

Package ‘circularEV’

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CalcRLsplineML	<i>Calculate T-year levels for spline ML model</i>
----------------	--

Description

Calculate T-year levels for spline ML model

Usage

```
CalcRLsplineML(
  Data,
  drc,
  h,
  xiBoot,
  sigBoot,
  TTs = c(100, 10000),
  thetaGrid = 1:360,
  timeRange,
  thr
)
```

Arguments

Data	Response variable
drc	Directional covariate
h	Bandwidth value
xiBoot	Bootstrap estimates for EVI
sigBoot	Bootstrap estimates for shape
TTs	T-year levels. For example, TTs = c(100, 10000).

thetaGrid	Grid values at which the estimation is performed
timeRange	Time range of the sample
thr	Threshold values along thetaGrid

Value

List including bootstrap estimates of T-year levels.

See Also

[SplineML](#) for examples.

Examples

```
## See also examples in vignettes:  
# vignette("localMethods", package = "circularEV")  
# vignette("splineML", package = "circularEV")
```

drc	<i>Directional covariate for HsSP data</i>
-----	--

Description

A vector of length 1521.

Usage

```
drc
```

Format

A vector of length 1521.

Details

Directional covariate of HsSP data used by Reistad, M., Breivik, Ø., Haakenstad, H., Aarnes, O. J., Furevik, B. R., and Bidlot, J.-R. (2011), A high-resolution hindcast of wind and waves for the North Sea, the Norwegian Sea, and the Barents Sea, *J. Geophys. Res.*, 116:1-18.

HsSP

Hindcast storm peak significant wave height data

Description

A vector of length 1521.

Usage

HsSP

Format

A vector of length 1521.

Details

HsSP data used by Reistad, M., Breivik, Ø., Haakenstad, H., Aarnes, O. J., Furevik, B. R., and Bidlot, J.-R. (2011), A high-resolution hindcast of wind and waves for the North Sea, the Norwegian Sea, and the Barents Sea, *J. Geophys. Res.*, 116:1-18.

LocalEstim

Local bootstrap estimation of EVI, scale and T-year levels

Description

Local bootstrap estimation of EVI, scale and T-year levels

Usage

```
LocalEstim(  
  Data,  
  drc,  
  thr = NULL,  
  thetaGrid,  
  nBoot = 100,  
  EVIestimator = "Mom",  
  h = 30,  
  useKernel = TRUE,  
  concent = 10,  
  movThr = TRUE,  
  TTs = NULL,  
  timeRange = NULL  
)
```

Arguments

Data	Response variable
drc	Directional covariate
thr	Threshold values along thetaGrid
thetaGrid	Grid values at which the estimation is performed
nBoot	Number of bootstrap resamples. Default to 100.
EVIestimator	It can be either "ML" or "Mom"
h	Bandwidth value
useKernel	Logical. If TRUE (default), use kernel to assign weights depending on the directional distance.
concent	Concentration parameter value for von Mises kernel
movThr	Logical. If TRUE (default), moving threshold within the window used.
TTs	T-year levels. For example, TTs = c(100, 10000).
timeRange	Time range of the sample

Details

See Konzen, E., Neves, C., and Jonathan, P. (2021). Modeling nonstationary extremes of storm severity: Comparing parametric and semiparametric inference. *Environmetrics*, 32(4), e2667.

Value

List including bootstrap estimates of EVI, scale and T-year levels.

Examples

```

data(HsSP)
data(drc)
timeRange <- 54.5

idx <- order(drc)
drc <- drc[idx]
Data <- HsSP[idx]
set.seed(1234)
Data <- Data + runif(length(Data), -1e-4, 1e-4)

thetaVec <- 1:360

data(thresholdExampleMom) # loads threshold example
thrResultMom <- thresholdExampleMom

h <- 60
useKernel <- TRUE
concent <- 10
movThr <- TRUE

```

```

nBoot <- 30
set.seed(1234)
output <- LocalEstim(Data=Data, drc=drc, thr=thrResultMom,
                    thetaGrid=thetaVec, nBoot=nBoot, EVIestimator="Mom", h=h,
                    useKernel=useKernel, concent=concent, movThr=movThr,
                    TTs=c(100, 10000), timeRange=timeRange)

RLBoot <- output$RLBoot

PlotParamEstim(bootEstimates=output$xiBoot, thetaGrid=thetaVec, ylab=bquote(hat(xi)),
              alpha=0.05, ylim=NULL, cex.axis=15, cex.lab=2, thrWidth=2)

PlotParamEstim(bootEstimates=output$sigBoot, thetaGrid=thetaVec, ylab=bquote(hat(sigma)),
              alpha=0.05, ylim=NULL, cex.axis=15, cex.lab=2, thrWidth=2)

# 100-year level
PlotRL(RLBootList=RLBoot, thetaGrid=thetaVec, Data=Data, drc=drc,
      TTs=c(100, 10000), whichPlot=1, alpha=0.05, ylim=NULL,
      pointSize=1, cex.axis=15, cex.lab=2, thrWidth=2)
if(requireNamespace("plotly", quietly = TRUE)) {
  PolarPlotRL(RLBootList=RLBoot, thetaGrid=thetaVec, Data=Data, drc=drc,
             TTs=c(100, 10000), whichPlot=1, alpha=0.05, ylim=NULL,
             pointSize=4, fontSize=12, lineWidth=2)
} else {
  message("Skipping PolarPlotRL examples because the 'plotly' package is not installed.")
}

## See examples in vignette:
# vignette("localMethods", package = "circularEV")

```

PlotData

Plot of circular data

Description

Plot of circular data

Usage

```

PlotData(
  Data,
  drc,
  thr = NULL,
  ylim = NULL,
  pointSize = 4,
  cex.axis = 15,
  cex.lab = 2,
  thrWidth = 2,

```

```

    thrColor = "#D45E1A",
    thrLineType = 1,
    ylab = NULL
  )

```

Arguments

Data	Response variable
drc	Directional covariate
thr	Threshold values along thetaGrid
ylim	Range of values
pointSize	Size of points (observations)
cex.axis	Graphical parameter
cex.lab	Graphical parameter
thrWidth	Threshold width
thrColor	Threshold colour
thrLineType	Graphical parameter
ylab	y-axis label

Value

Plot of circular data, possibly including a threshold.

Examples

```

data(HsSP)
data(drc)

PlotData(Data=HsSP, drc=drc, thr=NULL, pointSize=1, cex.axis=15, cex.lab=2,
         thrWidth=2)

data(thresholdExampleML) # loads threshold example

PlotData(Data=HsSP, drc=drc, thr=thresholdExampleML, pointSize=1, cex.axis=15,
         cex.lab=2, thrWidth=2)

```

 PlotParamEstim

Plot of parameter estimates with bootstrap confidence intervals

Description

Plot of parameter estimates with bootstrap confidence intervals

Usage

```
PlotParamEstim(  
  bootEstimates,  
  thetaGrid = 1:360,  
  alpha = 0.05,  
  ylim = NULL,  
  cex.axis = 15,  
  cex.lab = 2,  
  thrWidth = 2,  
  ylab = NULL,  
  thrColor = "#D45E1A"  
)
```

Arguments

<code>bootEstimates</code>	Bootstrap estimates (for example, shape or scale)
<code>thetaGrid</code>	Grid values at which the estimation is performed
<code>alpha</code>	Significance level for the confidence intervals. Default to 0.05.
<code>ylim</code>	Range for the y-axis
<code>cex.axis</code>	Graphical parameter
<code>cex.lab</code>	Graphical parameter
<code>thrWidth</code>	Threshold width
<code>ylab</code>	y-axis label
<code>thrColor</code>	Threshold colour

Value

Plot of parameter estimates.

See Also

[SplineML](#) and [LocalEstim](#) for examples.

Examples

```
## See examples in vignettes:  
# vignette("localMethods", package = "circularEV")  
# vignette("splineML", package = "circularEV")
```

PlotRL *Plot of T-year levels*

Description

Plot of T-year levels

Usage

```
PlotRL(
  RLBootList,
  Data,
  drc,
  thetaGrid = 1:360,
  TTs,
  whichPlot,
  alpha = 0.05,
  ylim = NULL,
  pointSize = 1,
  cex.axis = 15,
  cex.lab = 2,
  thrWidth = 2,
  thrColor = "#D45E1A",
  ylab = NULL
)
```

Arguments

RLBootList	List containing bootstrap estimates of T-year levels
Data	Response variable
drc	Directional covariate
thetaGrid	Grid values at which the estimation is performed
TTs	T-year levels. For example, TTs = c(100, 10000).
whichPlot	Index identifying which T-year level should be plotted from TTs. If TTs = c(100, 10000), then whichPlot=2 produces a plot for the 10000-year level
alpha	Significance level for the confidence intervals. Default to 0.05.
ylim	Range for the y-axis
pointSize	Size of points (observations)
cex.axis	Graphical parameter
cex.lab	Graphical parameter
thrWidth	Threshold width
thrColor	Threshold colour
ylab	y-axis label

Value

Plot of T-year levels.

See Also

[SplineML](#) and [LocalEstim](#) for examples.

Examples

```
## See also examples in vignettes:
# vignette("localMethods", package = "circularEV")
# vignette("splineML", package = "circularEV")
```

PolarPlotData

Polar plot of circular data

Description

Polar plot of circular data

Usage

```
PolarPlotData(
  Data,
  drc,
  thr = NULL,
  ylim = NULL,
  pointSize = 1,
  fontSize = 12,
  thrWidth = 4,
  thrColor = "#D45E1A"
)
```

Arguments

Data	Response variable
drc	Directional covariate
thr	Threshold values along thetaGrid
ylim	Range of values
pointSize	Size of points (observations)
fontSize	Font size
thrWidth	Threshold width
thrColor	Threshold colour

Value

Polar plot of circular data, possibly including a threshold

Examples

```

data(HsSP)
data(drc)

if(requireNamespace("plotly", quietly = TRUE)) {
  PolarPlotData(Data=HsSP, drc=drc, thr=NULL, pointSize=4, fontSize=14,
                thrWidth=4, ylim=c(0,max(HsSP)))

  data(thresholdExampleML) # loads threshold example

  PolarPlotData(Data=HsSP, drc=drc, thr=thresholdExampleML, pointSize=4,
                fontSize=12, thrWidth=4, ylim=c(0,max(HsSP)))
} else {
  message("Skipping PolarPlotData examples because the 'plotly' package is not installed.")
}

```

PolarPlotRL

Polar plot of T-year levels

Description

Polar plot of T-year levels

Usage

```

PolarPlotRL(
  RLBootList,
  Data,
  drc,
  thetaGrid = 1:360,
  TTs,
  whichPlot,
  alpha = 0.05,
  ylim = NULL,
  pointSize = 4,
  fontSize = 12,
  lineWidth = 4
)

```

Arguments

RLBootList	List containing bootstrap estimates of T-year levels
Data	Response variable

drc	Directional covariate
thetaGrid	Grid values at which the estimation is performed
TTs	T-year levels. For example, TTs = c(100, 10000).
whichPlot	Index identifying which T-year level should be plotted from TTs. If TTs = c(100, 10000), then whichPlot=2 produces a plot for the 10000-year level
alpha	Significance level for the confidence intervals. Default to 0.05.
ylim	Range for the y-axis
pointSize	Size of points (observations)
fontSize	Font size
lineWidth	Threshold width

Value

Polar plot of T-year levels.

See Also

[SplineML](#) and [LocalEstim](#) for examples.

Examples

```
## See also examples in vignettes:
# vignette("localMethods", package = "circularEV")
# vignette("splineML", package = "circularEV")
```

SplineML

Spline ML fitting

Description

Spline ML fitting

Usage

```
SplineML(
  excesses,
  drc,
  thetaVec = 0:360,
  nBoot = 100,
  numIntKnots = 10,
  knotsType = "eqSpaced",
  lambda = seq(0, 2, by = 0.5),
  kappa = seq(0, 2, by = 0.5),
  nCandidatesInit = 1000,
  numCores = 2
)
```

Arguments

excesses	Excesses data
drc	Directional covariate
thetaVec	Grid values at which the threshold will be evaluated
nBoot	Number of bootstrap resamples
numIntKnots	Number of internal knots
knotsType	Position of knots. Default to "eqSpaced". Otherwise, the knots will be placed at the quantiles of observed directions.
lambda	Penalty parameter values for lambda
kappa	Penalty parameter values for kappa
nCandidatesInit	Number of initial parameter vectors. Optimisation will start with the best.
numCores	Number of CPU cores to be used

Details

See Konzen, E., Neves, C., and Jonathan, P. (2021). Modeling nonstationary extremes of storm severity: Comparing parametric and semiparametric inference. *Environmetrics*, 32(4), e2667.

Value

List of bootstrap estimates of shape and scale, and optimal values of lambda and kappa.

Examples

```
data(HsSP)
data(drc)
timeRange <- 54.5

idx <- order(drc)
drc <- drc[idx]
Data <- HsSP[idx]
set.seed(1234)
Data <- Data + runif(length(Data), -1e-4, 1e-4)

thetaVec <- 1:360

data(thresholdExampleML) # loads threshold example
thrResultML <- thresholdExampleML

lambda <- 100
kappa <- 40

thrPerObs <- thrResultML[drc]
excess <- Data - thrPerObs
drcExcess <- drc[excess>0]
excess <- excess[excess>0]
```

```

splineFit <- SplineML(excesses = excess, drc = drcExcess, nBoot = 30,
                     numIntKnots = 16, lambda=lambda, kappa=kappa, numCores=2)

xiBoot <- splineFit$xi
sigBoot <- splineFit$sig

PlotParamEstim(bootEstimates=xiBoot, thetaGrid=0:360, ylab=bquote(hat(xi)),
               alpha=0.05, ylim=NULL, cex.axis=15, cex.lab=2, thrWidth=2)

PlotParamEstim(bootEstimates=sigBoot, thetaGrid=0:360, ylab=bquote(hat(sigma)),
               alpha=0.05, ylim=NULL, cex.axis=15, cex.lab=2, thrWidth=2)

h <- 60 # needed for calculating local probability of exceedances
RLBoot <- CalcRLsplineML(Data=Data, drc=drc, xiBoot=xiBoot, sigBoot=sigBoot, h=h,
                        TTs=c(100, 10000), thetaGrid=thetaVec,
                        timeRange=timeRange, thr=thrResultML)

# 100-year level
PlotRL(RLBootList=RLBoot, thetaGrid=thetaVec, Data=Data, drc=drc,
       TTs=c(100, 10000), whichPlot=1, alpha=0.05, ylim=NULL,
       pointSize=1, cex.axis=15, cex.lab=2, thrWidth=2)
if(requireNamespace("plotly", quietly = TRUE)) {
  PolarPlotRL(RLBootList=RLBoot, thetaGrid=thetaVec, Data=Data, drc=drc,
              TTs=c(100, 10000), whichPlot=1, alpha=0.05, ylim=c(0, 25),
              pointSize=4, fontSize=12, lineWidth=2)
} else {
  message("Skipping PolarPlotRL example because the 'plotly' package is not installed.")
}

## See also examples in vignette:
# vignette("splineML", package = "circularEV")

```

thresholdExampleML *Threshold for spline ML and local ML examples*

Description

A vector of threshold values at directions 1,...,360. It is used for spline ML and local ML examples.

Usage

```
thresholdExampleML
```

Format

A vector of 360 values.

Details

It has been generated as follows:

```
data(HsSP)
data(drc)
timeRange <- 54.5

idx <- order(drc)
drc <- drc[idx]
Data <- HsSP[idx]
set.seed(1234)
Data <- Data + runif(length(Data), -1e-4, 1e-4)

thetaVec <- seq(1,360, by=5)

thresholdExampleML <- ThrSelection(Data=Data, drc=drc, h=60, b=0.35,
                                   thetaGrid=thetaVec, EVIestimator="ML",
                                   useKernel=TRUE, concent=10, bw=30, numCores=2)$thr
```

thresholdExampleMom *Threshold for local Moment examples*

Description

A vector of threshold values at directions 1,...,360. It is used for local Moment examples.

Usage

```
thresholdExampleMom
```

Format

A vector of 360 values.

Details

It has been generated as follows:

```
data(HsSP)
data(drc)
timeRange <- 54.5

idx <- order(drc)
```

```
drc <- drc[idx]
Data <- HsSP[idx]
set.seed(1234)
Data <- Data + runif(length(Data), -1e-4, 1e-4)

thetaVec <- 1:360

thresholdExampleMom <- ThrSelection(Data=Data, drc=drc, h=60, b=0.35,
                                   thetaGrid=thetaVec, EVIestimator="Mom",
                                   useKernel=TRUE, concent=10, bw=30, numCores=2)$thr
```

ThrSelection

Threshold selection

Description

This function selects a moving threshold for circular data using an automatic procedure for selecting the local number of exceedances

Usage

```
ThrSelection(
  Data,
  drc,
  h = 30,
  b = 0.35,
  thetaGrid,
  EVIestimator = "ML",
  useKernel = TRUE,
  concent = 10,
  bw = 30,
  numCores = 2
)
```

Arguments

Data	Response variable
drc	Directional covariate
h	Bandwidth value
b	Parameter used in the automatic procedure for selection of local number of exceedances
thetaGrid	Grid values at which the estimation is performed
EVIestimator	It can be either "ML" or "Mom"
useKernel	Logical. If TRUE (default), use kernel to assign weights depending on the directional distance.

concent	Concentration parameter value for von Mises kernel
bw	Bandwidth parameter value for smoothing the sample path of the selected threshold
numCores	Number of CPU cores to be used

Details

See Konzen, E., Neves, C., and Jonathan, P. (2021). Modeling nonstationary extremes of storm severity: Comparing parametric and semiparametric inference. *Environmetrics*, 32(4), e2667.

Value

List containing the selected threshold and selected number of local exceedances at each direction in the grid.

See Also

[PlotData](#) and [PolarPlotData](#) to see how the threshold can be visualised.

Examples

```
data(HsSP)
data(drc)
timeRange <- 54.5

idx <- order(drc)
drc <- drc[idx]
Data <- HsSP[idx]
set.seed(1234)
Data <- Data + runif(length(Data), -1e-4, 1e-4)

thetaVec <- 1:360

thrResultMom <- ThrSelection(Data=Data, drc=drc, h=60, b=0.35, thetaGrid=thetaVec,
  EVIestimator="Mom", useKernel=TRUE, concent=10, bw=30,
  numCores=2)$thr
thrResultML <- ThrSelection(Data=Data, drc=drc, h=60, b=0.35, thetaGrid=thetaVec,
  EVIestimator="ML", useKernel=TRUE, concent=10, bw=30,
  numCores=2)$thr

## See also examples in vignettes:
# vignette("localMethods", package = "circularEV")
# vignette("splineML", package = "circularEV")
```

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