

# Package ‘assist’

May 7, 2026

**Title** A Suite of R Functions Implementing Spline Smoothing Techniques

**Version** 3.1.9

**Description** Fit various smoothing spline models. Includes an `ssr()` function for smoothing spline regression, an `nnr()` function for nonparametric nonlinear regression, an `snr()` function for semiparametric nonlinear regression, an `slm()` function for semiparametric linear mixed-effects models, and an `snm()` function for semiparametric nonlinear mixed-effects models. See Wang (2011) <[doi:10.1201/b10954](https://doi.org/10.1201/b10954)> for an overview.

**Depends** R (>= 3.0.2), nlme, lattice

**License** GPL-2

**LazyData** true

**URL** <https://yuedong.faculty.pstat.ucsb.edu/software.html>

**NeedsCompilation** yes

**Author** Yuedong Wang [aut, cre],  
Chunlei Ke [aut],  
Cleve Moler [cph]

**Maintainer** Yuedong Wang <yuedong@ucsb.edu>

**Repository** CRAN

**Date/Publication** 2023-08-22 07:00:02 UTC

## Contents

acid	3
alogit	4
anova.ssr	4
Arosa	6
bdiag	7
bond	7
canadaTemp	8
chickenpox	9
chol.new	9
climate	10
dcrdr	11

deviance.ssr . . . . .	11
dmudr . . . . .	12
dog . . . . .	14
dsidr . . . . .	14
dsms . . . . .	16
gdmudr . . . . .	17
gdsidr . . . . .	19
hat.ssr . . . . .	21
horm.cort . . . . .	22
ident . . . . .	23
inc . . . . .	23
intervals.nnr . . . . .	24
intervals.slm . . . . .	26
intervals.snm . . . . .	28
intervals.snr . . . . .	29
kron . . . . .	31
lspline . . . . .	32
nnr . . . . .	33
nnr.control . . . . .	35
paramecium . . . . .	36
periodic . . . . .	37
plot.bCI . . . . .	38
plot.ssr . . . . .	39
Polynomial . . . . .	40
Polynomial2 . . . . .	41
predict.slm . . . . .	42
predict.snm . . . . .	43
predict.snr . . . . .	44
predict.ssr . . . . .	45
print.anova.ssr . . . . .	47
print.nnr . . . . .	47
print.slm . . . . .	48
print.snm . . . . .	49
print.snr . . . . .	49
print.ssr . . . . .	50
print.summary.nnr . . . . .	51
print.summary.slm . . . . .	51
print.summary.snm . . . . .	52
print.summary.snr . . . . .	53
print.summary.ssr . . . . .	53
rk.prod . . . . .	54
seizure . . . . .	55
Shrinkage . . . . .	56
sine4p . . . . .	57
slm . . . . .	58
snm . . . . .	59
snm.control . . . . .	61
snr . . . . .	62

snr.control . . . . .	64
sphere . . . . .	66
ssr . . . . .	67
ssr.control . . . . .	69
ssr.object . . . . .	71
star . . . . .	72
Stratford . . . . .	72
summary.nnr . . . . .	73
summary.slm . . . . .	74
summary.snm . . . . .	74
summary.snr . . . . .	75
summary.ssr . . . . .	76
Thin . . . . .	76
TXtemp . . . . .	78
ultrasound . . . . .	79
USAtemp . . . . .	80
wesdr . . . . .	80
xyplot2 . . . . .	81
<b>Index</b>	<b>82</b>

---

 acid

*Lake Acidity Study*


---

## Description

The acid data frame has 112 rows and 4 columns of data derived based on the Eastern Lakes Survey of 1984 implemented by the Environmental Protection Agency of the USA.

## Usage

```
data(acid)
```

## Format

The data frame contains the following columns:

ph a numeric vector of surface pH values.

t1 a numeric vector of calcium concentrations in log10 milligrams per liter.

x1, x2 numeric vectors of the lakes' geographic locations.

## Details

112 lakes are extracted in the southern Blue Ridge mountains area. The surface pH values were recorded together with the calcium concentration and geographic locations.

**Source**

Douglas, A. and Delampady, M. (1990), Eastern Lake Survey Phase I: Documentation for the Data Base and the Derived Data sets. Tech Report 160 (SIMS), Dept. Statistics, University of British Columbia.

**References**

Gu, C. and Wahba, G. (1993) Smoothing Spline ANOVA with component-wise Bayesian confidence intervals. *Journal of Computational and Graphic Statistics* 55, 353-368.

---

alogit	<i>Calculate the Inverse Logit Transformation</i>
--------	---

---

**Description**

Perform an inverse logit calculation

**Usage**

```
alogit(x)
```

**Arguments**

x                    a numeric value

**Value**

Returned is  $e^x / (1 + e^x)$ .

**Author(s)**

Chunlei ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

---

anova.ssr	<i>Testing a Non-parametric Function Fitted via Smoothing Splines</i>
-----------	---

---

**Description**

For smoothing spline models with a single smoothing parameter, test the hypothesis that the unknown function lies in the null space using the local most powerful (LMP) test and a GCV or GML test.

**Usage**

```
## S3 method for class 'ssr'
anova(object, simu.size=100, ...)
```

**Arguments**

object	an object of class "ssr" fitted with a single smoothing parameter.
simu.size	an optional integer giving the number of simulations to calculate p-values based on simulation. Default is 100.
...	other available arguments, currently unused.

**Details**

For Gaussian data with one smoothing parameter, test the hypothesis that the function is in the null space  $H_0$ , i.e. the parametric part of the fitted model is sufficient. Available are the LMP and GCV or GML methods. However, the p-values cannot be calculated analytically since the null distributions for these testing statistics under  $H_0$  are unknown. Monte Carlo simulation is used to approximate the p-values for the LMP, and GCV (if `spar="v"`) or GML (if `spar="m"`) methods. Due to computation burden, the smoothing parameters are fixed at their estimate in the current calculation.

When `spar="m"`, an approximate p-value based on a mixture of two Chi-square distributions is also provided for the GML test, which tends to be conservative (Pinheiro and Bates, 2002).

Methods further developed in Liu and Wang (2004) and Liu, Meiring and Wang (2004) will be implemented in the future.

**Value**

a list including test values.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

Cox, D. and Koh, E. (1989). A smoothing spline based test of model adequacy in polynomial regression. *Ann. Ins. Stat. Math.* 41, 383-400.

Cox, D., Koh, E., Wahba, G. and Yandell, B.S. (1988). Testing the parametric null model hypothesis in semi-parametric partial and generalized spline models. *Ann. Statist.* 16, 113-119.

Wahba, G. (1990). *Spline Models for Observational Data*. SIAM, Vol. 59.

Pinheiro, J. C. and Bates, D. M. (2000) *Mixed-effects Models in S and S-Plus*. Springer.

Liu, A. and Wang, Y. (2004) Hypothesis Testing in Smoothing Spline Models. *Journal of Statistical Computation and Simulation*, to appear.

Liu, A., Meiring, W. and Wang, Y. (2004), Testing Generalized Linear Models Using Smoothing Spline Methods. *Statistica Sinica*, to appear.

**See Also**

[ssr](#), [print.anova.ssr](#)

**Examples**

```
## Not run:
data(acid)

# fit a partial thin-plate spline
temp <- ssr(ph~t1+x1+x2, rk=tp(t1), data=acid, spar="m")
anova(temp, 500)

## End(Not run)
```

---

Arosa

*Monthly Mean Ozone Thickness in Arosa of Switzerland*

---

**Description**

The Arosa data frame has 518 rows and 3 columns of data for monthly mean ozone thickness.

**Usage**

```
data(Arosa)
```

**Format**

The data frame contains the following columns:

year a vector of integers from 1 to 46 indicating the years when the measures were taken from 1926.

month a vector of integers from 1 to 12 representing the months in a year.

thick a numeric vector of mean ozone thickness (Dobson units).

**Details**

Monthly mean ozone thickness in Arosa, Switzerland was recorded from 1926-1971.

**Source**

Andrew, D. F. and Herzberg, A. M. (1985). Data: a collection of problems from many fields for the students and research workers. Springer: Berlin: New York.

---

`bdiag`*Construct a Block Diagonal Matrix*

---

**Description**

Return a block diagonal matrix formed from the input list of matrices

**Usage**`bdiag(x)`**Arguments**

`x` a list of matrices

**Value**

Returned is a matrix of the form  $\text{diag}(x_1, \dots, x_n)$  where  $n$  is the length of the list.

---

`bond`*Treasury and GE bonds*

---

**Description**

The bond data frame has 1234 rows and 5 columns of data derived from 144 General Electronic Company bonds and 78 Treasury bonds.

**Usage**`data(bond)`**Format**

The data frame contains the following columns:

`name` a vector of index for individual bond

`price` a numeric vector of current price

`time` a numeric vector of future time points at which the payments are made

`payment` a numeric vector of future payments

`type` a vector of character strings identifying the groups, "govt" or "ge", which the individual bonds belong to.

**Source**

Bloomberg

**references**

Chunlei Ke and Yuedong Wang (2004), Nonlinear Nonparametric Regression Models. Journal of the American Statistical Association 99, 1166-1175.

---

canadaTemp

*Monthly Mean Temperatures*

---

**Description**

The canadaTemp data frame has 420 rows and 3 columns of data for monthly mean temperatures in Canada

**Usage**

```
data(canadaTemp)
```

**Format**

The data frame contains the following columns:

temp a numeric vector of mean temperatures at some stations in Canada.

month a vector of integers from 1 to 12 representing the months in a year.

station a vector of integers from 1 to 35 indicating the stations where the temperatures were recorded.

**Source**

The data set was downloaded from <https://www.psych.mcgill.ca/misc/fda/downloads/FDAfuns/R/data/>.

**References**

Ramsay, J. O and Silverman, B. W. (1997). Functional Data Analysis. New York:Springer.

Ke, C. and Wang, Y. (2001). Semi-parametric Nonlinear Mixed Effects Models and Their Applications. JASA 96:1272-1298.

---

chickenpox	<i>Chickenpox in New York City</i>
------------	------------------------------------

---

**Description**

The chickenpox data frame has 498 rows and 3 columns of data recording the number of Chickenpox occurrences in New York City.

**Usage**

```
data(chickenpox)
```

**Format**

The data frame contains the following columns:

count the number of monthly reported Chickenpox cases.

month a vector of integers from 1 to 12 representing the month for the reported cases. year a numeric vector representing the year when the cases were reported.

**Details**

This data frame contains monthly number of reported cases of chickenpox in New York City from 1931 to the first six months of 1972.

**Source**

The data were downloaded from <https://robjhyndman.com/tsd1/>.

---

chol.new	<i>A Modified Cholesky Decomposition</i>
----------	--

---

**Description**

Returned a matrix forming Cholesky Decomposition

**Usage**

```
chol.new(Q)
```

**Arguments**

Q a symmetric matrix, maybe non-positive.

**Details**

This is used internally as an extension of chol that works on a positive matrix.

**Value**

A matrix  $M$  such that  $XX^T = Q$ .

**See Also**

[chol](#)

---

climate

*Winter Average Temperatures*

---

**Description**

The data frame `climate`, obtained from the Carbon Dioxide Information and Analysis Center, has 690 rows and 5 columns of data representing station winter temperature measurements.

**Usage**

```
data(climate)
```

**Format**

The data frame contains the following columns:

`temp` a numeric vector of temperatures in celsius.

`lat`, long numeric vectors identifying the latitudes and longitudes of the stations in.

`lat.degree`, `long.degree` numeric vectors identifying the latitudes and longitudes of the stations in degree.

**Details**

The station winter average temperatures were the averages of the December, January and February monthly average temperatures obtained from the Jones/Wigley data files obtainable from the CDIAC at Oak Ridge National Laboratory in the files `ndp020r1/jonesnh.data.Z` and `ndp020r1/jonessh.dat.Z` in the `pbu` directory at 128.219.24.36.

**Source**

Jones, P., Wigley, T. and Briffa, K.. Global and hemisphere temperature anomalies-land and marine instrumental records. In T. Boden, D. Kaiser, R. Sepanski, and F. Stoss, editors, *Trends '93: A Compendium of Data on Global Change*, ORNL/CDIAC-65, pages 603-608, Oak Ridge, TN 1994. CDIAC, Oak Ridge National Laboratory.

---

dcrdr                      *Interface to Fortran Subroutine dcrdr*

---

**Description**

Calculate some matrix operations needed to construct Bayesian confidence intervals

**Usage**

```
dcrdr(rkpk.obj, r)
```

**Arguments**

rkpk.obj	an object returned from calling dsidr
r	a matrix to evaluate reproducing kernels on grid points

**Value**

See the document for the corresponding Fortran subroutine.

---

deviance.ssr                      *Model Deviance*

---

**Description**

Extract deviance from a fitted ssr object

**Usage**

```
## S3 method for class 'ssr'
deviance(object,residuals=FALSE, ...)
```

**Arguments**

object	a fitted ssr object
.	
residuals	a logical value. If 'TRUE', deviance residuals are returned. If 'FALSE', the sum of deviance residuals squares is returned. Default is FALSE.
...	other arguments, currently unused.

**Details**

This is a method for the function deviance for objects inheriting from class ssr.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[ssr](#)

---

dmudr

*Interface of dmudr subroutine in RKPACk*

---

**Description**

To calculate a spline estimate with multiple smoothing parameters

**Usage**

```
dmudr(y, q, s, weight = NULL, vmu = "v", theta = NULL, varht = NULL,
      tol = 0, init = 0, prec = 1e-06, maxit = 30)
```

**Arguments**

y	a numerical vector representing the response.
q	a list, or an array, of square matrices of the same order as the length of y, which are the reproducing kernels evaluated at the design points.
s	the design matrix of the null space $H_0$ of size $(\text{length-of-}y, \text{dim}(H_0))$ , with elements equal to the bases of $H_0$ evaluated at design points.
weight	a weight matrix for penalized weighted least-square: $(y - f)'W(y - f) + n\lambda J(f)$ . Default is NULL for iid random errors.
vmu	a character string specifying a method for choosing the smoothing parameter. "v", "m" and "u" represent GCV, GML and UBR respectively. "u~", only used for non-Gaussian family, specifies UBR with estimated variance. Default is "v".
theta	If 'init=1', theta includes initial values for smoothing parameters. Default is NULL.
varht	needed only when vmu="u", which gives the fixed variance in calculation of the UBR function. Default is NULL.
tol	the tolerance for truncation in the tridiagonalization. Default is 0.0.
init	an integer of 0 or 1 indicating if initial values are provided for theta. If init=1, initial values are provided using theta. Default is 0.
prec	precision requested for the minimum score value, where precision is the weaker of the absolute and relative precisions. Default is $1e - 06$ .
maxit	maximum number of iterations allowed. Default is 30.

**Value**

info	an integer that provides error message. info=-1 indicates dimension error, info=-2 indicates $F_2^T Q_*^\theta F_2! \geq 0$ , info=-3 indicates tuning parameters are out of scope, info=-4 indicates fails to converge within maxite steps, info=-5 indicates fails to find a reasonable descent direction, info>0 indicates the matrix S is rank deficient with $info = rank(S) + 1$ .
fit	fitted values.
c	estimates of c.
d	estimates of d.
resi	vector of residuals.
varht	estimate of variance.
theta	estimates of parameters $\log_{10}(\theta)$ .
nlaht	the estimate of $\log_{10}(nobs * \lambda)$ .
score	the minimum GCV/GML/UBR score at the estimated smoothing parameters.
df	equivalent degree of freedom.
nobs	length(y), number of observations.
nnull	$\dim(H_0)$ , number of bases.
nq	length(rk), number of reproducing kernels.
s, q, y	changed from the inputs.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

- Gu, C. (1989). RKPACk and its applications: Fitting smoothing spline models. Proceedings of the Statistical Computing Section, ASA, 42-51.
- Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59

**See Also**

[dsidr](#), [gdsidr](#), [gdmudr](#), [ssr](#)

---

dog

*Coronary Ainus Potassium Concentrations*

---

**Description**

The dog data frame has 252 rows and 4 columns of data considered by Grizzle and Alen (1969)

**Usage**

```
data(dog)
```

**Format**

The data frame contains the following columns:

y a numeric vector of measurements of coronary sinus potassium concentrations.

group a vector of group index for the four groups of dogs.

dog a vector of integers identifying dogs.

time a numeric vector of time points measurements were made.

**Details**

The data are coronary sinus potassium concentrations measured on each of 36 dogs. These 36 dogs were divided into 4 treatment groups, and the measurements on each dog were taken every two minutes from 1 to 13 minutes after occlusion.

**Source**

Grizzle, J. E. and Allen, D. M. (1969). Analysis of growth and dose response curves, *Biometrics* 25: 357-381.

---

dsidr

*Interface of dsidr subroutines in RKPACK*

---

**Description**

To calculate a spline estimate with a single smoothing parameter

**Usage**

```
dsidr(y, q, s=NULL, weight=NULL, vmu="v", varht=NULL,  
limnla=c(-10, 3), job=-1, tol=0)
```

**Arguments**

y	a numerical vector representing the response.
q	a square matrix of the same order as the length of y, with elements equal to the reproducing kernel evaluated at the design points.
s	the design matrix of the null space $H_0$ of size $(\text{length}(y), \text{dim}(H_0))$ , with elements equal to the bases of $H_0$ evaluated at design points. Default is NULL, representing an empty NULL space.
weight	A weight matrix for penalized weighted least-square: $(y - f)'W(y - f) + n\lambda J(f)$ . Default is NULL for iid random errors.
vmu	a character string specifying a method for choosing the smoothing parameter. "v", "m" and "u" represent GCV, GML and UBR respectively. "u~", only used for non-Gaussian family, specifies UBR with estimated variance. Default is "v".
varht	needed only when vmu="u", which gives the fixed variance in calculation of the UBR function. Default is NULL.
limnla	a vector of length 2, specifying a search range for the n times smoothing parameter on $\log_{10}$ scale. Default is $(-10, 3)$ .
job	an integer representing the optimization method used to find the smoothing parameter. The options are job=-1: golden-section search on $(\text{limnla}(1), \text{limnla}(2))$ ; job=0: golden-section search with interval specified automatically; job >0: regular grid search on $[\text{limnla}(1), \text{limnla}(2)]$ with the number of grids = job + 1. Default is -1.
tol	tolerance for truncation used in 'dsidr'. Default is 0.0, which sets to square of machine precision.

**Value**

info	an integer that provides error message. info=0 indicates normal termination, info=-1 indicates dimension error, info=-2 indicates $F_2^T Q F_2! \geq 0$ , info=-3 indicates vmu is out of scope, and info>0 indicates the matrix S is rank deficient with $\text{info}=\text{rank}(S)+1$ .
fit	fitted values.
c	estimates of c.
d	estimates of d.
resi	vector of residuals.
varht	estimate of variance.
nlaht	the estimate of $\log_{10}(\text{nobs}*\lambda)$ .
limnla	searching range for nlaht.
score	the minimum GCV/GML/UBR score at the estimated smoothing parameter. When job>0, it gives a vector of GCV/GML/UBR functions evaluated at regular grid points.
df	equivalent degree of freedom.
nobs	$\text{length}(y)$ , number of observations.

nnull	$\dim(H_0)$ , number of bases.
s, qraux, jpvt	QR decomposition of $S=FR$ , as from Linpack 'dqrdc'.
q	first $\dim(H_0)$ columns gives $F^T Q F_1$ , and its bottom-right corner gives tridiagonalization of $F_2^T Q F_2$ .

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

Gu, C. (1989). RKPACk and its applications: Fitting smoothing spline models. Proceedings of the Statistical Computing Section, ASA, 42-51.

Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.

**See Also**

[dmudr](#), [gdsidr](#), [gdmudr](#), [ssr](#)

---

dsms

*Interface to Fortran Subroutine dsms*

---

**Description**

Calculate a matrix operation needed to construct Bayesian confidence intervals

**Usage**

dsms(rkpk.obj)

**Arguments**

rkpk.obj            an object returned from calling dsidr

**Value**

a matrix. See the corresponding Fortran subroutine.

gdmudr

*Interface of dbmdr, dbimdr, dgmdr, dpmdr in GRKPACK.***Description**

To calculate a spline estimate with multiple smoothing parameters for non-Gaussian data

**Usage**

```
gdmudr(y, q, s, family, vmu = "v", varht = NULL,
       init = 0, theta = NULL, tol1 = 0, tol2 = 0, prec1 = 1e-06,
       maxit1 = 30, prec2 = 1e-06, maxit2 = 30)
```

**Arguments**

y	a numerical vector representing the response, or a matrix of two columns for binomial data with the first column as the largest possible counts and the second column as the counts actually obsered.
q	a list, or an array, of square matrices of the same order as the length of y, which are the reproducing kernels evaluated at the design points.
s	the design matrix of the null space $H_0$ of size (length-of-y, $\dim(H_0)$ ), with elements equal to the bases of $H_0$ evaluated at design points.
family	a string specifying the family of distribution. Families supported are "binary", "binomial", "poisson" and "gamma" for Bernoulli, binomial, poisson, and gamma distributions respectively. Canonical links are used except for Gamma family where log link is used.
vmu	a character string specifying a method for choosing the smoothing parameter. "v", "m" and "u" represent GCV, GML and UBR respectively. "u~", only used for non-Gaussian family, specifies UBR with estimated variance. Default is "v".
varht	needed only when vmu="u", which gives the fixed variance in calculation of the UBR function. Default is 1.0.
init	an integer of 0 or 1 indicating if initial values are provided for theta. If init=1, initial values are provided using theta. Default is 0.
theta	If 'init=1', theta includes intial values for smoothing parameters. Default is NULL.
tol1	the tolerance for elements of w's. Default is 0.0 which sets to square of machine precision.
tol2	tolerance for truncation used in 'dsidr'. Default is 0.0 which sets to square of machine precision.
prec1	precision requested for the minimum score value, where precision is the weaker of the absolute and relative precisions. Default is 1e-06.
maxit1	maximum number of iterations allowed for DMUDR subroutine. Default is 30.
prec2	precision requested for stopping the iteration. Default is $1e - 06$ .
maxit2	maximum number of iterations allowed for the iteration in GRKPACK. Default is 30.

**Value**

info	an integer that provides error message. info=-1 indicates dimension error, info=-2 indicates $F_2^T Q_*^{theta} F_2 \geq 0$ , info=-3 indicates tuning parameters are out of scope, info=-4 indicates dmudr fails to converge within maxit1 steps, info=-5 indicates dmudr fails to find a reasonable descent direction, info=-6 indicates GRKPACK fails to converge within maxit2 steps, info=-7 indicates there are some w's equals to zero, info>0 indicates the matrix S is rank deficient with $info = rank(S) + 1$ .
fit	estimate of the function at design points.
c	estimates of c.
d	estimates of d.
resi	vector of working residuals.
varht	estimate of dispersion parameter.
theta	estimates of parameters $\log_{10}(theta)$ .
nlaht	the estimate of $\log_{10}(nobs * lambda)$ .
score	the minimum GCV/GML/UBR score at the estimated smoothing parameters.
df	equivalent degree of freedom.
nobs	length-of-y, number of observations.
nnull	$dim(H_0)$ , number of bases.
nq	length(rk), number of reproducing kernels.
s, q, y, init, maxit2	changed from the inputs.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

- Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.
- Wang, Y. (1997). GRKPACK: Fitting Smoothing Spline ANOVA Models for Exponential Families. Communications in Statistics: Simulation and Computation, 24: 1037-1059.

**See Also**

[dsidr](#), [dmudr](#), [gdsidr](#), [ssr](#)

gdsidr

*Interface of dbsdr, dbisdr, dgsdr, dpsdr in GRKPACK.***Description**

To calculate a spline estimate with single smoothing parameter for non-Gaussian data.

**Usage**

```
gdsidr(y, q, s, family, vmu="v", varht=NULL, limnla=c(-10, 3),
maxit=30, job=-1, tol1=0, tol2=0, prec=1e-06)
```

**Arguments**

y	a numerical vector representing the response, or a matrix of two columns for binomial data with the first column as the largest possible counts and the second column as the counts actually observed.
q	a square matrix of the same order as the length of y, with elements equal to the reproducing kernel evaluated at the design points.
s	the design matrix of the null space $H_0$ of size (length-of-y,dim( $H_0$ )), with elements equal to the bases of $H_0$ evaluated at design points.
family	a string specifying the family of distribution. Families supported are "binary", "binomial", "poisson" and "gamma" for Bernoulli, binomial, poisson, and gamma distributions respectively. Canonical links are used except for Gamma family where a log link is used.
vmu	a character string specifying a method for choosing the smoothing parameter. "v", "m" and "u" represent GCV, GML and UBR respectively. "u~", only used for non-Gaussian family, specifies UBR with estimated variance. Default is "v".
varht	needed only when vmu="u", which gives the fixed variance in calculation of the UBR function. Default is 1.0.
limnla	a vector of length 2, specifying a search range for the n times smoothing parameter on log10 scale. Default is (-10, 3).
maxit	maximum number of iterations allowed for the iteration in GRKPACK.
job	an integer representing the optimization method used to find the smoothing parameter. The options are job=-1: golden-section search on (limnla(1), limnla(2)); job=0: golden-section search with interval specified automatically; job >0: regular grid search on [limnla(1), limnla(2)] with the number of grids = job + 1. Default is -1.
tol1	the tolerance for elements of w's. Default is 0.0 which sets to square of machine precision.
tol2	tolerance for truncation used in 'dsidr'. Default is 0.0 which sets to square of machine precision.
prec	precision requested for stopping the iteration. Default is $1e - 06$ .

**Value**

info	an integer that provides error message. info=0 indicates normal termination, info=-1 indicates dimension error, info=-2 indicates $F_2^T Q F_2 \leq 0$ , info=-3 indicates vmu is out of scope, info=-4 indicates the algorithm fails to converge at the maxiter steps, info=-5 indicates there are some w's equals to zero, and info>0 indicates the matrix S is rank deficient with info=rank(S)+1.
fit	estimate of the function at design points.
c	estimates of c.
d	estimates of d.
resi	vector of working residuals.
varht	estimate of dispersion parameter.
nlaht	the estimate of $\log_{10}(nobs * lambda)$ .
limnla	searching range for nlaht.
score	the minimum GCV/GML/UBR score at the estimated smoothing parameter. When job>0, it gives a vector of GCV/GML/UBR functions evaluated at regular grid points.
df	equivalent degree of freedom.
nobs	length-of-y, number of observations.
nnull	$dim(H_0)$ , number of bases.
s, qraux, jpvt	QR decomposition of S=FR, as from Linpack 'dqrdc'.
q	first $dim(H_0)$ columns gives $F^T Q F_1$ , and its bottom-right corner gives tridiagonalization of $F_2^T Q F_2$ .

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

- Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.
- Wang, Y. (1997). GRKPACK: Fitting Smoothing Spline ANOVA Models for Exponential Families. Communications in Statistics: Simulation and Computation, 24: 1037-1059.

**See Also**

[dsidr](#), [dmudr](#), [gdmudr](#), [ssr](#)

---

`hat.ssr`*Extract the Hat Matrix from a ssr Object*

---

**Description**

Calculate the hat matrix for a ssr object.

**Usage**

```
hat.ssr(ssr.obj)
```

**Arguments**

`ssr.obj` a fitted ssr object.

**Details**

The hat matrix may be used for diagnosis. Note that the full name `hat.ssr` should be used since the function `hat` already exist.

**Value**

returned is the hat (influence, smoother) matrix.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

Eubank, R. L. (1984). The Hat Matrix for Smoothing Splines. *Statistics and Probability Letters*, 2:9-14.

Eubank, R. L. (1985). Diagnostics for Smoothing Splines. *Journal of the Royal Statistical Society B*, 47: 332-341.

Wahba, G. (1990). *Spline Models for Observational Data*. SIAM, Vol. 59.

**See Also**

[ssr](#)

**Examples**

```
## Not run: library(MASS)
## Not run: fit1<- ssr(accel~times, data=mcycle, scale=T, rk=cubic(times))
## Not run: h <- hat.ssr(fit1)
```

---

`horm.cort`*Hormone Measurements of Cortisol*

---

**Description**

The `horm.cort` data frame has 425 rows and 4 columns of data representing measurement of cortisol on 36 individuals.

**Usage**

```
data(horm.cort)
```

**Format**

The data frame contains the following columns:

`ID` a vector of index indicating individuals on whom measures were made.

`time` a numeric vector of time points of every 2 hours in 24 hours. The time is scaled into  $[0, 1]$ .

`type` a vector of character strings identifying the groups, "normal", "depressed", or "cushing", which the individuals belong to.

`conc` cortisol concentration measurements in  $\log_{10}$  scale.

**Details**

Blood samples were collected every 2 hours for 24 hours from three group of healthy normal volunteers and volunteers with depression and suchsing syndrome. They were analyzed for parameters that measure hormones of the hypothalamic-pituitary axis. Human circadian rhythm is one of the research objective. In this data set, only measurements of cortisol concetration were included.

**Source**

This data set was extracted from a stress study conducted in the medical center of the University of Michigan.

**References**

Wang, Y. and Brown, M. B. (1996). A Flexible Model for Human Circadian Rhythms. *Biometrics* 52, 588-596.

Yuedong Wang, Chunlei Ke and Morton B. Brown (2003), Shape Invariant Modelling of Circadian Rhythms with Random Effects and Smoothing Spline ANOVA Decompositions. *Biometrics*, 59:804-812.

---

 ident

*Scaling a Vector*


---

**Description**

Perform standarization of vector relative to another.

**Usage**

```
ident(x, y = x)
```

**Arguments**

x a numeric vector, matrix or data frame  
 y an optional numeric vector, matrix or data frame. Default is x.

**Details**

Scale y based on x component by component. For example, if both are a matrix,  $y[,i] = (y[,i] - \min(x[,i])) / (\max(x[,i]) - \min(x[,i]))$ .

**Value**

a scaled y.

---

inc

*Fit a Monotone Curve Using a Cubic Spline*


---

**Description**

Return a spline fit of a increasing curve.

**Usage**

```
inc(y, x, spar = "v", limnla = c(-6, 0), grid = x, prec = 1e-06, maxit = 50, verbose = F)
```

**Arguments**

y a vecetor, used as the response data  
 x a vector, used as the covariate. Assume an increasing relationship of y on x  
 spar a character string specifying a method for choosing the smoothing parameter. "v", "m" and "u" represent GCV, GML and UBR respectively. Default is "v" for GCV

limnla	a vector of length one or two, specifying a search range for $\log_{10}(n*\lambda)$ , where $\lambda$ is the smoothing parameter and $n$ is the sample size. If it is a single value, the smoothing parameter will be fixed at this value.
grid	a vector of $x$ used to assess convergence. Default is $x$
prec	a numeric value used to assess convergence. Default is $1e-6$
maxit	an integer representing the maximum iterations. Default is 50.
verbose	an optional logical value. If 'TRUE', detailed iteration results are displayed. Default is "FALSE"

### Details

This function is to fit a increasing function to the data. The monotone function is expressed as integral of an unknown function that a cubic spline is used to estimate.

### Value

a split fit together with the convergence information

### Author(s)

Yuedong Wang <yuedong@pstat.ucsb.edu> and Chunlei Ke <chunlei\_ke@yahoo.com>

### See Also

ssr

---

intervals.nnr	<i>Calculate Predictions and Approximate Posterior Standard Deviations for Spline Estimates From a nnr Object</i>
---------------	---

---

### Description

Approximate posterior standard deviations are calculated for the spline estimate of nonparametric functions from a nnr object, based on which approximate Bayesian confidence intervals may be constructed.

### Usage

```
## S3 method for class 'nnr'
intervals(object, level=0.95, newdata=NULL, terms, pstd=TRUE, ...)
```

**Arguments**

object	an object inheriting from class <code>nnr</code> , representing a nonlinear nonparametric regression model fit.
newdata	a data frame on which the fitted spline estimates are to be evaluated. Only those predictors, referred in <code>func</code> of <code>nnr</code> fitting, have to be present. The variable names of the data frame should correspond to the function(s)' arguments appearing in the option <code>func=</code> of <code>nnr</code> . Default is <code>NULL</code> , where predictions are made at the same values used to fit the object.
terms	an optional named list of vectors or matrices containing 0's and 1's collecting one or several combinations of the components of spline estimates in the fitted <code>snr</code> object. The length and names of the list shall match those of the unknown functions appearing in the 'snr' fit object. For the case of a single function, a vector of 0's and 1's can also be accepted. A value "1" at a particular position means that the component at that position is collected. Default is a vector of 1's, representing the overall fits of all unknown functions.
pstd	an optional logic value. If <code>TRUE</code> (the default), the posterior standard deviations are calculated. Orelse, only the predictions are calculated. Computation required for posterior standard deviations could be intensive.
level	a numeric value set as 0.95.
...	other arguments, currently unused.

**Details**

The standard deviation returned is based on approximate Bayesian confidence intervals as formulated in Ke and Wang (2002).

**Value**

an object of class `bCI` is returned, which is a list of length 2. Its first element is a matrix which contains predictions for combinations specified by `terms`, and second element is a matrix which contains corresponding posterior standard deviations.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

Ke, C. and Wang, Y. (2002). Nonlinear Nonparametric Regression Models. Submitted.

**See Also**

[nnr](#), [plot.bCI](#)

**Examples**

```
## Not run:
## fit a generalized varying coefficient models
data(Arosa)
Arosa$csmoonth <- (Arosa$month-0.5)/12
Arosa$csyear <- (Arosa$year-1)/45
ozone.fit <- nnr(thick~f1(csyear)+exp(f2(csyear))*f3(csmoonth),
  func=list(f1(x)~list(~I(x-.5),cubic(x)), f2(x)~list(~I(x-.5)-1,cubic(x)),
    f3(x)~list(~sin(2*pi*x)+cos(2*pi*x)-1,lspline(x,type="sine0"))),
  data=Arosa[Arosa$year%%2==1,], spar="m", start=list(f1=mean(thick),f2=0,f3=sin(csmoonth)),
  control=list(backfit=1))

x <- seq(0,1,len=50)
u <- seq(0,1,len=50)

## calculate Bayesian confidence limits for all components of all functions
p.ozone.fit <- intervals(ozone.fit, newdata=list(csyear=x,csmoonth=u),
  terms=list(f1=matrix(c(1,1,1,1,1,0,0,0,1),nrow=3,byrow=TRUE),
    f2=matrix(c(1,1,1,0,0,1),nrow=3,byrow=TRUE),
    f3=matrix(c(1,1,1,1,1,0,0,0,1),nrow=3,byrow=TRUE)))
plot(p.ozone.fit, x.val=x)

## End(Not run)
```

intervals.slm

*Calculate Predictions and Posterior Standard Deviations of Spline Estimates From a slm Object*

**Description**

Provide a way to calculate approximate posterior standard deviations and fitted values at any specified values for any combinations of elements of the spline estimate of nonparametric functions from a slm object, based on which approximate Bayesian confidence intervals may be constructed.

**Usage**

```
## S3 method for class 'slm'
intervals(object, level=0.95, newdata=NULL, terms, pstd=TRUE, ...)
```

**Arguments**

object	an object inheriting from class "slm", representing a semi-parametric nonlinear regression model fit.
level	set as 0.95, unused currently
newdata	an optional data frame on which the fitted spline estimate is to be evaluated.

terms	an optional vector of 0's and 1's collecting a combination of components, or a matrix of 0's and 1's collecting several combinations of components, in a fitted <code>ssr</code> object. All components include bases on the right side of <code>~</code> in the formula and reproducing kernels in the <code>rk</code> list. Note that the first component is usually a constant function if it is not specifically excluded in the formula. A value "1" at a particular position means that the component at that position is collected. Default is a vector of 1's, representing the overall fit.
pstd	an optional logic value. If TRUE (the default), the posterior standard deviations are calculated. Orelse, only the predictions are calculated. Computation required for posterior standard deviations could be intensive.
...	other arguments, currently unused.

### Details

The standard deviation returned is based on approximate Bayesian confidence intervals as formulated in Wang (1998).

### Value

an object of class `bCI` is returned, which is a list of length 2. Its first element is a matrix which contains predictions for combinations specified by `terms`, and second element is a matrix which contains corresponding posterior standard deviations.

### Author(s)

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

### References

Wang, Y. (1998). Mixed-effects smoothing spline ANOVA. *Journal of the Royal Statistical Society, Series B* 60, 159-174.

### See Also

[slm](#), [plot.bCI](#), [predict.ssr](#)

### Examples

```
## Not run:
data(dog)
# fit a SLM model with random effects for dogs
dog.fit<-slm(y~group*time, rk=list(cubic(time), shrink1(group),
  rk.prod(kron(time-0.5),shrink1(group)),rk.prod(cubic(time),
  shrink1(group))), random=list(dog=~1), data=dog)

intervals(dog.fit)

## End(Not run)
```

---

intervals.snm	<i>Calculate Predictions and Approximate Posterior Standard Deviations for Spline Estimate From a snm Object</i>
---------------	--

---

### Description

Provide a way to calculate approximate posterior standard deviations and fitted values at any specified values for any combinations of elements of the spline estimate of nonparametric functions from a snm object, based on which approximate Bayesian confidence intervals may be constructed.

### Usage

```
## S3 method for class 'snm'
intervals(object, level=0.95, newdata=NULL, terms, pstd=TRUE, ...)
```

### Arguments

object	an object inheriting from class snm, representing a semi-parametric nonlinear mixed effects model fit.
newdata	a data frame on which the fitted spline estimates are to be evaluated. Only those predictors, referred in 'func' of 'snm' fitting, have to be present. The variable names of the data frame should correspond to the function(s)' arguments appearing in the option func= of snm. Default is NULL, where predictions are made at the same values used to fit the object.
terms	an optional vector of 0's and 1's collecting a combination of components, or a matrix of 0's and 1's collecting several combinations of components of spline estimates in a fitted snm object. Note that in the cases of multiple functions, the order of all componets is collection of base functions for all functions followed by RK's. A value "1" at a particular position means that the component at that position is collected. Default is a vector of 1's, representing the overall fit.
pstd	an optional logic value. If TRUE (the default), approximate posterior standard deviations are calculated. Orelse, only the predictions are calculated. Computation required for posterior standard deviations could be intensive.
level	a numeric value set as 0.95.
...	other arguments, currently unused.

### Details

The standard deviation returned is based on approximate Bayesian confidence intervals as formulated in Ke and Wang (2001).

### Value

an object of class bCI is returned, which is a list of length 2. Its first element is a matrix which contains predictions for combinations specified by "terms", and second element is a matrix which contains corresponding posterior standard deviations.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>.

**References**

Ke, C. and Wang, Y. (2001). Semi-parametric Nonlinear Mixed Effects Models and Their Applications. JASA 96:1272-1298.

**See Also**

[snm](#), [plot.bCI](#), [predict.ssr](#)

**Examples**

```
## Not run:
data(horm.cort)

## extract normal subjects
cort.nor<- horm.cort[horm.cort$type=="normal",]

## fit a self-modelling model with random effects
cort.fit<- snm(conc~b1+exp(b2)*f(time-alogit(b3)),
  func=f(u)~list(periodic(u)), fixed=list(b1~1),
  random=pdDiag(b1+b2+b3~1), data=cort.nor,
  groups= ~ID,start=mean(cort.nor$conc))

## note the variable name of newdata
intervals(cort.fit, newdata=data.frame(u=seq(0,1,len=50)))

## End(Not run)
```

---

intervals.snr

*Calculate Predictions and Approximate Posterior Standard Deviations  
for Spline Estimates From a snr Object*

---

**Description**

Approximate posterior standard deviations are calculated for the spline estimate of nonparametric functions from a snr object, based on which approximate Bayesian confidence intervals may be constructed.

**Usage**

```
## S3 method for class 'snr'
intervals(object, level=0.95,newdata=NULL, terms=list(), pstd=TRUE, ...)
```

**Arguments**

object	an object inheriting from class 'snr', representing a semi-parametric nonlinear regression model fit.
level	set as 0.95, unused currently
newdata	a data frame on which the fitted spline estimates are to be evaluated. Only those predictors, referred in 'func' of 'snr' fitting, have to be present. The variable names of the data frame should correspond to the function(s)' arguments appearing in the option func= of snr. Default is NULL, where predictions are made at the same values used to fit the object.
terms	an optional named list of vectors or matrices containing 0's and 1's collecting one or several combinations of the components of spline estimates in the fitted snr object. The length and names of the list shall match those of the unknown functions appearing in the 'snr' fit object. For the case of a single function, a vector of 0's and 1's can also be accepted. A value "1" at a particular position means that the component at that position is collected. Default is a vector of 1's, representing the overall fits of all unknown functions.
pstd	an optional logic value. If TRUE (the default), the posterior standard deviations are calculated. Orelse, only the predictions are calculated. Computation required for posterior standard deviations could be intensive.
...	other arguments, currently unused.

**Details**

The standard deviation returned is based on approximate Bayesian confidence intervals as formulated in Ke (2000).

**Value**

a named list of objects of class "bCI" is returned, each component of which is a list of length 2. Within each component, the first element is a matrix which contains predictions for combinations specified by "terms", and the second element is a matrix which contains corresponding posterior standard deviations.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

Ke, C. (2000). Semi-parametric Nonlinear Regression and Mixed Effects Models. PhD thesis, University of California, Santa Barbara.

**See Also**

[snr](#), [plot.bCI](#), [predict.ssr](#)

**Examples**

```
## Not run:
data(CO2)
options(contrasts=rep("contr.treatment", 2))

## get start values
co2.fit1 <- nlme(uptake~exp(a1)*(1-exp(-exp(a2)*(conc-a3))),
               fixed=list(a1+a2~Type*Treatment,a3~1),
               random=a1~1, groups=~Plant,
               start=c(log(30),0,0,0,log(0.01),0,0,0,50),
               data=CO2)

M <- model.matrix(~Type*Treatment, data=CO2)[,-1]

## fit a SNR model
co2.fit2 <- snr(uptake~exp(a1)*f(exp(a2)*(conc-a3)),
               func=f(u)~list(~I(1-exp(-u))-1,lspline(u, type="exp")),
               params=list(a1~M-1, a3~1, a2~Type*Treatment),
               start=list(params=co2.fit1$coe$fixed[c(2:4,9,5:8)]), data=CO2)

p.co2.fit2<- intervals(co2.fit2, newdata=data.frame(u=seq(0,10,len=50)))

## End(Not run)
```

---

kron

*Calculate reproducing kernels for one-dimensional space*


---

**Description**

Return a matrix evaluating reproducing kernels for the one-dimensional space usually spanned by a vector

**Usage**

```
kron(x,y=x)
```

**Arguments**

x            a vector or a list of numerical values which spans the one-dimensional space.  
y            a vector or a list of numerical values. Default is x.

**Value**

a matrix with the numbers of row and column equal to the length of x and y respectively. The [i, j] element is the reproducing kernel evaluated at the ith element of x and jth element of y.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**[kronecker,ssr](#)**Examples**

```
## Not run:
x<-runif(10)
kron(x)

## End(Not run)
```

lspline

*Calculate Reproducing Kernels for Some L-splines***Description**

Return a matrix evaluating reproducing kernels for some L-splines at observed points.

**Usage**

```
lspline(x,y=x, type="exp", ...)
```

**Arguments**

x	a numeric vector on which reproducing kernels are evaluated.
y	an optional vector, specifying the second argument of reproducing kernels. Default is x.
type	a string indicating the type of L-splines. Available options are "exp", "logit", "sine", "sine1", and "linSinCos". Default is "exp".
...	other arguments needed.

**Details**

Denote  $L$  as the differential operator,  $H_0$  as the null (kernel) space. The available kernels correspond to the following  $L$ :

- exp:  $L = rD + D^2$ ,  $H_0 = \text{span}\{1, \exp(-rx)\}$ .  $r > 0$ , default to be 1;
- logit:  $L = D - 1/(1 + e^t)$ ,  $H_0 = \text{span}\{e^t/(1 + e^t)\}$ ;
- sine0:  $L = D^2 + (2\pi)^2$ ,  $H_0 = \text{span}\{\sin(2\pi x), \cos(2\pi x)\}$ ;
- sine1:  $L = D(D^2 + (2\pi)^2)$ ,  $H_0 = \text{span}\{1, \sin(2\pi x), \cos(2\pi x)\}$ ;
- linSinCos:  $L = D^4 + D^2$ ,  $H_0 = \text{span}\{1, x, \sin(x), \cos(x)\}$ .

**Value**

a matrix with the numbers of row and column equal to the lengths of  $x$  and  $y$  respectively. The  $[i, j]$  element is the reproducing kernel evaluated at  $(x[i], y[j])$ .

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.

Heckman, N and Ramsay, J. O. (2000). Penalised regression with model-based penalties. To appear in Canadian Journal of Statistics.

**See Also**

[ssr](#)

**Examples**

```
## Not run:
x<- seq(0,1, len=20)
lspline(x, type="exp", r=1.5)

## End(Not run)
```

---

 nnr

---

*Nonlinear Non-parametric Regression*


---

**Description**

Fit a nonlinear nonparametric regression models with spline smoothing based on extended Gauss-Newton/Newton-Raphson and backfitting.

**Usage**

```
nnr(formula, func, spar="v", data=list(),
     start=list(), verbose=FALSE, control=list())
```

**Arguments**

formula	a model formula, with the response on the left of a $\sim$ operator and on the right an expression representing the mean function with a nonparametric function appearing with a symbol, e.g. $f$ .
---------	---

func	a required formula specifying the spline components necessary to estimate the non-parametric function. On the left of a ~ operator is the unknown function symbol as well as its arguments, while the right side is a list of two components, an optional nb and a required rk. nb and rk are similar to formula and rk in <code>ssr</code> . A missing nb denotes an empty null space.
spar	a character string specifying a method for choosing the smoothing parameter. "v", "m" and "u" represent GCV, GML and UBR respectively. Default is "v" for GCV.
data	an optional data frame.
start	a list of vectors or expressions which input initial values for the unknown functions. If expressions, the argument(s) inside should be the same as in <code>func</code> . The length of <code>start</code> should be the same as the number of unknown functions. If named, the names of the list should match those in "func". If not named, the order of the list is taken as that appearing in "func".
verbose	an optional logical numerical value. If TRUE, information on the evolution of the iterative algorithm is printed. Default is FALSE.
control	an optional list of control values to be used. See <code>nnr.control</code> for details.

### Details

A nonlinear nonparametric model is fitted using the algorithms developed in Ke and Wang (2002).

### Value

an object of class `nnr` is returned, containing fitted values, fitted function values as well as other information used to assess the estimate.

### Author(s)

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>.

### References

Ke, C. and Wang, Y. (2002). Nonlinear Nonparametric Regression Models. Submitted.

### See Also

[nnr.control](#), [ssr](#), [print.nnr](#), [summary.nnr](#), [intervals.nnr](#)

### Examples

```
## Not run:
x<- 1:100/100
y<- exp(sin(2*pi*x))+0.3*rnorm(x)
fit<- nnr(y~exp(f(x)), func=list(f(u)~list(~u, cubic(u))), start=list(0))

## fit a generalized varying coefficient models
data(Arosa)
Arosa$csmnth <- (Arosa$month-0.5)/12
```

```

Arosa$csyear <- (Arosa$year-1)/45
ozone.vc.fit <- nnr(thick~f1(csyear)+exp(f2(csyear))*f3(csmonth),
  func=list(f1(x)~list(~I(x-.5),cubic(x)), f2(x)~list(~I(x-.5)-1,cubic(x)),
  f3(x)~list(~sin(2*pi*x)+cos(2*pi*x)-1,lspline(x,type="sine0"))),
  data=Arosa[Arosa$year%%2==1,], spar="m", start=list(f1=mean(thick),f2=0,f3=sin(csmonth)),
  control=list(backfit=1))

## End(Not run)

```

---

nnr.control

*Set Control Parameters for nnr*


---

### Description

Control parameters supplied in the function call replace the defaults to be used in calling nnr.

### Usage

```

nnr.control(job = -1, tol = 0, max.iter = 50, init = 0, limnla = c(-10,
  0), varht = NULL, theta = NULL, prec = 1e-06, maxit = 30,
  method = "NR", increment = 1e-04, backfit = 5, converg = "coef",
  toler = 0.001)

```

### Arguments

job	an integer representing the optimization method used to find the smoothing parameter. The options are job=-1: golden-section search on (limnla(1), limnla(2)); job=0: golden-section search with interval specified automatically; job >0: regular grid search on [limnla(1), limnla(2)] with the number of grids = job + 1. Default is -1.
tol	tolerance for truncation used in 'dsidr'. Default is 0.0, which sets to square of machine precision.
max.iter	maximum number of iterations allowed for the Gauss-Newton/Newton-Raphson iteration.
init	an integer of 0 or 1 indicating if initial values are provided for theta. If init=1, initial values are provided using theta. Default is 0.
limnla	a vector of length 2, specifying a search range for the n times smoothing parameter on log10 scale. Default is (-10, 0).
varht	needed only when vmu="u", which gives the fixed variance in calculation of the UBR function. Default is NULL.
theta	If 'init=1', theta includes initial values for smoothing parameters. Default is NULL.
prec	precision requested for the minimum score value, where precision is the weaker of the absolute and relative precisions. Default is 1e-06.
maxit	maximum number of iterations allowed. Default is 30.

method	a character string specifying a method for iterations, "GN" for Gauss-Newton and "NR" for Newton-Raphson. Default is "GN".
increment	specifies a small value as increment to calculate derivatives. Default is 1e-04.
backfit	an integer representing the number of backfitting iterations for multiple functions. Default is 5.
converg	an optional character, with possible values "coef" and "ortho", specifying the convergence criterion to be used. "coef" uses the change of estimate of parameters and functions to assess convergence, and "ortho" uses a criterion similar to the relative offset used in nls. Default is "coef".
toler	tolerance for convergence of the algorithm. Default is 0.001.

**Value**

returned is a list includes all re-seted control parameters.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[nnr](#), [dsidr](#), [dmudr](#)

**Examples**

```
## Not run:
## use Newton-Raphson
nnr.control(method="NR")

## End(Not run)
```

---

paramecium

*Growth of paramecium caudatum population*

---

**Description**

The 'paramecium' data frame has 25 rows and 2 columns of data from an experiment that grow paramecium caudatum

**Usage**

```
data(paramecium)
```

**Format**

The data frame contains the following columns:

day a numeric vector of days since the start of the experiment

density a numeric vector of mean number of individuals in 0.5 ml of medium of four different cultures started simultaneously

**Source**

Gause, G.F. (1934). *The Struggle for Existence*. Baltimore, MD: Williams & Wilkins.

**references**

Neal, D. (2004). *Introduction to Population Biology*. Cambridge University Press.

---

periodic	<i>Calculate Reproducing Kernels for Periodic Polynomial Splines with Period 1</i>
----------	--

---

**Description**

Return a matrix evaluating reproducing kernels for periodic polynomial splines at observed points.

**Usage**

```
periodic(s, t=s, order=2)
```

**Arguments**

s a numeric vector.

t an optional vector. Default is the same as s.

order an optional integer specifying the order of the polynomial spline. Default is 2 for the periodic cubic spline.

**Details**

The general formula of the reproducing kernel is sum of an infinite series, which is approximated by taking the first 50 terms. For the case of order=2, the close form is available and used.

**Value**

a matrix with the numbers of row and column equal to the lengths of s and t respectively. The [i, j] element is the reproducing kernel evaluated at (s[i], t[j]).

**References**

Wahba, G. (1990). *Spline Models for Observational Data*. SIAM, Vol. 59.

Gu, C. (2001). *Smoothing Spline ANOVA Modes*. Chapman and Hall.

**See Also**

[cubic](#), [lspline](#)

**Examples**

```
## Not run:
x<- seq(0, 1, len=100)
periodic(x, order=3)

## End(Not run)
```

---

plot.bCI

*Bayesian Confidence Interval Plot of a Smoothing Spline Fit*


---

**Description**

Create trellis plots of a nonparametric function fit together with its (approximate) 95% Bayesian confidence intervals from a `ssr/slm/snr/snm` object.

**Usage**

```
## S3 method for class 'bCI'
plot(x, x.val=NULL, type.name=NULL, ...)
```

**Arguments**

<code>x</code>	an object of class "bCI" containing point evaluation of the unknown function and/or corresponding posterior standard deviations.
<code>x.val</code>	an optional vector representing values of argument based on which the function is to evaluate.
<code>type.name</code>	an optional character vector specifying the names of fits.
<code>...</code>	options suitable for <code>xyplot</code> .

**Details**

This function is to visualize a spline fit by use of trellis graphic facility with Bayesian confidence intervals superposed. Multi-panel plots, based on `xyplot`, are suitable for SS ANOVA decomposition of a spline estimate.

**Author(s)**

Chunlei Ke <[chunlei\\_ke@yahoo.com](mailto:chunlei_ke@yahoo.com)> and Yuedong Wang <[yuedong@pstat.ucsb.edu](mailto:yuedong@pstat.ucsb.edu)>

**See Also**

[predict.ssr](#), [intervals.slm](#), [intervals.snr](#), [intervals.snm](#)

### Examples

```
## Not run:
x<- seq(0, 1, len=100)
y<- 2*sin(2*pi*x)+rnorm(x)*0.5

fit<- ssr(y~x, cubic(x))
p.fit<- predict(fit)
plot(p.fit)
plot(p.fit,type.name="fit")

## End(Not run)
```

---

plot.ssr

*Generate Diagnostic Plots for a ssr Object*

---

### Description

Creates a set of plots suitable for assessing a fitted smoothing spline model of class `ssr`.

### Usage

```
## S3 method for class 'ssr'
plot(x, ask=FALSE, ...)
```

### Arguments

<code>x</code>	a <code>ssr</code> object.
<code>ask</code>	if TRUE, <code>plot.ssr</code> operates in interactive mode.
<code>...</code>	Other options used for <code>plot</code> , currently inactive.

### Details

This function is a method for the generic function `plot` for class `ssr`. It can be invoked by calling `plot` for an object of the appropriate class, or directly by calling `plot.ssr` regardless of the class of the object.

An appropriate x-y plot is produced to display diagnostic plots. These can be one or all of the following choices:

- Estimate of function with CIs
- Residuals against Fitted values
- Response against Fitted values
- Normal QQplot of Residuals

The first plot of estimate of function with CIs is only useful for univariate smoothing spline fits.

When `ask=TRUE`, rather than produce each plot sequentially, `plot.ssr` displays a menu listing all the plots that can be produced. If the menu is not desired but a pause between plots is still wanted one must set `par(ask=TRUE)` before invoking this command with argument `ask=FALSE`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

plot, ssr, predict.ssr

**Examples**

```
## Not run: library(MASS)
## Not run: fit1<- ssr(accel~times, data=mcycle, scale=TRUE, rk=cubic(times))
## Not run: plot(fit1,ask=TRUE)
```

---

Polynomial

*Calculate Reproducing Kernels for Polynomial Splines on [0, 1]*

---

**Description**

Return a matrix evaluating reproducing kernels for polynomial splines at observed points.

**Usage**

```
linear(s, t=s)
cubic(s, t=s)
quintic(s, t=s)
septic(s, t=s)
```

**Arguments**

s a vector of values in [0, 1], at which the kernels are evaluated.  
t an optional vector in [0, 1]. Default is the same as s.

**Details**

The reproducing kernels implemented in these functions are based on Bernoulli functions with domain [0, 1].

**Value**

a matrix with the numbers of row and column equal to the lengths of s and t respectively. The [i, j] element is the reproducing kernel of linear, cubic, quintic, or septic spline evaluated at (s[i], t[j]).

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@ucsb.edu>

**References**

Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.

**See Also**

[ssr](#), [linear2](#), [cubic2](#), [quintic2](#), [septic2](#)

**Examples**

```
## Not run:  
x<-seq(0, 1, len=10)  
cubic(x)  
  
## End(Not run)
```

---

Polynomial2

*Calculate Reproducing Kernels for Polynomial Splines on  $[0, T]$*

---

**Description**

Return a matrix evaluating reproducing kernels for polynomial splines at observed points.

**Usage**

```
linear2(s, t=s)  
cubic2(s, t=s)  
quintic2(s, t=s)  
septic2(s, t=s)
```

**Arguments**

**s** a vector of non-negative values, at which the kernels are evaluated.  
**t** an optional non-negative vector. Default is the same as s.

**Details**

The reproducing kernels implemented in these functions are based on Green functions. The domain is  $[0, T]$ , where  $T$  is a given positive number.

**Value**

a matrix with the numbers of row and column equal to the length of  $s$  and  $t$  respectively. The  $[i, j]$  element is the reproducing kernel of linear, cubic, quintic, or septic spline evaluated at  $(s[i], t[j])$ .

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

## References

Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.

## See Also

[ssr](#), [linear](#), [cubic](#), [quintic](#), [septic](#)

## Examples

```
## Not run:  
x<- seq(0, 5, len=10)  
linear2(x)  
  
## End(Not run)
```

---

predict.slm

*Predict Method for Semiparametric Linear Mixed Effects Model Fits*

---

## Description

Predicted Values on different levels of random effects with the spline fit as part of fixed effects

## Usage

```
## S3 method for class 'slm'  
predict(object, newdata=NULL, ...)
```

## Arguments

object	an object inheriting from class <code>slm</code> , representing a semi-parametric linear mixed effects model fit.
newdata	a data frame containing the values at which predictions are required. Only those predictors, referred to in the right side of the formula in the object, need to be present by name in <code>newdata</code> . Default is <code>NULL</code> , where predictions are made at the same values used to compute the object.
...	other arguments, but currently unused.

## Value

returned is a data.frame with columns given by the predictions at different levels and the grouping factors. Note that the smooth part of the spline fit is regarded as fixed.

## Author(s)

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>.

**References**

- Wang, Y. (1998) Mixed Effects Smoothing Spline ANOVA. JRSS, Series B, 60:159–174.  
 Pinheiro, J. C. and Bates, D. M. (2000) Mixed-effects Models in S and S-Plus. Springer.

**See Also**

[slm](#)

**Examples**

```
## Not run:
data(dog)

dog.fit<-slm(y~group*time, rk=list(cubic(time), shrink1(group),
  rk.prod(kron(time-0.5),shrink1(group)),rk.prod(cubic(time),
  shrink1(group))), random=list(dog=~1), data=dog)

predict(dog.fit)

## End(Not run)
```

---

predict.snm

*Predictions from a Semiparametric Nonlinear Mixed Effects Model Fit*

---

**Description**

The predictions are obtained on a semiparametric nonlinear mixed effects model object by replacing the unknown functions and the unknown parameters with their estimates. Of note, only a population level of predictions is available.

**Usage**

```
## S3 method for class 'snm'
predict(object, newdata, ...)
```

**Arguments**

object	a fitted snm object.
newdata	a data frame containing the values at which predictions are required. Default are data used to fit the object.
...	other arguments, but currently unused.

**Details**

This function is a method for the generic function predict for class snm.

**Value**

a vector of prediction values, obtained by evaluating the model in the frame newdata

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.

Ke, C. and Wang, Y. (2001). Semi-parametric Nonlinear Mixed Effects Models and Their Applications. JASA.

**See Also**

[snm](#), [predict](#)

---

predict.snr

*Predict Method from a Semiparametric Nonlinear Regression Model Fit*

---

**Description**

The predictions on a semiparametric nonlinear regression model object are obtained by substituting the unknown functions together with unknown parameters with their estimates and evaluating the regression functional based on provided or default covariate values.

**Usage**

```
## S3 method for class 'snr'
predict(object, newdata, ...)
```

**Arguments**

object	a fitted snr object.
newdata	a data frame containing the values at which predictions are required. Default are NULL, where data used to produce the fit are to be taken.
...	other arguments, but currently unused.

**Details**

This function is a method for the generic function predict for class snr

**Value**

a vector of prediction values, obtained by evaluating the model in the frame newdata.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

- Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.  
 Ke, C. (2000). Semi-parametric Nonlinear Regression and Mixed Effects Models. PhD thesis, University of California, Santa Barbara.

**See Also**

[snr](#)

---

predict.ssr	<i>Calculate Predictions and Posterior Standard Deviations for a ssr Object</i>
-------------	---

---

**Description**

Provide a way to calculate predictions at any specified values for any combinations of elements in the fitted model. Posterior standard deviations may be used to construct Bayesian confidence intervals.

**Usage**

```
## S3 method for class 'ssr'
predict(object, newdata=NULL, terms, pstd=TRUE, ...)
```

**Arguments**

object	a fitted ssr object.
newdata	an optional data frame containing the values at which predictions are required. Default is NULL, where predictions are made at the same values used to compute the object. Note that if scale=T, the newdata is on the original scale before transformation.
terms	an optional vector of 0's and 1's collecting a combination of components, or a matrix of 0's and 1's collecting several combinations of components, in a fitted ssr object. All components include bases on the right side of ~ in the formula and reproducing kernels in the rk list. Note that the first component is usually a constant function if it is not specifically excluded in the formula. A value "1" at a particular position means that the component at that position is collected. Default is a vector of 1's, representing the overall fit.
pstd	an optional logic value. If TRUE (the default), the posterior standard deviations are calculated. Otherwise, only the predictions are calculated. Computation required for posterior standard deviations could be intensive.
...	other arguments, but currently unused.

**Details**

This function is a method for the generic function `predict` for class `ssr`. It can be used to construct Bayesian confidence intervals for any combinations of components in the fitted model.

**Value**

an object of class `bCI` is returned, which is a list of length 2. Its first element is a matrix which contains predictions for combinations specified by `terms`, and second element is a matrix which contains corresponding posterior standard deviations.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>.

**References**

Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.

**See Also**

[ssr](#), [plot.bCI](#)

**Examples**

```
## Not run:
data(acid)

# tp.pseudo calculates the pseudo kernel
acid.fit<- ssr( ph ~ t1 + x1 + x2, rk = list(tp.pseudo(t1),
      tp.pseudo(list(x1, x2))), spar = "m", data=acid)

# extract the main effect of t1
grid <- seq(min(acid$t1),max(acid$t1),length=100)
p <- predict(acid.fit,data.frame(t1=grid,x1=0,x2=0),
      terms=c(0,1,0,0,1,0))

# extract the main effect of (x1,x2)
grid <- expand.grid(x1=seq(min(acid$x1),max(acid$x1),length=20),
      x2=seq(min(acid$x2),max(acid$x2),length=20))
p <- predict(acid.fit,data.frame(t1=0,x1=grid$x1,x2=grid$x2),
      terms=c(0,0,1,1,0,1),pstd=FALSE)

## End(Not run)
```

---

print.anova.ssr      *Print an anova.ssr Object*

---

**Description**

Calculate and output p-values for tests available.

**Usage**

```
## S3 method for class 'anova.ssr'  
print(x, ...)
```

**Arguments**

x                    an object inheriting from class anova.ssr, generally obtained by applying the anova.ssr method to an ssr object.  
...                   other available arguments, currently unused.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[anova.ssr](#), [ssr](#)

---

print.nnr              *Print Values*

---

**Description**

Print the arguments of a 'nnr' object.

**Usage**

```
## S3 method for class 'nnr'  
print(x, ...)
```

**Arguments**

x                    a nnr object  
...                   unused argument

**Details**

This is a method for the function `print` for objects inheriting from class `nnr`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[nnr](#)

---

print.slm

*Print Values*

---

**Description**

Print the arguments of a slm object.

**Usage**

```
## S3 method for class 'slm'  
print(x, ...)
```

**Arguments**

x	a slm object
...	unused argument

**Details**

This is a method for the function `print` for objects inheriting from class `slm`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[slm](#)

---

print.snm	<i>Print Values</i>
-----------	---------------------

---

**Description**

Print the arguments of a 'snm' object.

**Usage**

```
## S3 method for class 'snm'  
print(x, ...)
```

**Arguments**

x	a snm object
...	unused argument

**Details**

This is a method for the function `print` for objects inheriting from class 'snm'.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[slm](#), [print](#)

---

print.snr	<i>Print Values</i>
-----------	---------------------

---

**Description**

Print the arguments of a snr object.

**Usage**

```
## S3 method for class 'snr'  
print(x, ...)
```

**Arguments**

x	a snr object
...	unused argument

**Details**

This is a method for the function `print` for objects inheriting from class `snr`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[snr](#)

---

print.ssr

*Print Values*

---

**Description**

Print the arguments of a `ssr` object.

**Usage**

```
## S3 method for class 'ssr'  
print(x, ...)
```

**Arguments**

<code>x</code>	a <code>ssr</code> object
<code>...</code>	unused argument

**Details**

This is a method for the function `print` for objects inheriting from class `ssr`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[ssr](#)

---

print.summary.nnr      *Print Vales*

---

**Description**

Print the arguments of a summary.nnr object

**Usage**

```
## S3 method for class 'summary.nnr'  
print(x, ...)
```

**Arguments**

x	an object of class summary.nnr
...	unused argument

**Details**

This is a method for the function print for objects inheriting from class summary.nnr.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[nnr](#), [summary.nnr](#)

---

print.summary.slm      *Print Values*

---

**Description**

Print the arguments of a summary.slm object

**Usage**

```
## S3 method for class 'summary.slm'  
print(x, ...)
```

**Arguments**

x	an object of class summary.slm
...	unused argument

**Details**

This is a method for the function `print` for objects inheriting from class `summary.slm`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[slm](#), [summary.slm](#)

---

print.summary.snm      *Print Values*

---

**Description**

Print the arguments of a `summary.snm` object

**Usage**

```
## S3 method for class 'summary.snm'  
print(x, ...)
```

**Arguments**

<code>x</code>	an object of class <code>summary.snm</code>
<code>...</code>	unused argument

**Details**

This is a method for the function `print` for objects inheriting from class `summary.snm`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[snm](#), [summary.snm](#)

---

print.summary.snr      *Print Values*

---

**Description**

Print the arguments of a summary.snr object

**Usage**

```
## S3 method for class 'summary.snr'  
print(x, ...)
```

**Arguments**

x	an object of class summary.snr
...	unused argument

**Details**

This is a method for the function print for objects inheriting from class summary.snr.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[snr](#), [summary.snr](#)

---

print.summary.ssr      *Print Values*

---

**Description**

Print the arguments of a summary.ssr object

**Usage**

```
## S3 method for class 'summary.ssr'  
print(x, ...)
```

**Arguments**

x	an object of class summary.ssr
...	unused argument.

**Details**

This is a method for the function `print` for objects inheriting from class `summary.ssr`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[ssr](#), [summary.ssr](#)

---

rk.prod

*Calculate product of reproducing kernels*

---

**Description**

Return a matrix as product of reproducing kernels

**Usage**

```
rk.prod(x, ...)
```

**Arguments**

`x` a matrix evaluating a reproducing kernel, or a vector.  
`...` optional lists of matrices evaluating reproducing kernels or vectors. All matrices must have the same dimensions. All vectors must have the same length. The length of each vector must equal to the column and row numbers of each matrix.

**Details**

The product of reproducing kernels is again a reproducing kernel. In SS ANOVA, product of reproducing kernels is often used to model interaction spline terms.

**Value**

a matrix as the product of reproducing kernels. If one argument is a vector, a kron kernel is constructed first.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

Gu, C. and Wahba, G. (1993a). Smoothing Spline ANOVA with component-wise Bayesian confidence intervals. *Journal of Computational and Graphical Statistics* 55, 353–368.  
Gu, C. and Wahba, G. (1993b). Semiparametric analysis of variance with tensor product thin plate splines. *JRSS B* 55, 353–368.

**See Also**[kron](#), [ssr](#)**Examples**

```
## Not run:  
x1<- 1:10/10  
x2<- runif(10)  
rk.prod(cubic(x1), periodic(x2))  
  
## End(Not run)
```

---

`seizure`*IEEG segments from a seizure patient*

---

**Description**

The 'seizure' data frame has 60,000 rows and 3 columns of data from an IEEG time series

**Usage**

```
data(seizure)
```

**Details**

The baseline segment contains 5-minute IEEG signal extracted at least four hours before the seizure's onset. The pre-seizure segment contains 5-minute IEEG signal right before a seizure's clinical onset. The sampling rate of the IEEG signal is 200 observations per second. Therefore there are 60,000 time points in each segment.

**Format**

The data frame contains the following columns:

`t` a numeric vector of the observation number

`base` a numeric vector of the baseline segment

`preseizure` a numeric vector of the segment right before a seizure

**Source**

D'Alessandro, M., Vachtsevanos, G., Esteller, R., Echauz, J. and Litt, B. (2001). A Generic Approach to Selecting the Optimal Feature for Epileptic Seizure Prediction. IEEE International Meeting of the Engineering in Medicine and Biology Society.

**references**

Qin, L. and Wang, Y. (2008), Nonparametric Spectral Analysis With Applications to Seizure Characterization Using EEG Time Series. *Annals of Applied Statistics* 2, 1432-1451.

---

Shrinkage

*Calculate reproducing kernels for Stein shrinkage estimate*

---

### Description

Return a matrix evaluating reproducing kernels for the discrete shrinkage towards zero or the mean estimate

### Usage

```
shrink0(x, y=x)
shrink1(x, y=x)
```

### Arguments

**x** a vector of numerical values or factor indicating different levels.  
**y** a vector of numerical values or factor indicating different levels. Default is x.

### Value

a matrix with the numbers of row and column equal to the length of x and y respectively. The  $[i, j]$  element is the reproducing kernel evaluated at the  $i$ th element of x and  $j$ th element of y.

shrink0 shrinks towards zero, and shrink1 shrinks towards the mean.

### Author(s)

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

### See Also

[shrink0,ssr](#)

### Examples

```
## Not run:
x<-rep(1:10,2)
shrink1(x)

## End(Not run)
```

---

`sine4p`*Calculate Reproducing Kernels for Periodic L-Splines with Period 1/2*

---

**Description**

Return a matrix evaluating reproducing kernels for periodic L-splines at observed points.

**Usage**

```
sine4p(s, t=s)
```

**Arguments**

`s` a numeric vector.  
`t` an optional vector. Default is the same as `s`.

**Details**

The general formula of the reproducing kernel is provided in Gu (2001). The close form is not available, so an approximate based on the first 50 terms of the series is used.

**Value**

a matrix with the numbers of row and column equal to the lengths of `s` and `t` respectively. The `[i, j]` element is the reproducing kernel evaluated at `(s[i], t[j])`.

**References**

Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.  
Gu, C. (2001). Smoothing Spline ANOVA Modes. Chapman and Hall.

**See Also**

[cubic](#), [lspline](#)

**Examples**

```
## Not run:  
x<- seq(0, 1, len=100)  
sine4p(x)  
  
## End(Not run)
```

slm

*Fit a Semi-parametric Linear Mixed Effects Model***Description**

Returns an object of class `slm` that represents a semi-parametric linear mixed effects model fit.

**Usage**

```
slm(formula, rk, data=list(), random, weights=NULL,
     correlation=NULL, control=list(apVar=FALSE))
```

**Arguments**

<code>formula</code>	a formula object, with the response on the left of a $\sim$ operator, and the bases of the null space $H_0$ of the non-parametric function and other terms, separated by $+$ operators, on the right.
<code>rk</code>	a list of expressions that specify the reproducing kernels of the spline function(s), $R^1, \dots, R^p$ for spaces $H_1, \dots, H_p$ . See the help file of <code>ssr</code> for more details.
<code>data</code>	An optional data frame containing the variables appearing in <code>formula</code> , <code>random</code> , <code>rk</code> , <code>correlation</code> , <code>weights</code> . By default, the variables are taken from the environment from which <code>slm</code> is called.
<code>random</code>	A named list of formulae, lists of formulae, or <code>pdMat</code> objects, which defines nested random effects structures. See help file of <code>lme</code> for more details.
<code>weights</code>	An optional <code>varFun</code> object or one-sided formula describing the within-group heteroscedasticity structure. See the help file of <code>lme</code> for more details.
<code>correlation</code>	An optional <code>corStruct</code> object specifying the within-group correlation structure. See <code>lme</code> for more details.
<code>control</code>	an optional list of any applicable control parameters from <code>lme</code> .

**Details**

This generic function fits a semi-parametric linear mixed effects model (or non-parametric mixed effects models) as described in Wang (1998), but allowing for general random and correlation structures. Because the connection to a linear mixed effects model is adopted, only GML is available to choose smoothing parameters.

**Value**

An object of class `slm` is returned. Generic functions such as `print`, `summary`, `predict` and `intervals` have methods to show the results of the fit.

Note: output from earlier versions of `slm` shows incorrect smoothing spline parameters for SSANOVA, which is corrected in this version.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>.

**References**

Wang, Y. (1998) Mixed Effects Smoothing Spline ANOVA. JRSS, Series B, 60:159–174.  
 Pinheiro, J. C. and Bates, D. M. (2000) Mixed-effects Models in S and S-Plus. Springer.

**See Also**

[ssr](#), [predict.slm](#), [intervals.slm](#), [print.slm](#), [summary.slm](#)

**Examples**

```
## Not run:
## SS ANOVA is used to model "time" and "group"
## with random intercept for "dog".
data(dog)

dog.fit<- slm(y~group*time, rk=list(cubic(time), shrink1(group),
  rk.prod(kron(time-0.5),shrink1(group)),rk.prod(cubic(time),
  shrink1(group))), random=list(dog=~1), data=dog)

## End(Not run)
```

---

 snm

---

*Fit a Semi-parametric Nonlinear Mixed-effects Model*


---

**Description**

This generic function fits a semi-parametric nonlinear mixed-effects model in the formulation described in Ke and Wang (2001). Current version only allows linear dependence on non-parametric functions.

**Usage**

```
snm(formula, func, data=list(), fixed, random=fixed,
  groups, start, spar="v", verbose=FALSE, method="REML", control=NULL,
  correlation=NULL, weights=NULL)
```

**Arguments**

`formula` a formula object, with the response on the left of a `~` operator, and an expression of variables, parameters and non-parametric functions on the right.

func	a list of spline formulae each specifying the spline components necessary to estimate each non-parametric function. On the left of a ~ operator of each component is the unknown function symbol(s) as well as its arguments, while the right side is a list of two components nb, an optional one-side formula for representing the null space's bases, and a required rk structure. nb and rk are similar to formula and rk in <code>ssr</code> . A missing nb denotes an empty null space.
fixed	a two-sided formula specifying models for the fixed effects. The syntax of <code>fixed</code> in <code>nlme</code> is adopted.
start	a numeric vector, the same length as the number of fixed effects, supplying starting values for the fixed effects.
spar	a character string specifying a method for choosing the smoothing parameter. "v", "m" and "u" represent GCV, GML and UBR respectively. Default is "v" for GCV.
data	An optional data frame containing the variables appearing in formula, random, rk, correlation, weights. By default, the variables are taken from the environment from which <code>snm</code> is called.
random	an optional random effects structure specifying models for the random effects. The same syntax of <code>random</code> in <code>nlme</code> is assumed.
groups	an optional one-sided formula of the form <code>~g1</code> (single level) or <code>~g1/.../gQ</code> (multiple levels of nesting), specifying the partitions of the data over which the random effects vary. <code>g1,...,gQ</code> must evaluate to factors in data. See <code>nlme</code> for details.
verbose	an optional logical numerical value. If TRUE, information on the evolution of the iterative algorithm is printed. Default is FALSE.
method	a character string. If 'REML' the model is fit by maximizing the restricted log-likelihood. If 'ML' the log-likelihood is maximized. Default is 'REML'.
control	a list of parameters to control the performance of the algorithm.
correlation	an optional <code>corStruct</code> object describing the within-group correlation structure. See the documentation of <code>corClasses</code> for a description of the available <code>corStruct</code> classes. Default is NULL, corresponding to no within-in group correlations.
weights	an optional <code>varFunc</code> object or one-sided formula describing the within-group heteroscedasticity structure. If given as a formula, it is used as the argument to <code>varFixed</code> , corresponding to fixed variance weights. See the documentation on <code>varClasses</code> for a description of the available <code>varFunc</code> classes. Defaults to NULL, corresponding to homoscedastic within-group errors.

### Value

an object of class `snm` is returned, representing a semi-parametric nonlinear mixed effects model fit. Generic functions such as `print`, `summary`, `predict` and `intervals` have methods to show the results of the fit.

### Author(s)

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>.

## References

- Ke, C. and Wang, Y. (2001). Semi-parametric Nonlinear Mixed Effects Models and Their Applications. *JASA* 96:1272-1298.
- Pinheiro, J.C. and Bates, D. M. (2000). *Mixed-Effects Models in S and S-PLUS*. Springer.

## See Also

[predict.snm](#), [intervals.snm](#), [snm.control](#), [print.snm](#), [summary.snm](#)

## Examples

```
## Not run:
data(CO2)

options(contrasts=rep("contr.treatment", 2))
co2.fit1 <- nlme(uptake~exp(a1)*(1-exp(-exp(a2)*(conc-a3))),
               fixed=list(a1+a2~Type*Treatment,a3~1),
               random=a1~1, groups=~Plant,
               start=c(log(30),0,0,0,log(0.01),0,0,0,50),
               data=CO2)

M <- model.matrix(~Type*Treatment, data=CO2)[,-1]
co2.fit2 <- snm(uptake~exp(a1)*f(exp(a2)*(conc-a3)),
               func=f(u)~list(~I(1-exp(-u))-1,lspline(u, type="exp")),
               fixed=list(a1~M-1,a3~1,a2~Type*Treatment),
               random=list(a1~1), group=~Plant, verbose=TRUE,
               start=co2.fit1$coe$fixed[c(2:4,9,5:8)], data=CO2)

## End(Not run)
```

---

snm.control

*Set Control Parameters for snm*

---

## Description

Control parameters supplied in the function call replace the defaults to be used in calling snm.

## Usage

```
snm.control(rkpk.control, nlme.control, prec.out=0.0005,
           maxit.out=30, converg="COEF", incDelta)
```

## Arguments

- `rkpk.control` a optional list of control parameters for `dsidr` or `dmudr` to estimate the unknown functions.
- `nlme.control` a list of control parameters for the nonlinear regression step, the same as `nlmeControl`. Default is `list(returnObject = T, maxIter = 5)`.

prec.out	tolerance for convergence criterion. Default is 0.0005.
maxit.out	maximum number of iterations for the algorithm. Default is 30.
converg	an optional character, with possible values "COEF" and "PRSS", specifying the convergence criterion to be used. "COEF" uses the change of estimate of parameters and functions to assess convergence, and "PRSS" uses penalized residual sums of squares. Default is "COEF".
incDelta	specifies a small value as increment to calculate derivatives. Default is 0.001.

**Value**

Returned is a list includes all re-seted control parameters.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[snm](#), [dsidr](#), [dmudr](#)

**Examples**

```
## Not run:
## set maximum iteration to be 50
snm.control(maxit.out=50)

## End(Not run)
```

---

 snr

*Fit A Semi-parametric Nonlinear Regression Model*

---

**Description**

This generic function fits a Semi-parametric Nonlinear Regression Model as formulated in Ke (2000).

**Usage**

```
snr(formula, func, params, data, start,
     spar = "v", verbose = FALSE, control = list(), correlation = NULL,
     weights = NULL)
```

**Arguments**

formula	a model formula, with the response on the left of a ~ operator and on the right an expression representing the mean function with at least one unknown function appearing with a symbol, e.g. f. If "data" is present, all names except the nonparametric function(s) used in the formula should be defined as parameters or variables in the data frame.
func	a list of spline formulae each specifying the spline components necessary to estimate each non-parametric function. On the left of a ~ operator of each component is the unknown function symbol(s) as well as its arguments, while the right side is a list of two components nb, an optional one-side formula for representing the null space's bases, and a required rk structure. nb and rk are similar to formula and rk in <code>ssr</code> . A missing nb denotes an empty null space.
params	a two-sided formula specifying models for the parameters. The syntax of <code>params</code> in <code>gnls</code> is adopted. See <code>gnls</code> for details.
data	an optional data frame containing the variables named in <code>model</code> , <code>params</code> , <code>correlation</code> and <code>weights</code> . By default the variables are taken from the environment from which <code>snr</code> is called.
start	a numeric list with two components: "params=", a vector of the size of the length of the unknown parameters, providing initial values for the parameters, and "f=" a list of vectors or expressions which input initial values for the unknown functions. If the unknown functions appear linear in the model, the initial values then are not necessary.
spar	a character string specifying a method for choosing the smoothing parameter. "v", "m" and "u" represent GCV, GML and UBR respectively. Default is "v" for GCV.
verbose	an optional logical numerical value. If TRUE, information on the evolution of the iterative algorithm is printed. Default is TRUE.
control	an optional list of control parameters. See <code>snr.control</code> for details.
correlation	an optional <code>corStruct</code> as in <code>gnls</code> . Default is NULL, corresponding to uncorrelation.
weights	an optional <code>varFunc</code> structure as in <code>gnls</code> . Default is NULL, representing equal variances.

**Details**

A semi-parametric regression model is generalization of self-modeling regression, nonlinear regression and smoothing spline models, including as special cases (nonlinear) partial spline models, varying coefficients models, PP regression and some other popular models. 'snr' is implemented with an alternate iterative procedures with smoothing splines to estimate the unknown functions and general nonlinear regression to estimate parameters.

**Value**

An object of class `snr` is returned, representing a semi-parametric nonlinear regression fit. Generic functions such as `print`, `summary`, `intervals` and `predict` have methods to show the results of the fit.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>.

**References**

- Ke, C. (2000). Semi-parametric Nonlinear Regression and Mixed Effects Models. PhD thesis, University of California, Santa Barbara.
- Pinheiro, J.C. and Bates, D. M. (2000). Mixed-Effects Models in S and S-PLUS. Springer.
- Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.

**See Also**

[intervals.snr](#), [predict.snr](#), [snr.control](#)

**Examples**

```
## Not run:
data(CO2)
options(contrasts=rep("contr.treatment", 2))
co2.fit1 <- nlme(uptake~exp(a1)*(1-exp(-exp(a2)*(conc-a3))),
               fixed=list(a1+a2~Type*Treatment,a3~1),
               random=a1~1, groups=~Plant,
               start=c(log(30),0,0,0,log(0.01),0,0,0,50),
               data=CO2)

M <- model.matrix(~Type*Treatment, data=CO2)[-1]

## fit a SNR model
co2.fit2 <- snr(uptake~exp(a1)*f(exp(a2)*(conc-a3)),
               func=f(u)~list(~I(1-exp(-u))-1,lspline(u, type="exp")),
               params=list(a1~M-1, a3~1, a2~Type*Treatment),
               start=list(params=co2.fit1$coe$fixed[c(2:4,9,5:8)]), data=CO2)

## End(Not run)
```

---

snr.control

*Set Control Parameters for snr*

---

**Description**

Control parameters supplied in the function call replace the defaults to be used in calling snr.

**Usage**

```
snr.control(rkpk.control = list(job = -1, tol = 0, init = 0, limnla = c(-10,
0), varht = NULL, theta = NULL, prec = 1e-06, maxit = 30),
nls.control = list(returnObject = TRUE, maxIter = 5), incDelta = 0.001,
prec.out = 0.001, maxit.out = 30, converg = "COEF", method = "GN",
backfit = 5)
```

**Arguments**

rkpk.control	a optional list of control parameters for dsidr or dmudr to estimate the unknown functions. Default is "list(job = -1, tol = 0, init = 0, limnla = c(-10, 0), varht = NULL, theta = NULL, prec = 1e-06, maxit = 30)".
nls.control	a list of control parameters for the nonlinear regression step, the same as gnlsControl. Default is "list(returnObject = TRUE, maxIter = 5)".
incDelta	the incremental value to be used to calculate derivatives for the unknown functions. Default is 0.001
prec.out	tolerance for convergence criterion. Default is 0.0001.
maxit.out	maximum number of iterations for the algorithm. Default is 30.
converg	an optional character, with possible values COEF and PRSS, specifying the convergence criterion to be used. COEF uses the change of estimate of parameters and functions to assess convergence, and PRSS uses penalized residual sums of squares. Default is COEF.
method	an optional string of value either GN for Gauss-Newton or NR for Newton-Raphson iteration methods to estimate the unknown functions. Default is GN.
backfit	an integer to set the number of backfitting iterations inside the loop. Default is 5

**Value**

returned is a list includes all re-seted control parameters.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>.

**See Also**

[snr](#), [dsidr](#), [dmudr](#)

**Examples**

```
## use Newton-Raphson iteration and only a single backfitting
## Not run:
snr.control(method="NR", backfit=1)

## End(Not run)
```

---

 sphere

---

*Calculate Pseudo Reproducing Kernels for Spherical Splines*


---

**Description**

Return a matrix evaluating reproducing kernels for splines on a sphere.

**Usage**

```
sphere(x, y=x, order=2)
```

**Arguments**

x	a matrix of two columns or a list of two components, representing observed latitude and longitude respectively.
y	a matrix of two columns or a list of two components, representing latitude and longitude respectively. Default is the same as x.
order	an optional integer specifying the order of the spherical spline. Available are 2, 3, 4, 5 and 6, with a default 2.

**Details**

The kernel for spherical splines is a series inconvenient to compute. This pseudo kernel is based on a topological equivalence as described in Wahba (1981), for which cases the closed form can be derived.

**Value**

a matrix with the numbers of row and column equal to the lengths of x and y respectively. The [i, j] element is the reproducing kernel evaluated at  $(x[i, ], y[j, ])$  (or  $((x[[1]][i], x[[2]][i]), (y[[1]][j], y[[2]][j]))$  for lists).

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

Wahba, G. (1981). Spline Interpolation and Smoothing on the Sphere. SIAM J. Sci. Stat. Comput., Vol. 2, No. 1, March 1981.

Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.

**See Also**

[periodic](#)

## Examples

```
## Not run:
x<- seq(0, 2*pi, len=10)
y<- seq(-pi/2, pi/2, len=10)
s.ker<- sphere(cbind(x, y), order=3)

## End(Not run)
```

---

ssr

*Fit a General Smoothing Spline Regression Model*


---

## Description

Returns an object of class `ssr` which is a general/generalized/correlated smoothing spline fit.

## Usage

```
ssr(formula, rk, data = list(), subset, weights = NULL,
correlation = NULL, family = "gaussian", scale = FALSE,
spar = "v", varht = NULL, limnla = c(-10, 3), control = list())
```

## Arguments

<code>formula</code>	a formula object, with the response on the left of a <code>~</code> operator, and the bases of the null space $H_0$ , separated by <code>+</code> operators, on the right. Thus it specifies the parametric part of the model that contains functions which are not penalized.
<code>rk</code>	a list of expressions specifying reproducing kernels $R^1, \dots, R^p$ for $H_1, \dots, H_p$ . For $p = 1$ , <code>rk</code> may be specified with given functions. Supported functions are: "linear", "cubic", "quintic", and "septic" for linear, cubic, quintic and septic polynomial splines with "linear2", "cubic2", "quintic2", and "septic2" for another construction; "periodic" for periodic splines; "shrink0" and "shrink1" for Stein's shrink-toward-zero and shrink-toward-mean estimates; "tp" for thin-plate-splines; "lspline" for L-splines. For details on these kernels, see their help files. Users may also write their own functions.
<code>data</code>	a data frame containing the variables occurring in the formula and the <code>rk</code> . If this option is not specified, the variables should be on the search list. Missing values are not allowed.
<code>subset</code>	an optional expression indicating which subset of the rows of the data should be used in the fit. This can be a logical vector (which is replicated to have length equal to the number of observations), a numeric vector indicating which observation numbers are to be included, or a character vector of the row names to be included. All observations are included by default.
<code>weights</code>	a vector or a matrix specifying known weights for weighted smoothing, or a <code>varFunc</code> structure specifying a variance function structure. Its length, if a vector, or its number of columns and rows, if a matrix, must be equal to the length of responses. See documentations of <code>nlme</code> for available <code>varFunc</code> structures. The default is that all weights are equal.

correlation	a corStruct object describing the correlation structure for random errors. See documentations of corClasses for available correlation structures. Default is NULL for no correlation.
family	an optional string specifying the distribution family. Families supported are "binary", "binomial", "poisson", "gamma" and "gaussian" for Bernoulli, binomial, poisson, gamma and Gaussian distributions respectively. Default is "gaussian".
scale	an optional logical value. If 'TRUE', all covariates appearing in "rk" will be scaled into interval [0, 1]. This transformation will affect predict.ssr. Default is FALSE.
spar	a character string specifying a method for choosing the smoothing parameter. "v", "m" and "u" represent GCV, GML and UBR respectively. "u~", only used for non-Gaussian families, specifies UBR with an estimated variance. Default is "v".
varht	needed only when 'u' is chosen for 'method', which gives the fixed variance in calculation of the UBR function. Default is NULL for 'family="gaussian"' and 1 for all other families.
limnla	a vector of length one or two, specifying a search range for $\log_{10}(n \cdot \lambda)$ , where $\lambda$ is the smoothing parameter and $n$ is the sample size. If it is a single value, the smoothing parameter will be fixed at this value. This option is only applicable to spline smoothing with a single smoothing parameter.
control	a list of iteration and algorithmic constants. See ssr.control for details and default values.

## Details

We adopt notations in Wahba (1990) for the general spline and smoothing spline ANOVA models. Specifically, the functional relationship between the predictor and independent variable is unknown and is assumed to be in a reproducing kernel Hilbert space  $H$ .  $H$  is decomposed into  $H_0$  and  $H_1 + \dots + H_p$ , where the null space  $H_0$  is a finite dimensional space spanned by bases specified at the right side of  $\sim$  in formula, and  $H_1, \dots, H_p$  are reproducing kernel Hilbert spaces with reproducing kernel specified in the list rk.

The function is estimated from weighted penalized least square. `ssr` can be used to fit the general spline and smoothing spline ANOVA models (Wahba, 1990), generalized spline models (Wang, 1997) and correlated spline models (Wang, 1998). `ssr` can also fit partial spline model with additional parametric terms specified in the formula (Wahba, 1990).

`ssr` could be slow and memory intensive, especially for large sample size and/or when  $p$  is large. For fitting a cubic spline with CV or GCV estimate of the smoothing parameter, the S-Plus function `smooth.spline` is more efficient.

Components can be extracted using extractor functions `predict`, `deviance`, `residuals`, and `summary`. The output can be modified using `update`.

## Value

an object of class `ssr` is returned. See `ssr.object` for details.

Note: output from earlier versions of `ssr` shows incorrect smoothing spline parameters for SSANOVA, which is corrected in this version.

**Author(s)**

Yuedong Wang <yuedong@pstat.ucsb.edu> and Chunlei Ke <chunlei\_ke@yahoo.com>

**References**

- Gu, C. (1989). RKPACK and its applications: Fitting smoothing spline models. Proceedings of the Statistical Computing Section, ASA, 42-51.
- Gu, C. (2002). Smoothing Spline ANOVA. Springer, New York.
- Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.
- Wang, Y. (1995). GRKPACK: Fitting Smoothing Spline ANOVA Models for Exponential Families. Communications in Statistics: Simulation and Computation, 24: 1037-1059.
- Wang, Y. (1998) Smoothing Spline Models with Correlated Random Errors. JASA, 93:341-348.
- Ke, C. and Wang, Y. (2002) ASSIST: A Suite of S-plus functions Implementing Spline smoothing Techniques. Available at: <https://yuedong.faculty.pstat.ucsb.edu/>

**See Also**

[deviance.ssr](#), [hat.ssr](#), [plot.ssr](#), [ssr.control](#), [predict.ssr](#), [print.ssr](#), [ssr.object](#), [summary.ssr](#), [smooth.spline](#).

**Examples**

```
## Not run:
library(MASS)
# fitting a cubic spline
fit1<- ssr(accel~times, data=mcycle, scale=T, rk=cubic(times))
summary(fit1)

# using GML to choose the smoothing parameter
fit2<- update(fit1, spar="m")

data(acid)
## fit an additive thin plate spline
acid.fit<- ssr( ph ~ t1 + x1 + x2, rk = list(tp(t1), tp(list(x1, x2))),
  data = acid, spar = "m", scale = FALSE)
acid.fit

## End(Not run)
```

---

ssr.control

*Set Control Parameters for 'ssr'*


---

**Description**

The values supplied in the function call replace the defaults and a list with all possible arguments is returned. The returned list is used as the 'control' argument to the 'ssr' function.

**Usage**

```
ssr.control(job=-1, tol=0.0, init=0.0, theta, prec=1e-06,
            maxit=30, tol.g=0.0, prec.g=1e-06, maxit.g=30)
```

**Arguments**

job	an integer representing the optimization method used to find the smoothing parameter. The options are job=-1: golden-section search on (limnla(1), limnla(2)); job=0: golden-section search with interval specified automatically; job >0: regular grid search on [limnla(1), limnla(2)] with the number of grids = job + 1. Default is -1. This is only applicable to smoothing spline model with a single smoothing parameter.
tol	tolerance for truncation used in 'dsidr' or 'dmudr'. Default is 0.0 which sets to square of machine precision.
init	init=0 means no initial values are provided for smoothing parameters theta; init=1 means initial values are provided for the theta. Default is 0. This option is only applicable to smoothing spline models with multiple smoothing parameters.
theta	If init=1, theta includes initial values for smoothing parameters. Default is NULL. This is only applicable to smoothing spline models with multiple smoothing parameters.
prec	precision requested for the minimum score value in 'dmudr', where precision is the weaker of the absolute and relative precisions. Default is 1e-06. This is only applicable to smoothing spline models with multiple smoothing parameters.
maxit	maximum number of iterations allowed in 'dmudr'. Default is 30. This is only applicable to smoothing spline model with multiple smoothing parameters.
tol.g	the tolerance for elements of w's in GRKPK. Default is 0.0 which means using the machine precision. This is only applicable to generalized spline smoothing.
prec.g	precision for stopping the iteration in GRKPK. Default is 1e-06. This is only applicable to generalized spline smoothing.
maxit.g	maximum number of iterations allowed for the iteration in GRKPACK. Default is 30. This is only applicable to generalized spline smoothing.

**Value**

a list with components for each of the possible arguments.

**See Also**

[ssr](#)

**Examples**

```
## Not run:
# use regular grid search method with 100 grid points
ssr.control(job=99)

## End(Not run)
```

---

ssr.object	<i>A fitted ssr Object</i>
------------	----------------------------

---

**Description**

An object returned by the `ssr` function, inheriting from class `ssr`, and representing a fitted smoothing spline model. Objects of this class have methods for the generic functions `predict`, `print` and `summary`.

**Value**

The following components must be included in a legitimate `ssr` object:

<code>call</code>	a list containing an image of the <code>ssr</code> call that produced the object
<code>coef</code>	estimated coefficients for the spline estimate
<code>lambda</code>	a vector representing the estimate smoothing parameters
<code>fitted</code>	fitted values of the unknown mean function
<code>family</code>	the distribution family used
<code>cor.est</code>	estimated parameters, if any, in <code>corMatrix</code>
<code>var.est</code>	estimated parameters, if any, in <code>varFunc</code>
<code>s</code>	design matrix extracted from formula
<code>q</code>	a list of matrices representing reproducing kernels evaluated at design points.
<code>residuals</code>	working residuals from the fit.
<code>df</code>	equivalent degrees of freedom. It is calculated as the trace of the hat matrix.
<code>weight</code>	a matrix representing the covariance matrix. It is <code>NULL</code> for iid data.
<code>rkpk.obj</code>	an object representing fits from <code>dsidr/dmudr/gdsidr/gdmudr</code> . See help files for <code>dsidr/dmudr/gdsidr/gdmudr</code> for more details.
<code>scale</code>	a logical value, specifying if scaling is used.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[ssr](#), [predict.ssr](#), [summary.ssr](#), [plot.ssr](#), [dsidr](#), [dmudr](#), [gdsidr](#), [gdmudr](#)

---

star	<i>Magnitude of the Mira Variable R Hydrae</i>
------	--

---

**Description**

The star data frame has 1086 rows and 2 columns of data from the Mira Variable R Hydrae

**Usage**

```
data(star)
```

**Details**

This dataset contains magnitude (brightness) of the Mira variable R Hydrae during 1900-1950.

**Format**

The data frame contains the following columns:

time a numeric vector of the observation time in days

magnitude a numeric vector of brightness of the Mira variable R Hydrae

**Source**

Genton, M. G. and Hall, P. (2007). Statistical Inference for Evolving Periodic Functions, Journal of the Royal Statistical Society B 69, 643-657.

**references**

Yuedong Wang and Chunlei Ke (2009), Smoothing Spline Semi-parametric Nonlinear Regression Models, Journal of Computational and Graphical Statistics 18, 165-183.

---

Stratford	<i>Daily maximum temperatures in Stratford</i>
-----------	--

---

**Description**

The Stratford data frame has 73 rows and 2 columns of data containing daily maximum temperatures in Stratford every five days in 1990

**Usage**

```
data(Stratford)
```

**Details**

Daily maximum temperatures from the station in Stratford, Texas, in the year 1990 were extracted. The year was divided into 73 five-day periods and measurements on the third day in each period were selected as observations.

**Format**

The data frame contains the following columns:

x a numeric vector representing time in a year scaled into [0,1]

y a numeric vector of the observed maximum temperature in Fahrenheit

**Source**

This is part of a climate dataset downloaded from the Carbon Dioxide Information Analysis Center at <http://cdiac.ornl.gov/ftp/ndp070>.

---

summary.nnr

*Object Summaries*

---

**Description**

Summarize a nnr object

**Usage**

```
## S3 method for class 'nnr'  
summary(object, ...)
```

**Arguments**

object	a fitted nnr object.
...	unused argument

**Details**

This is a method for the function `summary` for objects inheriting from class `nnr`. See `summary` for the general behavior of this function.

**Author(s)**

Chunlei Ke <[chunlei\\_ke@yahoo.com](mailto:chunlei_ke@yahoo.com)> and Yuedong Wang <[yuedong@pstat.ucsb.edu](mailto:yuedong@pstat.ucsb.edu)>

**See Also**

[nnr](#), [print.nnr](#)

summary.slm

*Object Summaries*

---

**Description**

Summarize a slm object

**Usage**

```
## S3 method for class 'slm'  
summary(object, ...)
```

**Arguments**

object	a fitted slm object.
...	unused argument

**Details**

This is a method for the function `summary` for objects inheriting from class `slm`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[slm](#), [print.slm](#)

---

summary.snm

*Object Summaries*

---

**Description**

Summarize a snm object

**Usage**

```
## S3 method for class 'snm'  
summary(object, ...)
```

**Arguments**

object	a fitted 'snm' object.
...	unused argument

**Details**

This is a method for the function `summary` for objects inheriting from class `snm`.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[snm](#), [print.snm](#)

---

summary.snr

*Object Summaries*

---

**Description**

Summarize a `snr` object

**Usage**

```
## S3 method for class 'snr'  
summary(object, ...)
```

**Arguments**

<code>object</code>	a fitted <code>snr</code> object.
<code>...</code>	unused argument

**Details**

This is a method for the function `summary` for objects inheriting from class `snr`. See `summary` for the general behavior of this function.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[snr](#), [print.snr](#)

---

summary.ssr	<i>Summarize a ssr object</i>
-------------	-------------------------------

---

**Description**

Provides a synopsis of a ssr object and perform tests.

**Usage**

```
## S3 method for class 'ssr'  
summary(object, ...)
```

**Arguments**

object	a fitted ssr object.
...	unused option.

**Details**

This is a method for the function summary for objects inheriting from class ssr.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**See Also**

[ssr](#), [print.ssr](#)

---

Thin	<i>Calculate Reproducing Kernels for Thin Plate Splines</i>
------	---

---

**Description**

Return a matrix evaluating reproducing kernels for thin plate splines at observed points.

**Usage**

```
tp.pseudo(s, u=s, order=2)  
tp(s, u=s, order=2)  
tp.linear(s, u=s)
```

**Arguments**

s	a list or matrix of observations. One component, if a list, and one column, if a matrix, contains observations on one variable. If a list, all components must be of the same length.
u	a list or matrix of observations. If a list, all components must be of the same length. The number of componets of the list, or the number of column of the matrix must be the same as that for s. Default is s.
order	an optional integer specifying the order of the thin plate spline. Default is 2. Let $d$ be the dimension of s (and u). Then order must satisfy $2 * order - d > 0$ .

**Details**

The pseudo kernel, which is conditional definite positive instead of definite positive, is easy to calculate, while the true reproducing kernel is complicated. Pseudo Kernels are enough to compute spline estimates, but to calualte Bayesian confidnece intervals, the true kernel is required. For the special case of  $d=2$  and  $order=2$ , the function `tp.linear` computes evaluations of the reproducing kernel of the space spanned by linear basis.

**Value**

a matrix with the numbers of row and column equal to the common length of componets or the number of row of s and t respectively. The  $[i, j]$  element is the pseudo, true, or linear reproducing kernel evaluated at the  $i$ th element of s and  $j$ th element of u.

**Author(s)**

Chunlei Ke <chunlei\_ke@yahoo.com> and Yuedong Wang <yuedong@pstat.ucsb.edu>

**References**

- Wahba, G. (1990). Spline Models for Observational Data. SIAM, Vol. 59.
- Gu, C. and Wahba, G (1993). Smoothing Spline ANOVA with component-wise Bayesian confidence intervals. Journal of Computational and Graphical Statistics 55, 353–368.

**See Also**

[ssr](#), [cubic](#)

**Examples**

```
data(acid)
## Not run: tp.pseudo(list(acid$x1, acid$x2))
## Not run: tp.pseud0(list(acid$x1, acid$x2), order=3)
```

---

TXtemp

*Texas Historical Climate Data*

---

### **Description**

The data frame TXtemp, obtained from the Carbon Dioxide Information and Analysis Center at Oak Ridge National Laboratory, has 17280 rows and 6 columns of data representing monthly temperature records for stations in Texas.

### **Usage**

```
data(TXtemp)
```

### **Format**

The data frame contains the following columns:

stacode a numeric vector of the unique station code formed by combining the two-digit state number [state numbers range from 1 to 48] and the four-digit station number (values range from 0008 to 9933);

lat, long numeric vectors identifying the latitudes and longitudes of the stations in decimal degree.

year a numeric vector comprising the year for the records

month a numeric vector of values 1 to 12, representing the month for the data

mmtemp a numeric vector of monthly average temperature in Fahrenheit scale.

### **Details**

The data set was extracted from a large national historical climate data, containing data for 48 stations in Texas from 1961 to 1990. Monthly temperature records as well as the latitude and longitude for each station were available.

Of note, the missing values were coded as -99.99.

### **Source**

Data are downloadable from <https://ess-dive.lbl.gov/>

---

ultrasound

*Ultrasound imaging of the tongue shape*

---

### **Description**

The 'ultrasound' data frame has 1,215 rows and 4 columns of data from an ultrasound experiment

### **Usage**

```
data(ultrasound)
```

### **Details**

A Russian speaker produced the consonant sequence, /gd/, in three different linguistic environments: '2words', 'cluster' and 'Schwa', with three replications for each environment. 15 points from each of 9 slices of tongue curves separated by 30 ms (milliseconds) are extracted. Therefore, in total there are  $15 \times 9 \times 3 = 1,215$  observations.

### **Format**

The data frame contains the following columns:

height a numeric vector of tongue height in mm

length a numeric vector of tongue length in mm

time a numeric vector of time in ms

env a factor with three levels: 1 2 and 3 for environment '2words', 'cluster' and 'Schwa' respectively

### **Source**

Phonetics-Phonology Lab of New York University.

### **references**

Davidson, L. (2006). Comparing Tongue Shapes from Ultrasound Imaging Using Smoothing Spline Analysis of Variance. *Journal of the Acoustical Society of America* 120, 407-415.

---

USAtemp

*Average Winter temperature in the United States*

---

### **Description**

The USAtemp data frame has 1214 rows and 3 columns of data containing average Winter temperatures in 1981 from 1205 stations in USA.

### **Usage**

```
data(USAtemp)
```

### **Format**

The data frame contains the following columns:

temp a numeric vector of average temperatures (Fahrenheit)

lat a numeric vector of the latitude of a station

long a numeric vector of the longitude of a station

### **details**

The average Winter temperatures are calculated as the averages of temperatures in December, January and February. The geological locations of 1214 stations are given in terms of longitude and latitude.

---

wesdr

*Wisconsin Epidemiological Study of Diabetic Retinopathy*

---

### **Description**

The wesdr data frame has 669 rows and 5 columns of data from an ongoing epidemiological study of a cohort of patients receiving their medical care in an 11-country area in southern Wisconsin.

### **Usage**

```
data(wesdr)
```

### **Details**

The progression of diabetic retinopathy was assessed together with a number of medical, demographic, ocular and other covariates and the retinopathy scores.

**Format**

This data frame contains the following columns:

num a numeric vector giving IDs for individuals.

dur a numeric vector of duration of at baseline in year.

gly a numeric vector of glycosylated hemoglobin, a measuer of hyperglycemia.

bmi a numeric vecttor of body mass index, weight in  $kg/(heightinmeter)^2$ .

prg a vector of 0 or 1's representing disease progression for each individual.

**Source**

Klein, R., Klein, B. E. K., Moss, S. E., Davis, M. D. and Demets, D. L. (1989a). The Wisconsin epidemiologic study of diabetic retinopathy. IX. Four year incidence and progression of diabetic retinopathy when age at diagnosis is less than 30 years. Arch. Ophthalmal. 107, 237-243.

Klein, R., Klein, B. E. K., Moss, S. E., Davis, M. D. and Demets, D. L. (1989b). The Wisconsin epidemiologic study of diabetic retinopathy. X. Four year incidence and progression of diabetic retinopathy when age at diagnosis is less than 30 years. Arch. Ophthalmal. 107, 244-249.

---

 xyplot2

*Extension of XYPLOT*


---

**Description**

Extend xyplot to superpose one or more symbols to each panel.

**Usage**

```
xyplot2(formula, data, type = "l", ...)
```

**Arguments**

formula	a two-sided formula as accepted in xyplot
data	a list of data frames. Each component shall be able to evaluate the vatiabes appearing in formula
type	a vector of characters to indicate what type of plots are to draw. Default is line.
...	any options as accepted in xyplot

**Value**

On each panel, several plot types, the length of data, are superposed.

# Index

## \* datasets

- acid, 3
- Arosa, 6
- bond, 7
- canadaTemp, 8
- chickenpox, 9
- climate, 10
- dog, 14
- horm.cort, 22
- paramecium, 36
- seizure, 55
- star, 72
- Stratford, 72
- TXtemp, 78
- ultrasound, 79
- USAtemp, 80
- wesdr, 80

## \* file

- alogit, 4
- anova.ssr, 4
- bdiag, 7
- chol.new, 9
- dcrdr, 11
- deviance.ssr, 11
- dmudr, 12
- dsidr, 14
- dsms, 16
- gdmudr, 17
- gdsidr, 19
- hat.ssr, 21
- ident, 23
- inc, 23
- intervals.nnr, 24
- intervals.slm, 26
- intervals.snm, 28
- intervals.snr, 29
- kron, 31
- lspline, 32
- nnr, 33

- nnr.control, 35
- periodic, 37
- plot.bCI, 38
- plot.ssr, 39
- Polynomial, 40
- Polynomial2, 41
- predict.slm, 42
- predict.snm, 43
- predict.snr, 44
- predict.ssr, 45
- print.anova.ssr, 47
- print.nnr, 47
- print.slm, 48
- print.snm, 49
- print.snr, 49
- print.ssr, 50
- print.summary.nnr, 51
- print.summary.slm, 51
- print.summary.snm, 52
- print.summary.snr, 53
- print.summary.ssr, 53
- rk.prod, 54
- Shrinkage, 56
- sine4p, 57
- slm, 58
- snm, 59
- snm.control, 61
- snr, 62
- snr.control, 64
- sphere, 66
- ssr, 67
- ssr.control, 69
- ssr.object, 71
- summary.nnr, 73
- summary.slm, 74
- summary.snm, 74
- summary.snr, 75
- summary.ssr, 76
- Thin, 76

- xyplot2, 81
- acid, 3
- alogit, 4
- anova.ssr, 4, 47
- Arosa, 6
- bdiag, 7
- bond, 7
- canadaTemp, 8
- chickenpox, 9
- chol, 10
- chol.new, 9
- climate, 10
- cubic, 38, 42, 57, 77
- cubic (Polynomial), 40
- cubic2, 41
- cubic2 (Polynomial2), 41
- dcrdr, 11
- deviance.ssr, 11, 69
- dmudr, 12, 16, 18, 20, 36, 62, 65, 71
- dog, 14
- dsidr, 13, 14, 18, 20, 36, 62, 65, 71
- dsms, 16
- gdmudr, 13, 16, 17, 20, 71
- gdsidr, 13, 16, 18, 19, 71
- hat.ssr, 21, 69
- horm.cort, 22
- ident, 23
- inc, 23
- intervals.nnr, 24, 34
- intervals.slm, 26, 38, 59
- intervals.snm, 28, 38, 61
- intervals.snr, 29, 38, 64
- kron, 31, 55
- kronecker, 32
- linear, 42
- linear (Polynomial), 40
- linear2, 41
- linear2 (Polynomial2), 41
- lspline, 32, 38, 57
- nnr, 25, 33, 36, 48, 51, 73
- nnr.control, 34, 35
- paramecium, 36
- periodic, 37, 66
- plot.bCI, 25, 27, 29, 30, 38, 46
- plot.ssr, 39, 69, 71
- Polynomial, 40
- Polynomial2, 41
- predict, 44
- predict.slm, 42, 59
- predict.snm, 43, 61
- predict.snr, 44, 64
- predict.ssr, 27, 29, 30, 38, 45, 69, 71
- print, 49
- print.anova.ssr, 5, 47
- print.nnr, 34, 47, 73
- print.slm, 48, 59, 74
- print.snm, 49, 61, 75
- print.snr, 49, 75
- print.ssr, 50, 69, 76
- print.summary.nnr, 51
- print.summary.slm, 51
- print.summary.snm, 52
- print.summary.snr, 53
- print.summary.ssr, 53
- quintic, 42
- quintic (Polynomial), 40
- quintic2, 41
- quintic2 (Polynomial2), 41
- rk.prod, 54
- seizure, 55
- septic, 42
- septic (Polynomial), 40
- septic2, 41
- septic2 (Polynomial2), 41
- shrink0, 56
- shrink0 (Shrinkage), 56
- shrink1 (Shrinkage), 56
- Shrinkage, 56
- sine4p, 57
- slm, 27, 43, 48, 49, 52, 58, 74
- smooth.spline, 69
- snm, 29, 44, 52, 59, 62, 75
- snm.control, 61, 61
- snr, 30, 45, 50, 53, 62, 65, 75
- snr.control, 64, 64

sphere, 66  
ssr, 5, 12, 13, 16, 18, 20, 21, 32–34, 41, 42,  
46, 47, 50, 54–56, 59, 67, 70, 71, 76,  
77  
ssr.control, 69, 69  
ssr.object, 69, 71  
star, 72  
Stratford, 72  
summary.nnr, 34, 51, 73  
summary.slm, 52, 59, 74  
summary.snm, 52, 61, 74  
summary.snr, 53, 75  
summary.ssr, 54, 69, 71, 76  
  
Thin, 76  
tp (Thin), 76  
TXtemp, 78  
  
ultrasound, 79  
USAtemp, 80  
  
wesdr, 80  
  
xyplot2, 81