

Package ‘jordan’

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Description A Jordan algebra is an algebraic object originally designed to study observables in quantum mechanics. Jordan algebras are commutative but non-associative; they satisfy the Jordan identity. The package follows the ideas and notation of K. McCrimmon (2004, ISBN:0-387-95447-3) ``A Taste of Jordan Algebras''. To cite the package in publications, please use Hankin (2023) <[doi:10.48550/arXiv.2303.06062](https://doi.org/10.48550/arXiv.2303.06062)>.

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VignetteBuilder knitr

Imports quadform,methods

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jordan-package	<i>A Suite of Routines for Working with Jordan Algebras</i>
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Description

A Jordan algebra is an algebraic object originally designed to study observables in quantum mechanics. Jordan algebras are commutative but non-associative; they satisfy the Jordan identity. The package follows the ideas and notation of K. McCrimmon (2004, ISBN:0-387-95447-3) "A Taste of Jordan Algebras". To cite the package in publications, please use Hankin (2023) <doi:10.48550/arXiv.2303.06062>.

Details

A *Jordan algebra* is a non-associative algebra over the reals with a multiplication that satisfies the following identities:

$$xy = yx$$

$$(xy)(xx) = x(y(xx))$$

(the second identity is known as the Jordan identity). In literature one usually indicates multiplication by juxtaposition but one sometimes sees $x \circ y$. Package idiom is to use an asterisk, as in `x*y`. There are five types of Jordan algebras:

1. Real symmetric matrices, class `real_symmetric_matrix`, abbreviated in the package to `rsm`
2. Complex Hermitian matrices, class `complex_herm_matrix`, abbreviated to `chm`
3. Quaternionic Hermitian matrices, class `quaternion_herm_matrix`, abbreviated to `qhm`
4. Albert algebras, the space of 3×3 octonionic matrices, class `albert`
5. Spin factors, class `spin`

(of course, the first two are special cases of the next). The `jordan` package provides functionality to manipulate jordan objects using natural R idiom.

Objects of all these classes are stored in dataframe (technically, a matrix) form with columns being elements of the jordan algebra.

The first four classes are matrix-based in the sense that the algebraic objects are symmetric or Hermitian matrices (the `S4` class is “`jordan_matrix`”). The fifth class, spin factors, is not matrix based.

One can extract the symmetric or Hermitian matrix from objects of class `jordan_matrix` using `as.list()`, which will return a list of symmetric or Hermitian matrices. A function name preceded by a “1” (for example `as.1matrix()` or `vec_to_qhm1()`) means that it deals with a single (symmetric or Hermitian) matrix.

Algebraically, the matrix form of `jordan_matrix` objects is redundant (for example, a `real_symmetric_matrix` of size $n \times n$ has only $n(n + 1)/2$ independent entries, corresponding to the upper triangular elements).

Author(s)

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References

K. McCrimmon 1978. “Jordan algebras and their applications”. *Bulletin of the American Mathematical Society*, Volume 84, Number 4.

Examples

```
rrsm()      # Random Real Symmetric matrices
rchm()      # Random Complex Hermitian matrices
rqhm()      # Random Quaternionic Hermitian matrices
ralbert()   # Random Albert algebra
rspin()     # Random spin factor

x <- rqhm(n=1)
y <- rqhm(n=1)
z <- rqhm(n=1)

x/1.2 + 0.3*x*y      # Arithmetic works as expected ...
x*(y*z) -(x*y)*z    # ... but '*' is not associative

## Verify the Jordan identity for type 3 algebras:

LHS <- (x*y)*(x*x)
RHS <- x*(y*(x*x))

diff <- LHS-RHS # zero to numerical precision

diff[1,drop=TRUE] # result in matrix form
```

Description

Methods for Arithmetic functions for jordans: +, -, *, /, ^

Usage

```

jordan_negative(z)
jordan_plus_jordan(e1,e2)
jordan_plus_numeric(e1,e2)
jordan_prod_numeric(e1,e2)
jordan_power_jordan(e1,e2)
albert_arith_albert(e1,e2)
albert_arith_numeric(e1,e2)
albert_inverse(e1)
albert_power_albert(...)
albert_power_numeric(e1,e2)
albert_power_single_n(e1,n)
albert_prod_albert(e1,e2)
chm_arith_chm(e1,e2)
chm_arith_numeric(e1,e2)
chm_inverse(e1)
chm_power_numeric(e1,e2)
chm_prod_chm(e1,e2)
numeric_arith_albert(e1,e2)
numeric_arith_chm(e1,e2)
numeric_arith_qhm(e1,e2)
numeric_arith_rsm(e1,e2)
qhm_arith_numeric(e1,e2)
qhm_arith_qhm(e1,e2)
qhm_inverse(x)
qhm_power_numeric(e1,e2)
qhm_prod_qhm(e1,e2)
rsm_arith_numeric(e1,e2)
rsm_arith_rsm(e1,e2)
rsm_inverse(e1)
rsm_power_numeric(e1,e2)
rsm_prod_rsm(e1,e2)
spin_plus_numeric(e1,e2)
spin_plus_spin(e1,e2)
spin_power_numeric(e1,e2)
spin_power_single_n(e1,n)
spin_power_spin(...)
spin_prod_numeric(e1,e2)
spin_prod_spin(e1,e2)

```

```

spin_inverse(...)
spin_negative(e1)
vec_albertprod_vec(x,y)
vec_chmprod_vec(x,y)
vec_qhmprod_vec(x,y)
vec_rsmprod_vec(x,y)

```

Arguments

z, e1, e2	Jordan objects or numeric vectors
n	Integer for powers
...	Further arguments (ignored)
x, y	Numeric vectors, Jordan objects in independent form

Details

The package implements the `Arith` group of S4 generics so that idiom like `A + B*C` works as expected with jordan.

Functions like `jordan_inverse()` and `jordan_plus_jordan()` are low-level helper functions. The only really interesting operation is multiplication; functions like `jordan_prod_jordan()`.

Names are implemented and the rules are inherited (via `onion::harmonize_oo()` and `onion::harmonize_on()`) from `rbind()`.

Value

generally return jordan

Author(s)

Robin K. S. Hankin

Examples

```

x <- rspin()
y <- rspin()
z <- rspin()

x*(y*(x*x)) - (x*y)*(x*x) # should be zero

x + y*z

```

c	<i>Concatenation</i>
---	----------------------

Description

Combines its arguments to form a single jordan object.

Usage

```
## S4 method for signature 'jordan'  
c(x,...)
```

Arguments

x, ... Jordan objects

Details

Returns a concatenated jordan of the same type as its arguments. Argument checking is not performed.

Value

Returns a Jordan object of the appropriate type (coercion is not performed)

Note

Names are inherited from the behaviour of cbind(), not c().

Author(s)

Robin K. S. Hankin

Examples

```
c(rqhm(),rqhm()*10)
```

Description

Various coercions needed in the package

Usage

```

as.jordan(x,class)
vec_to_rsm1(x)
vec_to_chm1(x)
vec_to_qhm1(x)
vec_to_albert1(x)
rsm1_to_vec(M)
chm1_to_vec(M)
qhm1_to_vec(M)
albert1_to_vec(H)
as.real_symmetric_matrix(x,d,single=FALSE)
as.complex_herm_matrix(x,d,single=FALSE)
as.quaternion_herm_matrix(x,d,single=FALSE)
as.albert(x,single=FALSE)
numeric_to_real_symmetric_matrix(x,d)
numeric_to_complex_herm_matrix(x,d)
numeric_to_quaternion_herm_matrix(x,d)
numeric_to_albert(e1)
as.list(x,...)
matrix1_to_jordan(x)

```

Arguments

x, e1	Numeric vector of independent entries
M, H	A matrix
d	Dimensionality of algebra
single	Boolean, indicating whether a single value is to be returned
class	Class of object
...	Further arguments, currently ignored

Details

The numeral “1” in a function name means that it operates on, or returns, a single element, usually a matrix. Thus function `as.1matrix()` is used to convert a jordan object to a list of matrices. Length one jordan objects are converted to a matrix.

Functions `vec_to_rsm1()` et seq convert a numeric vector to a (symmetric, complex, quaternion, octonion) matrix, that is, elements of a matrix-based Jordan algebra.

Functions `rsm1_to_vec()` convert a (symmetric, complex, quaternion, octonion) matrix to a numeric vector of independent components. The upper triangular components are used; no checking for symmetry is performed (the lower triangular components, and non-real components of the diagonal, are discarded).

Functions `as.real_symmetric_matrix()`, `as.complex_herm_matrix()`, `as.quaternion_herm_matrix()` and `as.albert()` take a numeric matrix and return a (matrix-based) Jordan object.

Functions `numeric_to_real_symmetric_matrix()` have not been coded up yet.

Function `matrix1_to_jordan()` takes a matrix and returns a length-1 (matrix based) Jordan vector. It uses the class of the entries (real, complex, quaternion, octonion) to decide which type of Jordan to return.

Value

Return a coerced value.

Author(s)

Robin K. S. Hankin

Examples

```
vec_to_chm1(1:16) # Hermitian matrix

as.1matrix(rchm())

as.complex_herm_matrix(matrix(runif(75), ncol=3))

matrix1_to_jordan(cprod(matrix(rnorm(35), 7, 5)))
matrix1_to_jordan(matrix(c(1, 1+1i, 1-1i, 3), 2, 2))
matrix1_to_jordan(0i1 + matrix(1, 3, 3))
```

Compare-methods

Methods for compare S4 group

Description

Methods for comparison (equal to, greater than, etc) of jordan. Only equality makes sense.

Usage

```
jordan_compare_jordan(e1, e2)
```

Arguments

e1, e2 Jordan objects

Value

Return a boolean

Examples

```
# rspin() > 0 # meaningless and returns an error
```

extract

Extract and replace methods for jordan objects

Description

Extraction and replace methods for jordan objects should work as expected.

Replace methods can take a jordan or a numeric, but the numeric must be zero.

Value

Generally return a jordan object of the same class as the first argument

Methods

```
[ signature(x = "albert", i = "index", j = "missing", drop = "logical"): ...
[ signature(x = "complex_herm_matrix", i = "index", j = "missing", drop = "logical"): ...
[ signature(x = "jordan", i = "index", j = "ANY", drop = "ANY"): ...
[ signature(x = "jordan", i = "index", j = "missing", drop = "ANY"): ...
[ signature(x = "quaternion_herm_matrix", i = "index", j = "missing", drop = "logical"):
...
[ signature(x = "real_symmetric_matrix", i = "index", j = "missing", drop = "logical"):
...
[ signature(x = "spin", i = "index", j = "missing", drop = "ANY"): ...
[ signature(x = "spin", i = "missing", j = "index", drop = "ANY"): ...
[<- signature(x = "albert", i = "index", j = "missing", value = "albert"): ...
[<- signature(x = "complex_herm_matrix", i = "index", j = "ANY", value = "ANY"): ...
[<- signature(x = "complex_herm_matrix", i = "index", j = "missing", value = "complex_herm_matrix"):
...
[<- signature(x = "jordan_matrix", i = "index", j = "missing", value = "numeric"): ...
[<- signature(x = "quaternion_herm_matrix", i = "index", j = "missing", value = "quaternion_herm_matrix"):
...
[<- signature(x = "real_symmetric_matrix", i = "index", j = "missing", value = "real_symmetric_matrix"):
...
[<- signature(x = "spin", i = "index", j = "index", value = "ANY"): ...
[<- signature(x = "spin", i = "index", j = "missing", value = "numeric"): ...
[<- signature(x = "spin", i = "index", j = "missing", value = "spin"): ...
```

Author(s)

Robin K. S. Hankin

Examples

```
showClass("index") # taken from the Matrix package

a <- rspin(7)
a[2:4] <- 0
a[5:7] <- a[1]*10
a
```

id

Multiplicative identities

Description

Multiplying a jordan object by the *identity* leaves it unchanged.

Usage

```
as.identity(x)
rsm_id(n,d)
chm_id(n,d)
qhm_id(n,d)
albert_id(n)
spin_id(n=3,d=5)
```

Arguments

n	Length of vector to be created
d	Dimensionality
x	In function <code>as.identity()</code> , a jordan object. Return value will be a jordan object of the same dimensionality but entries equal to the identity

Details

The identity object in the matrix-based classes (`jordan_matrix`) is simply the identity matrix. Function `as.identity()` takes an object of any of the five types (`rsm`, `chm`, `qhm`, `spin`, or `albert`) and returns a vector of the same length and type, but comprising identity elements.

Class `spin` has identity $(1, 0)$.

Value

A jordan object is returned.

Author(s)

Robin K. S. Hankin

Examples

```
x <- as.albert(matrix(sample(1:99,81,replace=TRUE),nrow=27))
I <- as.identity(x)
x == x*I # should be TRUE
```

```
rsm_id(6,3)
```

jordan

Create jordan objects

Description

Creation methods for jordan objects

Arguments

M	A matrix with columns representing independent entries in a matrix-based Jordan algebra
a, V	Scalar and vector components of a spin factor

Details

The functions documented here are the creation methods for the five types of jordan algebra.

- quaternion_herm_matrix()
- complex_herm_matrix()
- real_symmetric_matrix()
- albert()
- spin()

(to generate quick “get you going” Jordan algebra objects, use the rrrsm() family of functions, documented at random.Rd).

Value

Return jordans or Boolean as appropriate

Author(s)

Robin K. S. Hankin

See Also

[random](#)

Examples

```
A <- real_symmetric_matrix(1:10) # vector of length 1
as.1matrix(A)                   # in matrix form

complex_herm_matrix(cbind(1:25,2:26))
quaternion_herm_matrix(1:15)

albert(1:27)
spin(-6,cbind(1:12,12:1))

x <- rrsn() ; y <- rrsn() ; z <- rrsn() # also works with the other Jordans

x*(y*z) - (x*y)*z           # Jordan algebra is not associative...
(x*y)*(x*x) - x*(y*(x*x)) # but satisfies the Jordan identity
```

jordan-class

Classes in the "jordan" package

Description

Various classes in the **jordan** package.

Author(s)

Robin K. S. Hankin

References

K. McCrimmon 1978. "Jordan algebras and their applications". *Bulletin of the American Mathematical Society*, Volume 84, Number 4.

Examples

```
showClass("jordan")
```

misc	<i>Miscellaneous Jordan functionality</i>
------	---

Description

Miscellaneous Jordan functionality that should be documented somewhere

Usage

```
harmonize_spin_numeric(e1, e2)
harmonize_spin_spin(e1, e2)
```

Arguments

e1, e2 Objects to harmonize

Details

Miscellaneous low-level helper functions.

The harmonize functions `harmonize_spin_numeric()` and `harmonize_spin_spin()` work for spin objects for the matrix-based classes `onion::harmonize_oo()` and `onion::harmonize_on()` are used.

Value

These are mostly low-level helper functions; they not particularly user-friendly. They generally return either numeric or Jordan objects.

Author(s)

Robin K. S. Hankin

random	<i>Random Jordan objects</i>
--------	------------------------------

Description

Random jordan objects with specified properties

Usage

```
ralbert(n=3)
rrsm(n=3, d=5)
rchm(n=3, d=5)
rqhm(n=3, d=5)
rspin(n=3, d=5)
```

Arguments

n	Length of random object returned
d	Dimensionality of random object returned

Details

These functions give a quick “get you going” random Jordan object to play with.

Value

Return a jordan object

Author(s)

Robin K. S. Hankin

Examples

```
rism()
ralbert()
rspin()
```

r_to_n

Sizes of Matrix-based Jordan algebras

Description

Given the number of rows in a (matrix-based) Jordan object, return the size of the underlying associative matrix algebra

Usage

```
r_to_n_rsm(r)
r_to_n_chm(r)
r_to_n_qhm(r)
r_to_n_albert(r=27)
n_to_r_rsm(n)
n_to_r_chm(n)
n_to_r_qhm(n)
n_to_r_albert(n=3)
```

Arguments

n	Integer, underlying associative algebra being matrices of size $n \times n$
r	Integer, number of rows of independent representation of a matrix-based jordan object

Details

These functions are here for consistency, and the albert ones for completeness.

For the record, they are:

- Real symmetric matrices, `rsm`, $r = n(n + 1)/2$, $n = (\sqrt{1 + 4r} - 1)/2$
- Complex Hermitian matrices, `chm`, $r = n^2$, $n = \sqrt{r}$
- Quaternion Hermitian matrices, `qhm`, $r = n(2n - 1)$, $n = (1 + \sqrt{1 + 8r})/4$
- Albert algebras, $r = 27$, $n = 3$

Value

Return non-negative integers

Note

I have not been entirely consistent in my use of these functions.

Author(s)

Robin K. S. Hankin

Examples

```
r_to_n_qhm(nrow(rqhm()))
```

show

Print methods

Description

Show methods, to display objects at the prompt

Usage

```
albert_show(x)
spin_show(x)
jordan_matrix_show(x)
description(x, plural=FALSE)
```

Arguments

<code>x</code>	Jordan object
<code>plural</code>	Boolean, indicating whether plural form is to be given

Details

The special algebras use a bespoke show method, `jordan_matrix_show()` or `spin_show()`. If the number of elements is small, they display a concise representation and modify the row and column names of the underlying matrix slightly; spin factors are displayed with the scalar component offset from the vector component.

Print methods for special algebras are sensitive to the value of option `head_and_tail`, a two-element integer vector indicating the number of start lines and end lines to print.

Function `description()` gives a natural-language description of its argument, used in the print method.

Value

Returns the argument

Author(s)

Robin K. S. Hankin

Examples

```
rspin()
```

```
rqhm()
```

```
rchm()
```

valid

Validity methods

Description

Validity methods, to check that objects are well-formed

Usage

```
valid_rsm(object)  
valid_chm(object)  
valid_qhm(object)  
valid_albert(object)  
is_ok_rsm(r)  
is_ok_chm(r)  
is_ok_qhm(r)  
is_ok_albert(r)  
is_ok_rsm(r)
```

Arguments

object	Putative jordan object
r	Integer, number of rows in putative jordan object

Details

Validity methods. The `validity_foo()` functions test for an object to be the right type, and the `is_ok_foo()` functions test the number of rows being appropriate for a jordan object of some type; these functions return an error if not appropriate, or, for `jordan_matrix` objects, the size of the matrix worked with.

Value

Return a Boolean

Author(s)

Robin K. S. Hankin

Examples

```
is_ok_qhm(45) # 5x5 Hermitian quaternionic matrices
#is_ok_qhm(46) # FALSE
```

zero	<i>The zero Jordan object</i>
------	-------------------------------

Description

Package idiom for the zero Jordan object, and testing

Usage

```
is.zero(x)
is_zero_jordan(e1, e2=0)
```

Arguments

x, e1	Jordan object to test for zeroness
e2	Dummy numeric object to make the <code>Arith</code> method work

Details

One often wants to test a jordan object for being zero, and natural idiom would be `rchm()==0`. The helper function is `is_zero_jordan()`, and the generic is `is.zero()`.

Value

Returns a Boolean

Author(s)

Robin K. S. Hankin

Examples

```
rrsm()*0 == 0
```

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