

# Package ‘msPCA’

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**Type** Package

**Title** Sparse Principal Component Analysis with Multiple Principal Components

**Version** 0.4.0

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**Description** Implements an algorithm for computing multiple sparse principal components of a dataset. The method is based on Cory-Wright and Pauphilet ``Sparse PCA with Multiple Principal Components" (2026) <[doi:10.48550/arXiv.2209.14790](https://doi.org/10.48550/arXiv.2209.14790)>. The algorithm uses an iterative deflation heuristic with a truncated power method applied at each iteration to compute sparse principal components with controlled sparsity.

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**Imports** Rcpp (>= 1.0.11)

**LinkingTo** Rcpp, RcppEigen

**RoxygenNote** 7.3.3

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**NeedsCompilation** yes

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feasibility\_violation\_off  
*Feasibility violation*

---

### Description

Computes the feasibility violation defined as  $\sum_{t>s} u_t^\top u_s$  if orthogonality constraints are enforced (feasibilityConstraintType = 0) and  $\sum_{t>s} u_t^\top C u_s$  if zero-correlation constraints are enforced (feasibilityConstraintType = 1).

### Usage

```
feasibility_violation_off(C, U, feasibilityConstraintType)
```

### Arguments

**C** A matrix. The correlation or covariance matrix (p x p).

**U** A matrix. Each column correspond to an p-dimensional PC.

**feasibilityConstraintType**  
 An integer. Type of feasibility constraints to be enforced. 0: orthogonality constraints; 1: uncorrelatedness constraints.

### Value

A float.

### Examples

```
library(datasets)
TestMat <- cor(datasets::mtcars)
mspcares <- mspca(TestMat, 2, c(4,4))
feasibility_violation_off(TestMat, mspcares$x_best, 0)
```

---

fraction\_variance\_explained  
*Fraction of variance explained*

---

**Description**

Computes the fraction of variance explained (variance explained normalized by the trace of the covariance/correlation matrix) by a set of PCs.

**Usage**

```
fraction_variance_explained(C, U)
```

**Arguments**

C                    A matrix. The correlation or covariance matrix (p x p).  
U                    A matrix. The matrix containing the r PCs (p x r).

**Value**

A float.

**Examples**

```
library(datasets)
TestMat <- cor(datasets::mtcars)
mspcars <- mspca(TestMat, 2, c(4,4))
fraction_variance_explained(TestMat, mspcars$x_best)
```

---

fraction\_variance\_explained\_perPC  
*Fraction of variance explained per PC*

---

**Description**

Computes the fraction of variance explained (variance explained normalized by the trace of the covariance/correlation matrix) by each PC.

**Usage**

```
fraction_variance_explained_perPC(C, U)
```

**Arguments**

C                    A matrix. The correlation or covariance matrix (p x p).  
U                    A matrix. The matrix containing the r PCs (p x r).

**Value**

An array.

---

mspca

*Multiple Sparse PCA*


---

**Description**

Returns multiple sparse principal component of a matrix using an iterative deflation heuristic.

**Usage**

```
mspca(
  Sigma,
  r,
  ks,
  feasibilityConstraintType = 0L,
  verbose = TRUE,
  maxIter = 200L,
  feasibilityTolerance = 1e-04,
  stallingTolerance = 1e-08,
  timeLimitTPM = 20L,
  maxRestartTPM = 20L,
  minRestartTPM = 10L
)
```

**Arguments**

Sigma	A matrix. The correlation or covariance matrix, whose sparse PCs will be computed.
r	An integer. Number of principal components (PCs) to be computed.
ks	A list of integers. Target sparsity of each PC.
feasibilityConstraintType	(optional) An integer. Type of feasibility constraints to be enforced. 0: orthogonality constraints; 1: uncorrelatedness constraints. Default 0.
verbose	(optional) A Boolean. Controls console output. Default TRUE.
maxIter	(optional) An integer. Maximum number of iterations of the algorithm. Default 200.
feasibilityTolerance	(optional) A float. Tolerance for the violation of the orthogonality constraints. Default 1e-4
stallingTolerance	(optional) A float. Controls the objective improvement below which the algorithm is considered to have stalled. Default 1e-8

- `timeLimitTPM` (optional) An integer. Maximum time in seconds for the truncated power method (inner iteration). Default 20.
- `maxRestartTPM` (optional) An integer. Number of random restarts of the truncated power method (inner iteration) for the first outer iteration. Default 20.
- `minRestartTPM` (optional) An integer. Number of random restarts of the truncated power method (inner iteration) for outer iterations  $\geq 2$ . Default 10.

**Value**

An object with 4 fields: `'x_best'` (p x r array containing the sparse PCs), `'objective_value'`, `'feasibility_violation'`, `'runtime'`.

**Examples**

```
library(datasets)
TestMat <- cor(datasets::mtcars)
mspca(TestMat, 2, c(4,4))
```

---

<code>print_mspca</code>	<i>Print mspca output</i>
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---

**Description**

Displays the output of the msPCA algorithm.

**Usage**

```
print_mspca(sol_object, C)
```

**Arguments**

- `sol_object` A list. The output of the mspca or tpm function.
- `C` A matrix. The correlation or covariance matrix (p x p).

**Value**

None. Prints output to console.

**Examples**

```
library(datasets)
TestMat <- cor(datasets::mtcars)
mspcars <- mspca(TestMat, 2, c(4,4))
print_mspca(mspcars, TestMat)
```

---

tpm

*Truncated Power Method*

---

## Description

Returns the leading sparse principal component of a matrix using the truncated power method.

## Usage

```
tpm(Sigma, k, maxIter = 200L, verbose = TRUE, timeLimit = 10L)
```

## Arguments

Sigma	A matrix. The correlation or covariance matrix, whose sparse PCs will be computed.
k	An integer. Target sparsity of the PC.
maxIter	(optional) An integer. Maximum number of iterations of the algorithm. Default 200.
verbose	(optional) A Boolean. Controls console output. Default TRUE.
timeLimit	(optional) An integer. Maximum time in seconds. Default 10.

## Value

An object with 3 fields: 'x\_best' (p x 1 array containing the sparse PC), 'objective\_value', 'runtime'.

## References

Yuan, X. T., & Zhang, T. (2013). Truncated power method for sparse eigenvalue problems. *The Journal of Machine Learning Research*, 14(1), 899-925.

## Examples

```
library(datasets)
TestMat <- cor(datasets::mtcars)
tpm(TestMat, 4)
```

---

`variance_explained_perPC`  
*Variance explained per PC*

---

**Description**

Computes the variance explained by each PC.

**Usage**

`variance_explained_perPC(C, U)`

**Arguments**

- C            A matrix. The correlation or covariance matrix (p x p).
- U            A matrix. The matrix containing the r PCs (p x r).

**Value**

An array.

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