

Package ‘mycaas’

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Type Package

Title My Computerized Adaptive Assessment

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Description Implementation of adaptive assessment procedures based on Knowledge Space Theory (KST, Doignon & Falgout, 1999 <ISBN:9783540645016>) and Formal Psychological Assessment (FPA, Spoto, Stefanutti & Vidotto, 2010 <doi:10.3758/BRM.42.1.342>) frameworks. An adaptive assessment is a type of evaluation that adjusts the difficulty and nature of subsequent questions based on the test taker's responses to previous ones. The package contains functions to perform and simulate an adaptive assessment. Moreover, it is integrated with two 'Shiny' interfaces, making it both accessible and user-friendly. The package has been partially funded by the European Union - NextGenerationEU and by the Ministry of University and Research (MUR), National Recovery and Resilience Plan (NRRP), Mission 4, Component 2, Investment 1.5, project “RAISE - Robotics and AI for Socio-economic Empowerment” (ECS00000035).

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| | |
|-------------------|--|
| AA_knowledge_test | <i>Example of a test to showcase the Adaptive Assessment tools</i> |
|-------------------|--|

Description

The dataset contains a six items test concerning basic knowledge on computerized adaptive assessment. This test has been developed during the creation of this R package.

Usage

AA_knowledge_test

Format

A assessment object based on six multiple choice items.

states Structure with six items and twelve states.

likelihood Uniformly distributed across the states.

Stopping_rule The stopping rules is "likelihood_maximization" with a criterion of .5.

Question Six multiple choice items.

adaptive The value is set on TRUE allowing adaptive administration.

repetition The value is set on FALSE not allowing items repetition.

Source

Created to serve as an Example for this package.

Examples

```
data(AA_knowledge_test) #Lazy loading
```

 assessment

Assessment function

Description

Function that performs computerized assessment

Usage

```
assessment(
  likelihood = NA,
  states,
  beta,
  eta,
  questioning_rule = "half_split",
  termination = "likelihood_maximization",
  SC = 0.5,
  N_items = NULL,
  ki = 1,
  textq = NULL,
  textr = NULL,
  repetition = FALSE,
  adaptive = TRUE,
  simulation = TRUE,
  interactiveplot = FALSE
)
```

Arguments

| | |
|------------------|--|
| likelihood | A vector of the likelihood distribution on the states in the structure. |
| states | A state-by-problem matrix representing the structure, where an element is one if the item is included in the state, and zero otherwise. |
| beta | Vector of careless error probabilities. |
| eta | Vector of lucky guess error probabilities. |
| questioning_rule | A function which is used a questioning rules for the assessment. the default questioning rule is 'half_split'. |
| termination | Define and select one of the termination criteria: "likelihood_maximization" the assessment terminates when the likelihood of a knowledge state in a knowledge structure became higher of the termination criteria (Heller, and Repitsch, 2012). "items_discrimination" the assessment terminates if the marginal likelihood of all the items is outside the interval of the stopping criteria (Donadello, Spoto, Sambo, Badaloni, Granziol, Vidotto, 2017). |

| | |
|-----------------|---|
| SC | The Stopping criterion for the assessment is a numeric vector of values between 0 and 1. When the "termination" parameter is "likelihood_maximization" this is a single scalar that corresponds to the likelihood that a knowledge state needed to terminate the assessment. When the "termination" parameter is "items_discrimination" this is a numeric vector of length two, the assessment terminate if the the marginal likelihood of each item is outside of the interval between the two elements. |
| N_items | Number of items in the test. Optional entry in case of adaptive = FALSE. |
| ki | A number indicating the row in the structure to simulate as the true knowledge states. |
| textq | A character vector containing the text of the questions. |
| textr | A list containing for each question the correct and incorrect answers. |
| repetition | Logical value. When the value is TRUE the assessment procedure is allowed to administer the same item more then one time. |
| adaptive | Logical value. When the value is TRUE the assessment proceed with an adaptive procedure, otherwise the items presentation is randomized |
| simulation | Logical value. When the value is TRUE the assessment proceed with simulating a complete assessment with a user knowledge state define in variable ki. Otherwise the assessment collect answer from the user. |
| interactiveplot | Logical value. When the value is TRUE the knowledge structure is plot using a color thermometer scale to represents the likelihood of the states. |

Value

The outcome of a single assessment.

References

- Doignon, J.-P., & Falmagne, J.-C. (1999). Knowledge spaces. Springer.
- Donadello, I., Spoto, A., Sambo, F., Badaloni, S., Granzio, U., & Vidotto, G. (2017). ATS-PD: An adaptive testing system for psychological disorders. *Educational and psychological measurement*, 77(5), 792-815.
- Heller, J., & Repitsch, C. (2012). Exploiting prior information in stochastic knowledge assessment. *Methodology*.

Examples

```
# Example 1: From Brancaccio,de Chiusole, Stefanutti (2023)
# Consider the knowledge space and the parameters used in Brancaccio,
# de Chiusole, Stefanutti (2023) in Example 1

states<-matrix(c( 0,0,0,0,0,
                 0,0,0,0,1,
                 0,0,1,0,1,
                 0,0,0,1,1,
                 0,0,1,1,1,
                 1,0,1,0,1,
```

```

      0,1,0,1,1,
      1,0,1,1,1,
      0,1,1,1,1,
      1,1,0,1,1,
      1,1,1,1,1), byrow=TRUE, ncol=5)
beta <-c(.004,.03,.02,.01,.007)
eta <-c(5e-06, 5e-05, 4e-05,.007,.08)
likelihood <-rep(1,nrow(states))/nrow(states)
assessment(likelihood,states,beta,eta)

# Example 2: Random items presentation

assessment(N_items = 5 ,adaptive = FALSE)

# Example 3: Interactive mode on in the console

TextQuestion<-c("I frequently use computers.",
"I know how to build an assessment instrument (i.e., a paper-and-pencil questionnaire).",
"I can code and implement a 'for' loop (independently of its purpose).",
"When you administer an adaptive assessment, each question: ",
"I usually programme or code my assessment tools ",
"I add my assessment in a programme (i.e , google form) ")

TextResponse<-list(
correct=list("Yes","Yes","Yes","depend from the previous questions","Yes","Yes"),
incorrect=list(c("No"),c("No"),c("No"),c("is independent from the others questions",
"depend from the gender of the interviewed"),c("No"),c("No"))
)

map <- matrix(c(1,0,0,0,
0,1,0,0,
1,0,1,0,
0,1,0,1,
1,1,1,0,
1,1,0,0), ncol=4)

skillmap<-cbind(1:6,map)

states<-pks::delineate(skillmap)$K
rownames(states)<-NULL

eta <- rep(0.1,ncol(states))
beta <- rep(0.1,ncol(states))
likelihood <-rep(1,nrow(states))/nrow(states)

if(interactive()){token <- assessment(likelihood,states,beta,eta,textq=TextQuestion,
textr=TextResponse,simulation=FALSE)}

```

Description

Rule to select the most informative item at each step of the assessment.

Usage

```
half_split(likelihood, states, beta, eta, Q_pool = NA)
```

Arguments

| | |
|------------|---|
| likelihood | A vector of the likelihood distribution on the states in the structure. |
| states | A state-by-problem matrix representing the structure, where an element is one if the item is included in the state, and zero otherwise. |
| beta | Vector of careless error probabilities. |
| eta | Vector of lucky guess error probabilities. |
| Q_pool | A vector contains the pool of items for the assessment in this moment of the procedure. |

Value

The item that maximizes the information (for details see, Doignon and Falmagne, 2012).

References

Doignon, J.-P., & Falmagne, J.-C. (1999). Knowledge spaces. Berlin: Springer.

Examples

```
# Consider the knowledge space and the parameters used in Brancaccio,
# de Chiusole, Stefanutti (2023) in Example 1

states<-matrix(c( 0,0,0,0,0,
                 0,0,0,0,1,
                 0,0,1,0,1,
                 0,0,0,1,1,
                 0,0,1,1,1,
                 1,0,1,0,1,
                 0,1,0,1,1,
                 1,0,1,1,1,
                 0,1,1,1,1,
                 1,1,0,1,1,
                 1,1,1,1,1), byrow=TRUE, ncol=5)
beta <-c(.004,.03,.02,.01,.007)
eta <-c(5e-06, 5e-05, 4e-05,.007,.08)
likelihood <-c(0,0,0,0,0,1/3,0,1/3,0,0,1/3)
Q_pool <- c(2,4,5)
half_split(likelihood,states,beta,eta,Q_pool)
```

`performance_simulation`*Performance indexes*

Description

Simulation producing efficiency and accuracy performance curves and indexes based on simulated assessment of all the states in structure

Usage

```
performance_simulation(  
  states,  
  beta,  
  eta,  
  likelihood = NA,  
  questioning_rule = "half_split",  
  nrep = 1  
)
```

Arguments

| | |
|-------------------------------|---|
| <code>states</code> | A state-by-problem matrix representing the structure, where an element is one if the item is included in the state, and zero otherwise. |
| <code>beta</code> | Vector of careless error probabilities. |
| <code>eta</code> | Vector of lucky guess error probabilities. |
| <code>likelihood</code> | A vector of the likelihood for each state, if omitted the initial likelihood is assumed equally distributed. |
| <code>questioning_rule</code> | A function which is used a questioning rules for the assessment. the default questioning rule is 'half_split'. |
| <code>nrep</code> | Number of times in which each state is simulated. The default value is one. |

Value

Efficiency and Accuracy curves plots.

Examples

```
# Consider the knowledge space and the parameters used in Brancaccio,  
# de Chiusole, Stefanutti (2023) in Example 1  
  
states<-matrix(c( 0,0,0,0,0,  
                 0,0,0,0,1,  
                 0,0,1,0,1,  
                 0,0,0,1,1,
```

```

      0,0,1,1,1,
      1,0,1,0,1,
      0,1,0,1,1,
      1,0,1,1,1,
      0,1,1,1,1,
      1,1,0,1,1,
      1,1,1,1,1), byrow=TRUE, ncol=5)
beta <-c(.004,.03,.02,.01,.007)
eta <-c(5e-06, 5e-05, 4e-05,.007,.08)
performance_simulation(states,beta,eta)

```

| | |
|-----------------|----------------------|
| plot.assessment | <i>Plot (Method)</i> |
|-----------------|----------------------|

Description

Function used to plot an assessment object.

Usage

```

## S3 method for class 'assessment'
plot(x, bg_color = NULL, verices_color = "black", ...)

```

Arguments

| | |
|---------------|--|
| x | Assessment object to display. |
| bg_color | Background color. The default is white. |
| verices_color | Color of the nodes label. |
| ... | Additional arguments affecting the summary produced. |

Value

The function returns the graph representation of the structure.

Examples

```

# Example: Random items presentation

token<- assessment(N_items = 5 ,adaptive = FALSE)
plot(token)

```

| | |
|----------------|---------------------------|
| print_question | <i>Print the question</i> |
|----------------|---------------------------|

Description

Function to print in the console the item and collect the answer.

Usage

```
print_question(  
  TextQuestion,  
  TextResponse = list(correct = "correct", incorrect = c("wrong1", "wrong2", "wrong3"))  
)
```

Arguments

TextQuestion A character contain the text of the question.
TextResponse A list containing for each question the correct and incorrect answers.

Value

The answers of the question as numeric (1) if is correct and (0) if is false.

| | |
|----------------|--------------------------------|
| run_Assessment | <i>run Assessment shinyApp</i> |
|----------------|--------------------------------|

Description

This function run a shinyApp in which the is available: iii) The GUI implementation of the adaptive assessment

Usage

```
run_Assessment(file = NULL)
```

Arguments

file Logical value.

Value

The results of the assessment

Examples

```
# Try the test example yourself
data(AA_knowledge_test)
if(interactive()){
  run_Assessment(AA_knowledge_test)}
```

```
run_Practice          run Practice Assessment shinyApp
```

Description

This function run a shinyApp in which the following pages are available: i) a brief introduction of the assessment tools; ii) the GUI to create "assessment" files from a "csv" of items; iii) the GUI implementation of the adaptive assessment; and iv) the GUI implementation of the outcome.

Usage

```
run_Practice()
```

Value

The results of the assessment

Examples

```
# Try to build your test
if(interactive()){
  run_Practice()}
```

```
stopping_criterion   Stopping rule
```

Description

Rule to decide when terminate the assessment

Usage

```
stopping_criterion(
  likelihood,
  states,
  termination = "likelihood_maximization",
  SC = c(0.8)
)
```

Arguments

| | |
|-------------|--|
| likelihood | A vector of the likelihood distribution on the states in the structure. |
| states | A state-by-problem matrix representing the structure, where an element is one if the item is included in the state, and zero otherwise. |
| termination | Define and select one of the termination criteria: "likelihood_maximization" the assessment terminates when the likelihood of a knowledge state in a knowledge structure became higher of the termination criteria (Heller, and Repitsch, 2012). "items_discrimination" the assessment terminates if the marginal likelihood of all the items is outside the interval of the stopping criteria (Donadello, Spoto, Sambo, Badaloni, Granzio, Vidotto, 2017). |
| SC | The Stopping criterion for the assessment is a numeric vector of values between 0 and 1. When the "termination" parameter is "likelihood_maximization" this is a single scalar that corresponds to the likelihood that a knowledge state needed to terminates the assessment. When the "termination" parameter is "items_discrimination" this is a numeric vector of length two, the assessment terminate if the the marginal likelihood of each item is outside of the interval between the two elements. |

Value

Return TRUE if the assessment should terminates under the criteria, otherwise FALSE

References

Donadello, I., Spoto, A., Sambo, F., Badaloni, S., Granzio, U., & Vidotto, G. (2017). ATIS-PD: An adaptive testing system for psychological disorders. *Educational and psychological measurement*, 77(5), 792-815.

Heller, J., & Repitsch, C. (2012). Exploiting prior information in stochastic knowledge assessment. *Methodology*.

Examples

```
# Consider the knowledge space and the parameters used in Brancaccio,
# de Chiusole, Stefanutti (2023) in Example 1
```

```
states<-matrix(c( 0,0,0,0,0,
                 0,0,0,0,1,
                 0,0,1,0,1,
                 0,0,0,1,1,
                 0,0,1,1,1,
                 1,0,1,0,1,
                 0,1,0,1,1,
                 1,0,1,1,1,
                 0,1,1,1,1,
                 1,1,0,1,1,
                 1,1,1,1,1), byrow=TRUE, ncol=5)
beta <-c(.004,.03,.02,.01,.007)
eta <-c(5e-06, 5e-05, 4e-05,.007,.08)
likelihood <-c(0,0,0,0,0,0,0,.49,0,0,.51)
#stopping criterion based on the likelihood mode
```

```

stopping_criterion(likelihood,states, termination="likelihood_maximization" ,SC=c(0.5))
#stopping criterion based on the items marginal probabilities
stopping_criterion(likelihood,states, termination="items_discrimination" ,SC=c(0.2,0.8))

```

summary.assessment *Summary (Method)*

Description

Function used to produce result summaries of an assessment object.

Usage

```

## S3 method for class 'assessment'
summary(object, ...)

```

Arguments

object Assessment object to display
... Additional arguments affecting the summary produced.

Value

The function return a summary of the information in the a assessment object

Examples

```

# Example of random items presentation

token<- assessment(N_items = 5 ,adaptive = FALSE, ki=15)
summary(token)

```

updating *Updating rules*

Description

Multiplicative rule as in Falmagne and Doignon 2010 (Chapter 13, Section 10)

Usage

```

updating(likelihood, states, q, r_q, beta, eta)

```

Arguments

| | |
|------------|---|
| likelihood | A vector of the likelihood distribution on the states in the structure. |
| states | A state-by-problem matrix representing the structure, where an element is one if the item is included in the state, and zero otherwise. |
| q | Last administered item |
| r_q | Observed response to item q |
| beta | Vector of careless error probabilities |
| eta | Vector of lucky guess error probabilities |

Value

The updated likelihood distribution on the knowledge states

Examples

```
# Let consider the knowledge space and the parameters used in Brancaccio,
# de Chiusole, Stefanutti (2023) in Example 1
```

```
states<-matrix(c( 0,0,0,0,0,
                 0,0,0,0,1,
                 0,0,1,0,1,
                 0,0,0,1,1,
                 0,0,1,1,1,
                 1,0,1,0,1,
                 0,1,0,1,1,
                 1,0,1,1,1,
                 0,1,1,1,1,
                 1,1,0,1,1,
                 1,1,1,1,1), byrow=TRUE, ncol=5)
beta <-c(.004,.03,.02,.01,.007)
eta <-c(5e-06, 5e-05, 4e-05,.007,.08)
likelihood_0 <-rep(1,nrow(states))/nrow(states)
# Item asked
q = 3
# response observed
r_q = 1
likelihood_1 <- updating(likelihood_0,states,q,r_q,beta,eta)
```

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