the Bingham distribution. See details for more information on this.

**Details**

The user must have calculated the eigenvalues of the diagonal symmetric matrix of the Bingham distribution. The function accepts the q-1 eigenvalues only. This means, that the user must have subtracted the lowest eigenvalue from the rest and give the non zero ones. The function uses rejection sampling.

**Value**

A matrix with the simulated data.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

**References**

- Kent J.T., Ganeiber A.M. and Mardia K.V. (2013). A new method to simulate the Bingham and related distributions in directional data analysis with applications. <http://arxiv.org/pdf/1310.8110v1.pdf>
- C.J. Fallaize and T. Kypraios (2014). Exact Bayesian Inference for the Bingham Distribution. Statistics and Computing (No volum assigned yet). <http://arxiv.org/pdf/1401.2894v1.pdf>

**See Also**

[rvmf](#)

**Examples**

```
x <- rbing( 100, c(1, 0.6, 0.1) )
x
```

---

Simulation of random values from a Bingham distribution with any symmetric matrix

*Simulation of random values from a Bingham distribution with any symmetric matrix*

---

**Description**

Simulation of random values from a Bingham distribution with any symmetric matrix.

**Usage**

```
rbingham(n, A)
```

**Arguments**

n	Sample size.
A	A symmetric matrix.

**Details**

The eigenvalues of the  $q \times q$  symmetric matrix  $A$  are calculated and the smallest of them is subtracted from the rest. The  $q - 1$  non zero eigenvalues are then passed to [rbing](#). The generated data are then right multiplied by  $V^T$ , where  $V$  is the matrix of eigenvectors of the matrix  $A$ .

**Value**

A matrix with the simulated data.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

**References**

Kent J.T., Ganeiber A.M. and Mardia K.V. (2013). A new method to simulate the Bingham and related distributions in directional data analysis with applications. <http://arxiv.org/pdf/1310.8110v1.pdf>

C.J. Fallaize and T. Kypraios (2014). Exact Bayesian Inference for the Bingham Distribution. Statistics and Computing (No volum assigned yet). <http://arxiv.org/pdf/1401.2894v1.pdf>

**See Also**

[rvmf](#)

**Examples**

```
A <- cov( iris[, 1:4] )
x <- rbingham(100, A)
x
```

---

Simulation of random values from a normal distribution  
*Simulation of random values from a normal distribution*

---

**Description**

Simulation of random values from a normal distribution.

**Usage**

```
Rnorm(n, m = 0, s = 1, seed = NULL)
```

**Arguments**

n	The sample size.
m	The mean, set to 0 by default.
s	The standard deviation, set to 1 by default.
seed	If you want the same to be generated again use a seed for the generator, an integer number.

**Details**

By using the Ziggurat method of generating standard normal variates, this function is really fast when you want to generate large vectors. For less than 2,000 this might make no difference when compared with R's "rnorm", but for 10,000 this will be 6-7 times faster.

**Value**

A vector with n values.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**See Also**

[matrnorm](#), [rvonmises](#), [rvmf](#), [rmvnorm](#)

**Examples**

```
x <- Rnorm(500)
```

---

Simulation of random values from a von Mises-Fisher distribution  
*Random values simulation from a von Mises-Fisher distribution*

---

**Description**

It generates random vectors following the von Mises-Fisher distribution. The data can be spherical or hyper-spherical.

**Usage**

```
rvmf(n, mu, k, parallel = FALSE)
```

**Arguments**

n	The sample size.
mu	The mean direction, a unit vector.
k	The concentration parameter. If $k = 0$ , random values from the spherical uniform will be drawn. Values from a multivariate normal distribution with zero mean vector and the identity matrix as the covariance matrix. Then each vector becomes a unit vector.
parallel	Run the algorithm in parallel. The parallel algorithm needs memory.

**Details**

It uses a rejection sampling as suggested by Andrew Wood (1994).

**Value**

A matrix with the simulated data.

**Author(s)**

Michail Tsagris and Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm85@gmail.com>

**References**

Wood A. T. A. (1994). Simulation of the von Mises Fisher distribution. *Communications in statistics-simulation and computation*, 23(1): 157–164.

Dhillon I. S. & Sra S. (2003). Modeling data using directional distributions. Technical Report TR-03-06, Department of Computer Sciences, The University of Texas at Austin. <http://citeseerx.ist.psu.edu/viewdoc/download?>

**See Also**

[vmf.mle](#), [rvonmises](#), [iag.mle](#)

**Examples**

```
m <- rnorm(4)
m <- m/sqrt(sum(m^2))
#x <- rvmf(1000, m, 25)
#res<-vmf.mle(x)
```

---

Skeleton of the PC algorithm

*The skeleton of a Bayesian network produced by the PC algorithm*

---

**Description**

The skeleton of a Bayesian network produced by the PC algorithm.

**Usage**

```
pc.skel(dataset, method = "pearson", alpha = 0.01, R = 1, stat = NULL, ini.pvalue = NULL)
```

**Arguments**

dataset	A numerical matrix with the variables. If you have a data.frame (i.e. categorical data) turn them into a matrix using <code>data.frame.to.matrix</code> . Note, that for the categorical case data, the numbers must start from 0. No missing data are allowed.
method	If you have continuous data, you can choose either "pearson" or "spearman". If you have categorical data though, this must be "cat". In this case, make sure the minimum value of each variable is zero. The <code>g2Test</code> and the relevant functions work that way.
alpha	The significance level (suitable values in (0, 1)) for assessing the p-values. Default (preferred) value is 0.01.
R	The number of permutations to be conducted. The p-values are assessed via permutations. Use the default value if you want no permutation based assessment.
stat	If the initial test statistics (univariate associations) are available, pass them through this parameter.
ini.pvalue	if the initial p-values of the univariate associations are available, pass them through this parameter.

**Details**

The PC algorithm as proposed by Spirtes et al. (2000) is implemented. The variables must be either continuous or categorical, only. The skeleton of the PC algorithm is order independent, since we are using the third heuristic (Spirtes et al., 2000, pg. 90). At every stage of the algorithm use the pairs which are least statistically associated. The conditioning set consists of variables which are most statistically associated with each other of the pair of variables.

For example, for the pair (X, Y) there can be two conditioning sets for example (Z1, Z2) and (W1, W2). All p-values and test statistics and degrees of freedom have been computed at the first step

of the algorithm. Take the p-values between (Z1, Z2) and (X, Y) and between (Z1, Z2) and (X, Y). The conditioning set with the minimum p-value is used first. If the minimum p-values are the same, use the second lowest p-value. If the unlikely, but not impossible, event of all p-values being the same, the test statistic divided by the degrees of freedom is used as a means of choosing which conditioning set is to be used first.

If two or more p-values are below the machine epsilon (`.Machine$double.eps` which is equal to  $2.220446e-16$ ), all of them are set to 0. To make the comparison or the ordering feasible we use the logarithm of p-value. Hence, the logarithm of the p-values is always calculated and used.

In the case of the  $G^2$  test of independence (for categorical data) with no permutations, we have incorporated a rule of thumb. If the number of samples is at least 5 times the number of the parameters to be estimated, the test is performed, otherwise, independence is not rejected according to Tsamardinos et al. (2006). We have modified it so that it calculates the p-value using permutations.

### Value

A list including:

<code>stat</code>	The test statistics of the univariate associations.
<code>ini.pvalue</code>	The initial p-values univariate associations.
<code>pvalue</code>	The logarithm of the p-values of the univariate associations.
<code>runtime</code>	The amount of time it took to run the algorithm.
<code>kappa</code>	The maximum value of k, the maximum cardinality of the conditioning set at which the algorithm stopped.
<code>n.tests</code>	The number of tests conducted during each k.
<code>G</code>	The adjacency matrix. A value of 1 in $G[i, j]$ appears in $G[j, i]$ also, indicating that i and j have an edge between them.
<code>sepset</code>	A list with the separating sets for every value of k.

### Author(s)

Marios Dimitriadis.

R implementation and documentation: Marios Dimitriadis <[kmdimitriadis@gmail.com](mailto:kmdimitriadis@gmail.com)>.

### References

- Spirtes P., Glymour C. and Scheines R. (2001). Causation, Prediction, and Search. The MIT Press, Cambridge, MA, USA, 3rd edition.
- Tsamardinos I., Borboudakis G. (2010) Permutation Testing Improves Bayesian Network Learning. In Machine Learning and Knowledge Discovery in Databases. ECML PKDD 2010. 322-337.
- Tsamardinos I., Brown E.L. and Aliferis F.C. (2006). The max-min hill-climbing Bayesian network structure learning algorithm. Machine learning 65(1):31-78.

### See Also

[g2Test](#), [g2Test\\_univariate](#), [cora](#), [correls](#)

**Examples**

```
# simulate a dataset with continuous data
dataset <- matnorm(100, 10)
a <- pc.skel(dataset, method = "pearson", alpha = 0.05)
```

---

Skewness and kurtosis coefficients  
*Skewness and kurtosis coefficients*

---

**Description**

Skewness and kurtosis coefficients.

**Usage**

```
skew(x, pvalue = FALSE)
kurt(x, pvalue = FALSE)
```

**Arguments**

x	A numerical vector with data.
pvalue	If you want a hypothesis test that the skewness or kurtosis are significant set this to TRUE. This checks whether the skewness is significantly different from 0 and whether the kurtosis is significantly different from 3.

**Details**

The sample skewness and kurtosis coefficient are calculated. For the kurtosis we do not subtract 3.

**Value**

If "pvalue" is FALSE (default value) the skewness or kurtosis coefficients are returned. Otherwise, the p-value of the significance of the coefficient is returned.

**Author(s)**

Klio Lakiotaki  
R implementation and documentation: Klio Lakiotaki <kliolak@gmail.com>.

**References**

<https://en.wikipedia.org/wiki/Skewness>  
<https://en.wikipedia.org/wiki/Kurtosis>

**See Also**

[colskewness](#), [skew.test2](#), [colmeans](#), [colVars](#), [colMedians](#)

**Examples**

```
x <- rgamma(500,1, 4)
res<-skew(x)
res<-kurt(x, TRUE)
```

---

Some summary statistics of a vector for each level of a grouping variable

*Some summary statistics of a vector for each level of a grouping variable*

---

**Description**

Some summary statistics of a vector for each level of a grouping variable.

**Usage**

```
group(x, ina, method="sum", ina.min=NULL, ina.max = NULL,
      ina.length.unique=NULL, mad.method="median", std = FALSE, sorted = TRUE)
group.sum(x, ina, ina.max = NULL, ina.min = NULL)
```

**Arguments**

<code>x</code>	A numerical vector with data.
<code>ina</code>	A numerical vector with numbers. Note that zero and negative values are not allowed as this can cause R to run forever or crash.
<code>ina.length.unique</code>	Length of the unique numerical values of <code>ina</code> argument.
<code>method</code>	A character vector with values "sum", "var", "all", "any", "mad", "mean", "med", "min", "max", "min.max".
<code>ina.max</code>	Maximum number for vector <code>ina</code> .
<code>ina.min</code>	Minimum number for vector <code>ina</code> .
<code>mad.method</code>	A character vector with values "median", for median absolute deviation or "mean", for mean absolute deviation. This works only with <code>method="mad"</code> .
<code>std</code>	A boolean value for method <b>var</b> for using standard deviation.
<code>sorted</code>	A boolean value for getting the results sorted based on <code>ina</code> .

**Details**

This command works only for vectors. Median absolute deviation, mean, median, minimum, maximum are some of the options offered.

**Value**

A vector with the variance, or standard deviation, or mean, or minimum, or maximum, or median, or minimum-maximum of `x` for each distinct value of `ina`.

**Author(s)**

Manos Papadakis and Michail Tsagris

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

**See Also**

[colmeans](#), [colVars](#), [colMedians](#)

**Examples**

```
x <- rgamma(100,1, 4)
ina <- sample(1:5, 100, TRUE)
res<-group(x, ina,method="var")
```

---

Sort - Integer Sort - Sort a vector coresponding to another

*Sort - Integer Sort - Sort a vector coresponding to another*

---

**Description**

Fast sorting a vector.

**Usage**

```
Sort(x,descending=FALSE,partial=NULL,stable=FALSE,na.last=NULL,parallel = FALSE)
Sort.int(x)
sort_cor_vectors(x, base, stable = FALSE, descending = FALSE)
```

**Arguments**

x	A numerical/integer/character vector with data.
base	A numerical/character vector to help sorting the x.
descending	A boolean value (TRUE/FALSE) for sorting the vector in descending order. By default sorts the vector in ascending.
partial	This argument has two usages. The first is an index number for sorting partial the vector. The second is a vector with 2 values, start and end c(start,end). Gives you a vector where the elements between start and end will be sorted only. Not character vector.
stable	A boolean value (TRUE/FALSE) for choosing a stable sort algorithm. Stable means that discriminates on the same elements. Not character vector.
na.last	Accept 4 values. TRUE, FALSE, NA, NULL. TRUE/FALSE: for put NAs last or first. NA: for remove NAs completely from vector. NULL: by default. Leave it like that if there is no NA values.

`parallel` Do you want to do it in parallel, in C++? TRUE or FALSE. (Supported on Windows and most of the unix)

### Details

This function uses the sorting algorithm from C++. The implementation is very fast and highly optimised. Especially for large data.

### Value

`Sort` and `Sort.int`: The sorted vector.

`sort_cor_vectors`: The first argument but sorted according to the second.

### Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

### See Also

[nth](#), [colnth](#), [rownth](#), [sort\\_unique](#), [Round](#)

### Examples

```
x <- rnorm(1000)
s1 <- Sort(x)
s2 <- sort(x)
all.equal(s1,s2) #true but not if many duplicates.
```

```
s1 <- Sort(x,partial=100)
s2 <- sort(x,partial=100)
all.equal(s1,s2) #true
```

```
s1 <- Sort(x,stable=TRUE)
s2 <- sort(x)
all.equal(s1,s2) #true
```

```
x <- as.character(x)
s1 <- Sort(x)
s2 <- sort(x)
all.equal(s1,s2) #true
```

```
y <- runif(1000)
b <- sort_cor_vectors(x,y)
```

```
x<-rpois(100,100)
all.equal(Sort.int(x),sort.int(x))
```

```
x<-y<-y<-s1<-s2<-NULL
```

---

Sort and unique numbers

*Sort and unique*

---

## Description

Sort and unique numbers.

## Usage

```
sort_unique(x)
sort_unique.length(x)
Unique(x, fromLast = FALSE)
```

## Arguments

x	A numeric vector.
fromLast	logical indicating if duplication should be considered from the last, i.e., the last (or rightmost) of identical elements will be kept. This only matters for names or dimnames.

## Details

The "sort\_unique" function implements R's "unique" function using C++'s function but also sort the result. The "sort\_unique.length" returns the length of the unique numbers only for **itegers**.

## Value

Returns the discrete values or sorted or their length (depending on the function you do).

## Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>

## See Also

[colSort](#), [rowSort](#), [sort\\_cor\\_vectors](#)

## Examples

```
y <- rnorm(100)
a <- sort_unique(y)
b <- sort.int(unique(y))
all.equal(as.vector(a), as.vector(b))
x <- rpois(1000, 10)
sort_unique.length(x)
length(sort_unique(x))
```

```
x<-a<-b<-NULL
```

---

Sorting of the columns-rows of a matrix  
*Sorting of the columns-rows of a matrix*

---

### Description

Fast sorting of the columns-rows of a matrix.

### Usage

```
colSort(x, descending = FALSE, stable = FALSE, parallel=FALSE, cores = 0)  
rowSort(x, descending = FALSE, stable = FALSE, parallel=FALSE, cores = 0)  
sort_mat(x,by.row=FALSE,descending=FALSE,stable=FALSE,parallel=FALSE)
```

### Arguments

<code>x</code>	A numerical matrix or data.frame with data.
<code>descending</code>	If you want the sorting in descending order, set this to TRUE.
<code>stable</code>	If you the stable version, so that the results are the same as R's (in the case of ties) set this to TRUE. If this is TRUE, the algorithm is a bit slower.
<code>parallel</code>	Do you want to do it in parallel in C++? TRUE or FALSE. Works with every other argument.
<code>by.row</code>	TRUE or FALSE for applying sort in rows or column.
<code>cores</code>	Number of cores to use for parallelism. Valid only when argument parallel is set to TRUE. Default value is 0 and it means the maximum supported cores.

### Value

The matrix with its columns-rows (or rows) independently sorted.

### Author(s)

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

### See Also

[nth](#), [colMaxs](#), [colMins](#), [colrange](#), [sort\\_cor\\_vectors](#), [sort\\_unique](#)

**Examples**

```
x <- matrix( rnorm(100 * 200), ncol = 200 )
s1 <- colSort(x)
#s2 <- apply(x, 2, sort)
#all.equal(as.vector(s1), as.vector(s2))

x<-NULL
```

---

Source many R files     *Source many R files*

---

**Description**

Source many R/Rd files.

**Usage**

```
sourceR(path,local=FALSE,encode = "UTF-8",print.errors=FALSE)
sourceRd(path,print.errors=FALSE, macros = NULL)
```

**Arguments**

path	An full path to the directory where R file are.
local	TRUE, FALSE or an environment, determining where the parsed expressions are evaluated. FALSE (the default) corresponds to the user's workspace (the global environment) and TRUE to the environment from which source is called.
encode	Character vector. The encoding(s) to be assumed when file is a character string: see file. A possible value is "unknown" when the encoding is guessed: see the "Encodings" section.
print.errors	A boolean value (TRUE/FALSE) for printing the errors, if exists, for every file.
macros	A full or relative path to the macros file.

**Details**

Reads many R files and source them.

**Value**

Returns the files that had produced errors during source.

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[AddToNamespace](#)

**Examples**

```
# for example: path="C:\some_file\R\" where is R files are
# system.time( a<-sourceR(path) )
# for example: path="C:\some_file\man\" where is Rd files are
# system.time( a<-sourceRd(path) )
```

---

Spatial median for Euclidean data

*Spatial median for Euclidean data*

---

**Description**

Spatial median for Euclidean data.

**Usage**

```
spat.med(x, tol = 1e-09)
```

**Arguments**

x	A matrix with Euclidean data, continuous variables.
tol	A tolerance level to terminate the process. This is set to 1e-09 by default.

**Details**

The spatial median, using a fixed point iterative algorithm, for Euclidean data is calculated. It is a robust location estimate.

**Value**

A vector with the spatial median.

**Author(s)**

Manos Papadakis and Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

**References**

Jyrki Mottonen, Klaus Nordhausen and Hannu Oja (2010). Asymptotic theory of the spatial median. In *Nonparametrics and Robustness in Modern Statistical Inference and Time Series Analysis: A Festschrift in honor of Professor Jana Jureckova*.

T. Karkkainen and S. Ayramo (2005). On computation of spatial median for robust data mining. *Evolutionary and Deterministic Methods for Design, Optimization and Control with Applications to Industrial and Societal Problems, EUROGEN 2005*, R. Schilling, W.Haase, J. Periaux, H. Baier, G. Bugeđa (Eds) FLM, Munich. [http://users.jyu.fi/~samiayr/pdf/ayramo\\_eurogen05.pdf](http://users.jyu.fi/~samiayr/pdf/ayramo_eurogen05.pdf)

**See Also**[colMedians](#)**Examples**

```
res<-spat.med( as.matrix( iris[, 1:4] ) )
res<-colMeans( as.matrix(iris[, 1:4]) )
res<-colMedians( as.matrix(iris[, 1:4]) )
```

---

Spatial median regression

*Spatial median regression*

---

**Description**

Spatial median regression with Euclidean data.

**Usage**

```
spatmed.reg(y, x, tol = 1e-07)
```

**Arguments**

y	A matrix with the response variable.
x	The predictor variable(s), they have to be continuous.
tol	The threshold upon which to stop the iterations of the Newton-Rapshon algorithm.

**Details**

The objective function is the minimization of the sum of the absolute residuals. It is the multivariate generalisation of the median regression.

**Value**

A list including:

iters	The number of iterations that were required.
be	The beta coefficients.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Biman Chakraborty (2003) On multivariate quantile regression. Journal of Statistical Planning and Inference [http://www.stat.nus.edu.sg/export/sites/dsap/research/documents/tr01\\_2000.pdf](http://www.stat.nus.edu.sg/export/sites/dsap/research/documents/tr01_2000.pdf)

**See Also**

[spat.med](#), [sscov](#), [lmfit](#)

**Examples**

```
x <- as.matrix(iris[, 3:4])
y <- as.matrix(iris[, 1:2])
mod1 <- spatmed.reg(y, x)
```

---

Spatial sign covariance matrix  
*Spatial sign covariance matrix*

---

**Description**

Spatial sign covariance matrix.

**Usage**

```
sscov(x, me = NULL, tol = 1e-09)
```

**Arguments**

<code>x</code>	A matrix with continuous data.
<code>me</code>	If you have already computed the spatial median plug it in here.
<code>tol</code>	A tolerance level to terminate the process of finding the spatial median. This is set to 1e-09 by default.

**Details**

The spatial median is at first computed (if not supplied) and then the covariance matrix.

**Value**

The spatial sign covariance matrix.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <[mtsagris@uoc.gr](mailto:mtsagris@uoc.gr)>.

**References**

Durre A, Vogel D. and D.E. Tyler D.E.(2014). The spatial sign covariance matrix with unknown location. *Journal of Multivariate Analysis*, 130: 107-117. <http://arxiv.org/pdf/1307.5706v2.pdf>

**See Also**

[spat.med](#), [spatmed.reg](#)

**Examples**

```
res<-sscov( as.matrix(iris[, 1:4]) )
```

---

Spherical and hyperspherical median

*Fast calculation of the spherical and hyperspherical median*

---

**Description**

It calculates, very fast, the (hyper-)spherical median of a sample.

**Usage**

```
mediandir(x)
```

**Arguments**

x                    The data, a numeric matrix with unit vectors.

**Details**

The "mediandir" employes a fixed point iterative algorithm stemming from the first derivative (Cabrera and Watson, 1990) to find the median direction as described in Fisher (1985) and Fisher, Lewis and Embleton (1987).

**Value**

The median direction.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <[mtsagris@uoc.gr](mailto:mtsagris@uoc.gr)>

**References**

- Fisher N. I. (1985). Spherical medians. *Journal of the Royal Statistical Society. Series B*, 47(2): 342-348.
- Fisher N. I., Lewis T. and Embleton B. J. (1987). *Statistical analysis of spherical data*. Cambridge university press.
- Cabrera J. and Watson G. S. (1990). On a spherical median related distribution. *Communications in Statistics-Theory and Methods*, 19(6): 1973-1986.

**See Also**

[vmf.mle](#)

**Examples**

```
m <- rnorm(3)
m <- m / sqrt( sum(m^2) )
#x <- rvmf(100, m, 10)
#res<-mediandir(x)
x <- NULL
```

---

Standardisation

*Standardisation*

---

**Description**

Standardisation.

**Usage**

```
standardise(x, center = TRUE, scale = TRUE)
```

**Arguments**

- |        |   |
|--------|---|
| x      | A matrix with data. It has to be matrix, if it is data.frame for example the function does not turn it into a matrix. |
| center | Should the data be centred as well? TRUE or FALSE.  |
| scale  | Should the columns have unit variance, yes (TRUE) or no (FALSE)?  |

**Details**

Similar to R's built in functions "scale" there is the option for centering or scaling only or both (default).

**Value**

A matrix with the standardised data.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colVars](#), [colmeans](#), [colMads](#)

**Examples**

```
x <- matnorm( 100, 100 )
a1 <- scale(x)[1:100, ]
a2 <- standardise(x)
all.equal(as.vector(a1), as.vector(a2))
x <- NULL
```

---

Sub-matrix

*Sub-matrix*

---

**Description**

Sub-matrix.

**Usage**

```
submatrix(x, rowStart=1, rowEnd=1, colStart=1, colEnd=1)
```

**Arguments**

x	A Matrix, List, Dataframe or Vector.
rowStart	Start of the row.
rowEnd	End of the row.
colStart	Start of the col.
colEnd	End of the col.

**Value**

sub matrix like R's, `x[startrow:endrow,startcol:endcol]`. Fast especially for big sub matrices.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[Match](#), [mvbetas](#), [correals](#), [univglms](#), [colsums](#), [colVars](#)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100 )
res<-submatrix(x,1,50,1,25) # x[1:50,1:25]

x<-NULL
```

---

Table Creation - Frequency of each value

*Table Creation - Frequency of each value*

---

**Description**

Table Creation - Frequency of each value.

**Usage**

```
Table(x,y=NULL,names = TRUE,useNA = FALSE,rm.zeros = FALSE)
Table.sign(x,names = TRUE,useNA = FALSE)
```

**Arguments**

x	A vector with numeric/character data.
names	A logical value (TRUE/FALSE) for add names.
y	A vector with numeric/character data. Doesn't work with "useNA".
rm.zeros	A logical value for removing zero columns/rows. Only for integer vectors for now.
useNA	Table: Integer/logical value: FALSE: not NA values in vector. TRUE: count NAs and add the value in the last position of the returned vector. any other integer except 0,1: for just removing NAs. Table.sign: Logical value, TRUE, for count NAs. Otherwise FALSE. Doesn't work character data.

**Details**

Like R's "table":

for giving one argument,"x": If "names" is FALSE then, if "useNA" is TRUE then the NAs will be count, if is FALSE it means there are no NAs and for any other integer value the NAs will be ignored.

for giving two arguments,"x","y": If "names" is FALSE then, creates the contingency table, otherwise sets the col-row names with discrete values. If "rm.zeros" is FALSE then it won't remove the zero

columns/rows from the result but it will work only for positive integers for now. For this if "names" is TRUE then the col-row names will be the seq(min(),max()) for "x","y". In future updates it will be changed.

for both algorithms: You can't use "useNA" with "names" for now. It is much faster to get the result without names (names = FALSE) but all the algorithms are more efficient than R's.

Like R's "table(sign())" but more efficient. Count the frequencies of positives, negatives, zeros and NAs values. If argument "names" is FALSE then the returned vector doesn't have names. Otherwise "-1,0,+1,NA". If "useNA" is TRUE then the NAs will be count, otherwise not. You can use "useNA" with "names".

## Value

Table:

for giving one argument,"x": if "names" is TRUE then return a vector with names the discrete values of "x" and values there frequencies, otherwise only the frequencies

for giving two arguments,"x","y": if "names" is TRUE then return a contingency matrix with row-names the discrete values of "x", colnames the discrete values of "y" and values the frequencies of the pairs, otherwise only the frequencies of the pairs.

Table.sign: A vector with 4 values/frequencies: index 1: negatives index 2: zeros index 3: positives if "names" is TRUE then the returned vector have names "-1,0,+1". if "useNA" is TRUE then 4th value has the frequencies of NAs and the returned vector will have one more name, "-1,0,+1,NA", if "names" is also TRUE.

## Author(s)

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

## See Also

[colShuffle](#), [colVars](#), [colmeans](#), [is\\_integer](#), [as\\_integer](#)

## Examples

```
x<-runif(10)
y1<-Table(x)
y2<-as.vector(table(x)) # Needs a lot of time.
all.equal(y1,y2)
y1<-Table(x,names=FALSE)
all.equal(y1,y2) # the name attribute of y1 is null

y1<-Table.sign(x)
y2<-table(sign(x))
all.equal(y1,y2)

x<-y1<-y2<-NULL
```

---

Tests for the dispersion parameter in Poisson distribution

*Tests for the dispersion parameter in Poisson distribution*

---

### Description

Tests for the dispersion parameter in Poisson distribution.

### Usage

```
poisdisp.test(y, alternative = "either", logged = FALSE)
pois.test(y, logged = FALSE)
```

### Arguments

y	A numerical vector with count data, 0, 1,...
alternative	Do you want to test specifically for either over or underspersion ("either"), overdispersion ("over") or underspersion ("under")?
logged	Set to TRUE if you want the logarithm of the p-value.

### Value

A vector with two elements, the test statistic and the (logged) p-value.

### Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

### References

Yang Zhao, James W. Hardin, and Cheryl L. Addy. (2009). A score test for overdispersion in Poisson regression based on the generalized Poisson-2 model. *Journal of statistical planning and inference* 139(4): 1514-1521.

Dimitris Karlis and Evdokia Xekalaki (2000). A Simulation Comparison of Several Procedures for Testing the Poisson Assumption. *Journal of the Royal Statistical Society. Series D (The Statistician)*, 49(3): 355-382.

Bohning, D., Dietz, E., Schaub, R., Schlattmann, P. and Lindsay, B. (1994) The distribution of the likelihood ratio for mixtures of densities from the one-parameter exponential family. *Annals of the Institute of Statistical Mathematics*, 46(): 373-388.

### See Also

[poisson.mle](#), [negbin.mle](#), [poisson.anova](#), [poisson.anovas](#), [poisson\\_only](#)

**Examples**

```
y <- rnbinom(500, 10, 0.6)
res<-poisdisp.test(y, "either")
res<-poisdisp.test(y, "over")
res<-pois.test(y)
```

```
y <- rpois(500, 10)
res<-poisdisp.test(y, "either")
res<-poisdisp.test(y, "over")
res<-pois.test(y)
```

---

Topological sort of a DAG

*Topological sort of a DAG*

---

**Description**

Topological sort of a DAG.

**Usage**

```
topological_sort(dag)
```

**Arguments**

dag	A square matrix representing a directed graph which contains 0s and 1s. If $G[i, j] = 1$ it means there is an arrow from node $i$ to node $j$ . When there is no edge between nodes $i$ and $j$ if $G[i, j] = 0$ .
-----	--

**Details**

The function is an R translation from an old matlab code.

**Value**

A vector with numbers indicating the sorting. If the dag is not a Directed acyclic Graph, NA will be returned.

**Author(s)**

Michail Tsagris and Manos Papadakis

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>

**References**

Chickering, D.M. (1995). A transformational characterization of equivalent Bayesian network structures. Proceedings of the 11th Conference on Uncertainty in Artificial Intelligence, Montreal, Canada, 87-98.

**See Also**

[floyd](#), [pc.skel](#)

**Examples**

```
G <- matrix(0, 5, 5)
G[2, 1] <- 1
G[3, 1] <- 1
G[4, 2] <- 1
G[5, 4] <- 1
res<-topological_sort(G)
G[2, 4] <- 1
res<-topological_sort(G)
```

---

Transpose of a matrix *Transpose of a matrix*

---

**Description**

Transpose of a matrix.

**Usage**

```
transpose(x)
```

**Arguments**

`x`                    A numerical **square** matrix with data.

**Value**

The transposed matrix.

**Author(s)**

Manos Papadakis

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**References**

Gilbert Strang (2006). Linear Algebra and its Applications (4th edition).

**See Also**

[nth](#), [colMaxs](#), [colMins](#), [colrange](#)

**Examples**

```
x <- matrix( rnorm(100 * 100), ncol = 100, nrow=100 )
transpose(x) #t(x)

x<-NULL
```

---

Uniformity test for circular data

*Uniformity tests for circular data*

---

**Description**

Hypothesis tests of uniformity for circular data.

**Usage**

```
kuiper(u)

watson(u)
```

**Arguments**

`u` A numeric vector containing the circular data which are expressed in radians.

**Details**

These tests are used to test the hypothesis that the data come from a circular uniform distribution.

**Value**

A vector with two elements, the value of the test statistic and its associated p-value.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Jammalamadaka, S. Rao and SenGupta, A. (2001). Topics in Circular Statistics, pg. 153-55 (Kuiper's test) & 156-157 (Watson's test).

**See Also**

[vmf.mle](#), [rvonmises](#)

**Examples**

```
#x <- rvonmises(n = 50, m = 2, k = 10)
#res<-kuiper(x)
#res<-watson(x)
x <- runif(50, 0, 2 * pi)
#res<-kuiper(x)
#res<-watson(x)
```

---

Variance of a vector    *Variance (and standard deviation) of a vector*

---

**Description**

Variance (and standard deviation) of a vector.

**Usage**

```
Var(x, std = FALSE, na.rm = FALSE)
```

**Arguments**

x	A vector with data.
std	If you want the standard deviation set this to TRUE, otherwise leave it FALSE.
na.rm	TRUE or FALSE for remove NAs if exists.

**Details**

This is a faster calculation of the usual variance of a matrix.

**Value**

The variance of the vector.

**Author(s)**

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colVars](#), [cova](#)

**Examples**

```
x <- rnorm(100)
a1 <- Var(x)
a2 <- var(x)
x<-NULL
```

---

Vector allocation in a symmetric matrix  
*Vector allocation in a symmetric matrix*

---

**Description**

Vector allocation in a symmetric matrix.

**Usage**

```
squareform(x)
```

**Arguments**

**x** An numerical vector whose size must be the one that matches the dimensions of the final matrix. See examples.

**Details**

The functions is written in C++ in order to be as fast as possible.

**Value**

A symmetric matrix. The vector is allocated in the upper and in the lower part of the matrix. The diagonal is filled with zeros.

**Author(s)**

R implementation and documentation: Manos Papadakis <papadakm95@gmail.com>.

**See Also**

[colShuffle](#), [colVars](#), [colmeans](#)

**Examples**

```
x <- rnorm(1)
res<-squareform(x) ## OK
x <- rnorm(3)
res<-squareform(x) ## OK
x <- rnorm(4)
res<-squareform(x) ## not OK
```

---

Weibull regression model

*Weibull regression model*

---

### Description

Weibull regression model.

### Usage

```
weib.reg(y, x, tol = 1e-07, maxiters = 100)
```

### Arguments

y	The dependent variable; a numerical vector with strictly positive data, i.e. greater than zero.
x	A matrix with the data, where the rows denote the samples (and the two groups) and the columns are the variables. This can be a matrix or a data.frame (with factors).
tol	The tolerance value to terminate the Newton-Raphson algorithm.
maxiters	The max number of iterations that can take place in each regression.

### Details

The function is written in C++ and this is why it is very fast. No standard errors are returned as they are not correctly estimated. We focused on speed.

### Value

When full is FALSE a list including:

iters	The iterations required by the Newton-Raphson.
loglik	The log-likelihood of the model.
shape	The shape parameter of the Weibull regression.
be	The regression coefficients.

### Author(s)

Stefanos Fafalios

R implementation and documentation: Stefanos Fafalios <stefanosfafalios@gmail.com>.

### References

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

**See Also**

[poisson\\_only](#), [logistic\\_only](#), [univglms](#), [regression](#)

**Examples**

```
x <- matrix(rnorm(100 * 2), ncol = 2)
y <- rexp(100, 1)
res<-weib.reg(y, x)
```

---

Yule's Y (coefficient of colligation)

*Yule's Y (coefficient of colligation)*

---

**Description**

Yule's Y (coefficient of colligation).

**Usage**

```
yule(x)
```

**Arguments**

**x** A 2 x 2 matrix or a vector with 4 elements. In the case of the vector make sure it corresponds to the correct table.

**Details**

Yule's coefficient of colligation is calculated.

**Value**

Yule's Y is returned.

**Author(s)**

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R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>

**References**

Yule G. Udny (1912). On the Methods of Measuring Association Between Two Attributes. *Journal of the Royal Statistical Society*, 75(6):579-652.

**See Also**

[col.yule](#), [odds.ratio](#)

**Examples**

```
x <- rpois(4, 30) + 2
res<-yule(x)
res<-yule( matrix(x, ncol = 2) )
```

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