

# Package ‘optconerrf’

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**Title** Optimal Monotone Conditional Error Functions

**Version** 1.0.2

**Description** Design and analysis of confirmatory adaptive clinical trials using the optimal conditional error framework according to Brannath and Bauer (2004) <[doi:10.1111/j.0006-341X.2004.00221.x](https://doi.org/10.1111/j.0006-341X.2004.00221.x)>. An extension to the optimal conditional error function using interim estimates as described in Brannath and Dreher (2024) <[doi:10.48550/arXiv.2402.00814](https://doi.org/10.48550/arXiv.2402.00814)> and functions to ensure that the resulting conditional error function is non-increasing are also available.

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|             |   |
|-------------|---|
| .rangeCheck | <i>Simple range check for numeric variables</i> |
|-------------|---|

---

### Description

This function performs very basic range checks for numeric variables and throws an error if the range is violated. A custom hint may be added to the message.

### Usage

```
.rangeCheck(variable, range, allowedEqual, hint = "")
```

### Arguments

|              |   |
|--------------|---|
| variable     | The (named) variable to be checked.                                       |
| range        | A vector of length 2 giving the minimum and maximum of the allowed range. |
| allowedEqual | Logical. Are the borders of range valid values?                           |
| hint         | Additional message that may be printed after the error.                   |

**Value**

Invisibly returns TRUE if the check was successful.

---

```
getDesignOptimalConditionalErrorFunction
```

*Create a design object for the optimal conditional error function.*

---

**Description**

This function returns a design object which contains all important parameters for the specification of the optimal conditional error function. The returned object is of class `TrialDesignOptimalConditionalError` and can be passed to other package functions.

**Usage**

```
getDesignOptimalConditionalErrorFunction(
  alpha,
  alpha1,
  alpha0,
  conditionalPower = NA_real_,
  delta1 = NA_real_,
  delta1Min = NA_real_,
  delta1Max = Inf,
  ncp1 = NA_real_,
  ncp1Min = NA_real_,
  ncp1Max = Inf,
  useInterimEstimate = TRUE,
  firstStageInformation,
  likelihoodRatioDistribution,
  minimumSecondStageInformation = 0,
  maximumSecondStageInformation = Inf,
  minimumConditionalError = 0,
  maximumConditionalError = 1,
  conditionalPowerFunction = NA,
  levelConstantMinimum = 0,
  levelConstantMaximum = 10,
  enforceMonotonicity = TRUE,
  ...
)
```

**Arguments**

|                     |   |
|---------------------|---|
| <code>alpha</code>  | The overall type I error rate $\alpha$ of the design. Must be a numeric value between 0 and 1.  |
| <code>alpha1</code> | Stage 1 efficacy boundary $\alpha_1$ (p-value scale). Must be a numeric value between 0 and 1. Should be smaller than <code>alpha0</code> . |

|  |  |
|--|--|
| <code>alpha0</code>                      | Binding stage 1 futility boundary $\alpha_0$ (p-value scale). Must be a numeric value between 0 and 1. Should be greater than <code>alpha1</code> . For use of a non-binding futility boundary, specify <code>alpha0=1</code> .  |
| <code>conditionalPower</code>            | The target conditional power $CP$ of the design. Must be a numeric value.  |
| <code>delta1</code>                      | Fixed effect assumption at which the conditional power should be achieved, expressed on the mean difference scale. Is only used if <code>useInterimEstimate=FALSE</code> . Alternatively, <code>ncp1</code> can be specified. Must be a numeric value greater than 0.  |
| <code>delta1Min</code>                   | The minimum for an interim estimate of the treatment effect, specified on the mean difference scale. If the interim estimate (on the mean difference scale) yields a value smaller than <code>delta1Min</code> , <code>delta1Min</code> is used for it. Is only used if <code>useInterimEstimate=TRUE</code> . Alternatively, <code>ncp1Min</code> can be specified. Must be a numeric value.  |
| <code>delta1Max</code>                   | The maximum for an interim estimate of the treatment effect, specified on the mean difference scale. If the interim estimate (on the mean difference scale) yields a value larger than <code>delta1Max</code> , <code>delta1Max</code> is used for it. Is only used if <code>useInterimEstimate=TRUE</code> . Alternatively, <code>ncp1Max</code> can be specified. Must be a numeric value. Default value is <code>Inf</code> , i.e., no upper restriction.                 |
| <code>ncp1</code>                        | Fixed effect assumption at which the conditional power should be achieved, expressed on the non-centrality parameter scale. Is only used if <code>useInterimEstimate=FALSE</code> . Alternatively, <code>delta1</code> can be specified. Must be a numeric value greater than 0.   |
| <code>ncp1Min</code>                     | The minimum for an interim estimate of the treatment effect, specified on the non-centrality parameter scale. If the interim estimate (on the non-centrality parameter scale) yields a value smaller than <code>ncp1Min</code> , <code>ncp1Min</code> is used for it. Is only used if <code>useInterimEstimate=TRUE</code> . Alternatively, <code>delta1Min</code> can be specified. Must be a numeric value.  |
| <code>ncp1Max</code>                     | The maximum for an interim estimate of the treatment effect, specified on the non-centrality parameter scale. If the interim estimate (on the non-centrality parameter scale) yields a value larger than <code>ncp1Max</code> , <code>ncp1Max</code> is used for it. Is only used if <code>useInterimEstimate=TRUE</code> . Alternatively, <code>delta1Max</code> can be specified. Must be a numeric value. Default value is <code>Inf</code> , i.e., no upper restriction. |
| <code>useInterimEstimate</code>          | Logical. Defines whether or not an interim estimate should be used for conditional power. If <code>TRUE</code> , a lower cut-off for the interim estimate must be specified by <code>delta1Min</code> or <code>ncp1Min</code> . An upper cut-off may also be specified by <code>delta1Max</code> or <code>ncp1Max</code> . If <code>FALSE</code> , the fixed effect size must be specified by <code>delta1</code> or <code>ncp1</code> .                                     |
| <code>firstStageInformation</code>       | Information of the first stage of the trial. Must be a positive numeric value.   |
| <code>likelihoodRatioDistribution</code> | The distribution to be used for the effect size of the likelihood ratio in the optimal conditional error function. Options are "fixed", "normal", "exp", "unif", "maxlr" for fixed effect size, normally distributed, exponentially distributed, uniformly distributed prior of the effect size and maximum likelihood ratio, respectively. Each case requires different additional specifications:  |

- `likelihoodRatioDistribution="fixed"` uses one (or more) fixed effect sizes for the likelihood ratio and requires the parameter `deltaLR` which provides the mean difference under which to calculate the likelihood ratio. If `deltaLR` contains multiple values, they may be weighted using an additional argument `weightsDeltaLR`. Omitting `weightsDeltaLR` automatically leads to equal weighting.
- `likelihoodRatioDistribution="normal"` uses a normal prior for the effect size and requires parameters `deltaLR` and `tauLR` for the mean and standard deviation of the normal distribution (both on mean difference scale).
- `likelihoodRatioDistribution="exp"` uses an exponential prior for the effect size and requires the parameter `kappaLR` which is the mean of the exponential distribution (on the mean difference scale).
- `likelihoodRatioDistribution="unif"` uses a uniform prior for the effect size and requires the specification of `deltaMaxLR`, which is the maximum of the support for the uniform likelihood ratio distribution (on the mean difference scale).
- `likelihoodRatioDistribution="maxlr"` estimates the non-centrality parameter to be used for the likelihood ratio from the data. No additional parameters must be specified.

`minimumSecondStageInformation`

The minimum information allowed in the second stage of the trial. Must be a numeric value. Default value is 0, i.e., no restriction.

`maximumSecondStageInformation`

The maximum information allowed in the second stage of the trial. Must be a numeric value. Default value is Inf, i.e., no restriction.

`minimumConditionalError`

Lower boundary for the optimal conditional error function. Default 0 (no restriction).

`maximumConditionalError`

Upper boundary for the optimal conditional error function. Default value is 1, however, the optimal conditional error function is inherently bounded by the conditional power.

`conditionalPowerFunction`

A user-specified function which calculates the conditional power from the first-stage p-value. This function should not be increasing in the first-stage p-value or monotonicity issues may occur.

`levelConstantMinimum`

The minimum of the interval on which the value for the level constant should be searched. Default value is 0.

`levelConstantMaximum`

The maximum of the interval on which the value for the level constant should be searched. Default value is 10.

`enforceMonotonicity`

Logical. Determines whether or not the optimal conditional error function should automatically be modified to be non-increasing. Default is TRUE.

... Additional arguments required for the specification of the likelihood ratio.

## Details

The design object contains the information required to determine the specific setting of the optimal conditional error function and can be passed to other package functions. From the given user specifications, the constant to achieve level condition for control of the overall type I error rate as well as the constants to ensure a non-increasing optimal CEF (if required) are automatically calculated.

## Value

An object of class `TrialDesignOptimalConditionalError`, which can be passed to other package functions.

## Likelihood ratio distribution

To calculate the optimal conditional error function, an assumption about the true parameter under which the second-stage information is to be minimised is required. Various options are available and can be specified via the argument `likelihoodRatioDistribution`:

- `likelihoodRatioDistribution="fixed"`: calculates the likelihood ratio for a fixed  $\Delta$ . The non-centrality parameter of the likelihood ratio  $\vartheta$  is then computed as `deltaLR*sqrt(firstStageInformation)` and the likelihood ratio is calculated as:

$$l(p_1) = e^{\Phi^{-1}(1-p_1)\vartheta - \vartheta^2/2}.$$

`deltaLR` may also contain multiple elements, in which case a weighted likelihood ratio is calculated for the given values. Unless positive weights that sum to 1 are provided by the argument `weightsDeltaLR`, equal weights are assumed.

- `likelihoodRatioDistribution="normal"`: calculates the likelihood ratio for a normally distributed prior of  $\vartheta$  with mean `deltaLR*sqrt(firstStageInformation)` ( $\mu$ ) and standard deviation `tauLR*sqrt(firstStageInformation)` ( $\sigma$ ). The parameters `deltaLR` and `tauLR` must be specified on the mean difference scale.

$$l(p_1) = (1 + \sigma^2)^{-\frac{1}{2}} \cdot e^{-(\mu/\sigma)^2/2 + (\sigma\Phi^{-1}(1-p_1) + \mu/\sigma)^2/(2 \cdot (1 + \sigma^2))}$$

- `likelihoodRatioDistribution="exp"`: calculates the likelihood ratio for an exponentially distributed prior of  $\vartheta$  with mean `kappaLR*sqrt(firstStageInformation)` ( $\eta$ ). The likelihood ratio is then calculated as:

$$l(p_1) = \kappa \cdot \sqrt{2\pi} \cdot e^{(\Phi^{-1}(1-p_1) - \eta)^2/2} \cdot \Phi(\Phi^{-1}(1-p_1) - \eta)$$

- `likelihoodRatioDistribution="unif"`: calculates the likelihood ratio for a uniformly distributed prior of  $\vartheta$  on the support  $[0, \Delta \cdot \sqrt{I_1}]$ , where  $\Delta$  is specified as `deltaMaxLR` and  $I_1$  is the `firstStageInformation`.

$$l(p_1) = \frac{\sqrt{2\pi}}{\Delta \cdot \sqrt{I_1}} \cdot e^{\Phi^{-1}(1-p_1)^2/2} \cdot (\Phi(\Delta \cdot \sqrt{I_1} - \Phi^{-1}(1-p_1)) - p_1)$$

- `likelihoodRatioDistribution="maxlr"`: the non-centrality parameter  $\vartheta$  is estimated from the data and no additional parameters must be specified. The likelihood ratio is estimated from the data as:

$$l(p_1) = e^{\max(0, \Phi^{-1}(1-p_1))^2/2}$$

The maximum likelihood ratio is always restricted to effect sizes  $\vartheta \geq 0$  (corresponding to  $p_1 \leq 0.5$ ).

### Effect for conditional power

For the treatment effect at which the target conditional power should be achieved, either a fixed effect or an interim estimate can be used. The usage of a fixed effect is indicated by setting `useInterimEstimate=FALSE`, in which case the fixed effect is provided by `delta1` on the mean difference scale or by `ncp1` on the non-centrality parameter scale (i.e.,  $\text{delta1} \cdot \sqrt{\text{firstStageInformation}}$ ). For an interim estimate, specified by `useInterimEstimate=TRUE`, a lower cut-off for the interim estimate must be provided, either by `delta1Min` on the mean difference scale, or `ncp1Min` on the non-centrality parameter scale. In addition, an upper limit of the estimate may be analogously provided by `delta1Max` or `ncp1Max`.

### Sample size and information

The first-stage information of the trial design must be specified to allow for calculations between the mean difference and non-centrality parameter scale. It is provided to the design object via `firstStageInformation`.

Listed below are some examples for the calculation between information ( $I_1$ ) and sample size:

- One-sample z-test with  $n$  total patients:  $I_1 = \frac{n}{\sigma^2}$ , where  $\sigma^2$  is the variance of an individual observation
- Balanced two-sample z-test with  $n_1$  patients per group:  $I_1 = \frac{1}{2} \cdot \frac{n_1}{\sigma^2}$ , where  $\sigma^2$  is the common variance
- General two-sample z-test with  $n_1, n_2$  patients per group:  $I_1 = 1 / (\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2})$ , where  $\sigma_1^2, \sigma_2^2$  are the group-wise variances

### Monotonicity

By default, the optimal conditional error function returned by `getDesignOptimalConditionalErrorFunction()` is transformed to be non-increasing in the first-stage p-value  $p_1$  if found to be increasing on any interval. The necessary intervals and constants for the transformation are calculated by `getMonotonisationConstants()`. Although not recommended for the operating characteristics of the design, the transformation may be omitted by setting `enforceMonotonicity=FALSE`.

### Constraints

In some applications, it may be feasible to restrict the optimal conditional error function by a lower and/or upper limit. These constraints can be directly implemented on the function by using the arguments `minimumConditionalError` and `maximumConditionalError`. By default, `minimumConditionalError=0` and `maximumConditionalError=1`, i.e., no constraints are applied. The constraints may also be specified on the second-stage information via `minimumSecondStageInformation` and `maximumSecondStageInformation`. If both `minimumConditionalError` and `minimumSecondStageInformation` respectively `maximumConditionalError` and `maximumSecondStageInformation` are provided, both constraints will be applied.

### Level constant

The level constant is determined by the helper function `getLevelConstant()`. It is identified using the `uniroot()` function and by default, the interval between 0 and 10 is searched for the level constant. In specific settings, the level constant may lie outside of this interval. In such cases, the search interval can be changed by altering the parameters `levelConstantMinimum` and `levelConstantMaximum`.

If inappropriate constraints to the optimal conditional error function are provided via `minimumConditionalError` and `maximumConditionalError` or `minimumSecondStageInformation` and `maximumSecondStageInformation`, it may be impossible to find a level constant which exhausts the full alpha level.

### Generic functions

The `print()` and `plot()` functions are available for objects of class `TrialDesignOptimalConditionalError`. For details, see `?print.TrialDesignOptimalConditionalError` and `?plot.TrialDesignOptimalConditionalError`.

### References

Brannath, W. & Bauer, P. (2004). Optimal conditional error functions for the control of conditional power. *Biometrics*. <https://www.jstor.org/stable/3695393>

Brannath, W., Dreher, M., zur Verth, J., Scharpenberg, M. (2024). Optimal monotone conditional error functions. <https://arxiv.org/abs/2402.00814>

### Examples

```
# Create a single-arm design with fixed parameter for the likelihood ratio
# and a fixed effect for conditional power. 80 patients are observed in the
# first-stage (firstStageInformation = 80 in the one-sample test, variance 1).
# The second-stage information is restricted to be between 40 and 160.
getDesignOptimalConditionalErrorFunction(
  alpha = 0.025, alpha1 = 0.001, alpha0 = 0.5, conditionalPower = 0.9,
  delta1 = 0.25, likelihoodRatioDistribution = "fixed", deltaLR = 0.25,
  firstStageInformation = 80, useInterimEstimate = FALSE,
  minimumSecondStageInformation = 40, maximumSecondStageInformation = 160
)

# Create a design comparing two groups using the maximum likelihood ratio
# and an interim estimate for the effect for conditional power.
# 160 patients per arm are observed in the first stage
# (firstStageInformation = 80 in the balanced two-sample test, variance 1).
getDesignOptimalConditionalErrorFunction(
  alpha = 0.025, alpha1 = 0.001, alpha0 = 0.5, conditionalPower = 0.9,
  delta1Min = 0.25, likelihoodRatioDistribution = "maxlr",
  firstStageInformation = 80, useInterimEstimate = TRUE
)
```

---

`getExpectedSecondStageInformation`

*Calculate Expected Second-stage Information*

---

### Description

Calculate the expected second-stage information using the optimal conditional error function with specific assumptions.

**Usage**

```

getExpectedSecondStageInformation(
    design,
    likelihoodRatioDistribution = NULL,
    ...
)

```

**Arguments**

**design** An object of class `TrialDesignOptimalConditionalError` created by `getDesignOptimalConditionalError`. Contains all necessary arguments to calculate the optimal conditional error function for the specified case.

**likelihoodRatioDistribution** The distribution to be used for the effect size of the likelihood ratio in the calculation of the expected second-stage information. Options are "fixed", "normal", "exp", "unif", "maxlr" for fixed effect size, normally distributed, exponentially distributed, uniformly distributed prior of the effect size and maximum likelihood ratio, respectively. Each case requires different additional specifications:

- `likelihoodRatioDistribution="fixed"` uses one (or more) fixed effect sizes for the likelihood ratio and requires the parameter `deltaLR` which provides the mean difference under which to calculate the likelihood ratio. If `deltaLR` contains multiple values, they may be weighted using an additional argument `weightsDeltaLR`. Omitting `weightsDeltaLR` automatically leads to equal weighting.
- `likelihoodRatioDistribution="normal"` uses a normal prior for the effect size and requires parameters `deltaLR` and `tauLR` for the mean and standard deviation of the normal distribution (both on mean difference scale).
- `likelihoodRatioDistribution="exp"` uses an exponential prior for the effect size and requires the parameter `kappaLR` which is the mean of the exponential distribution (on the mean difference scale).
- `likelihoodRatioDistribution="unif"` uses a uniform prior for the effect size and requires the specification of `deltaMaxLR`, which is the maximum of the support for the uniform likelihood ratio distribution (on the mean difference scale).
- `likelihoodRatioDistribution="maxlr"` estimates the non-centrality parameter to be used for the likelihood ratio from the data. No additional parameters must be specified.

The default is `likelihoodRatioDistribution=NULL`. In this case, the likelihood ratio distribution under which the expected second-stage information is calculated is taken directly from the design object.

... Additional parameters required for the specification of `likelihoodRatioDistribution`.

**Details**

The expected second-stage information is calculated as:

$$\mathbb{E}(I_2) = \int_{\alpha_1}^{\alpha_0} \frac{\nu(\alpha_2(p_1)) \cdot l(p_1)}{\Delta_1^2} dp_1,$$

where

- $\alpha_1, \alpha_0$  are the first-stage efficacy and futility boundaries
- $\alpha_2(p_1)$  is the optimal conditional error calculated for  $p_1$
- $l(p_1)$  is the "true" likelihood ratio under which to calculate the expected sample size. This can be different from the likelihood ratio used to calibrate the optimal conditional error function.
- $\Delta_1$  is the assumed treatment effect to power for, expressed as a mean difference. It may depend on the interim data (i.e.,  $p_1$ ) in case `useInterimEstimate = TRUE` was specified for the design object.
- $\nu(\alpha_2(p_1)) = (\Phi^{-1}(1 - \alpha_2(p_1)) + \Phi^{-1}(CP))^2$  is a factor calculated for the specific assumptions about the optimal conditional error function and the target conditional power  $CP$ .

**Value**

Expected second-stage information.

**References**

Brannath, W. & Bauer, P. (2004). Optimal conditional error functions for the control of conditional power. *Biometrics*. <https://www.jstor.org/stable/3695393>

**See Also**

[getDesignOptimalConditionalErrorFunction\(\)](#), [getSecondStageInformation\(\)](#)

**Examples**

```
# Get a design
design <- getDesignOptimalConditionalErrorFunction(
  alpha = 0.025, alpha1 = 0.001, alpha0 = 0.5, conditionalPower = 0.9,
  delta1 = 0.25, likelihoodRatioDistribution = "fixed", deltaLR = 0.25,
  firstStageInformation = 80, useInterimEstimate = FALSE,
)
# Calculate expected information under correct specification
getExpectedSecondStageInformation(design)

# Calculate expected information under the null hypothesis
getExpectedSecondStageInformation(
  design = design, likelihoodRatioDistribution = "fixed", deltaLR = 0
)
```

---

|                  |  |
|------------------|--|
| getLevelConstant | <i>Get Level Constant for Optimal Conditional Error Function</i> |
|------------------|--|

---

### Description

Find the constant required such that the conditional error function meets the overall level condition.

### Usage

```
getLevelConstant(design)
```

### Arguments

|        |  |
|--------|--|
| design | An object of class <code>TrialDesignOptimalConditionalError</code> created by <code>getDesignOptimalConditionalError</code> . Contains all necessary arguments to calculate the optimal conditional error function for the specified case. |
|--------|--|

### Details

The level condition is defined as:

$$\alpha = \alpha_1 + \int_{\alpha_1}^{\alpha_0} \alpha_2(p_1) dp_1.$$

The constant  $c_0$  of the optimal conditional error function is calibrated such that it meets the level condition. For a valid design, the additional following condition must be met to be able to exhaust the level  $\alpha$ :

$$\alpha_1 + CP(\alpha_0 - \alpha_1) > \alpha.$$

This condition is checked by `getLevelConstant()` and the execution is terminated if it is not met. In case a conditional power function is used, the condition is instead:

$$\alpha_1 + \int_{\alpha_1}^{\alpha_0} CP(p_1) dp_1 > \alpha.$$

### Value

A list that contains the constant (element `$root`) and other components provided by `uniroot()`. The level constant is calculated corresponding to the mean difference scale.

### References

- Brannath, W. & Bauer, P. (2004). Optimal conditional error functions for the control of conditional power. *Biometrics*. <https://www.jstor.org/stable/3695393>
- Brannath, W., Dreher, M., zur Verth, J., Scharpenberg, M. (2024). Optimal monotone conditional error functions. <https://arxiv.org/abs/2402.00814>

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|                                 |                                   |
|---------------------------------|-----------------------------------|
| <code>getLikelihoodRatio</code> | <i>Calculate Likelihood Ratio</i> |
|---------------------------------|-----------------------------------|

---

### Description

Calculate the likelihood ratio of a p-value for a given distribution.

### Usage

```
getLikelihoodRatio(firstStagePValue, design)
```

### Arguments

`firstStagePValue`

First-stage p-value or p-values. Must be a numeric vector between 0 and 1.

`design`

An object of class `TrialDesignOptimalConditionalError` created by `getDesignOptimalConditionalError`. Contains all necessary arguments to calculate the optimal conditional error function for the specified case.

### Details

The calculation of the likelihood ratio for a first-stage p-value  $p_1$  is done based on a distributional assumption, specified in the design object. The different options require different parameters, elaborated in the following.

- `likelihoodRatioDistribution="fixed"`: calculates the likelihood ratio for a fixed  $\Delta$ . The non-centrality parameter of the likelihood ratio  $\vartheta$  is then computed as `deltaLR*sqrt(firstStageInformation)` and the likelihood ratio is calculated as:

$$l(p_1) = e^{\Phi^{-1}(1-p_1)\vartheta - \vartheta^2/2}.$$

`deltaLR` may also contain multiple elements, in which case a weighted likelihood ratio is calculated for the given values. Unless positive weights that sum to 1 are provided by the argument `weightsDeltaLR`, equal weights are assumed.

- `likelihoodRatioDistribution="normal"`: calculates the likelihood ratio for a normally distributed prior of  $\vartheta$  with mean `deltaLR*sqrt(firstStageInformation)` ( $\mu$ ) and standard deviation `tauLR*sqrt(firstStageInformation)` ( $\sigma$ ). The parameters `deltaLR` and `tauLR` must be specified on the mean difference scale.

$$l(p_1) = (1 + \sigma^2)^{-\frac{1}{2}} \cdot e^{-(\mu/\sigma)^2/2 + (\sigma\Phi^{-1}(1-p_1) + \mu/\sigma)^2/(2 \cdot (1 + \sigma^2))}$$

- `likelihoodRatioDistribution="exp"`: calculates the likelihood ratio for an exponentially distributed prior of  $\vartheta$  with mean `kappaLR*sqrt(firstStageInformation)` ( $\eta$ ). The likelihood ratio is then calculated as:

$$l(p_1) = \eta \cdot \sqrt{2\pi} \cdot e^{(\Phi^{-1}(1-p_1) - \eta)^2/2} \cdot \Phi(\Phi^{-1}(1-p_1) - \eta)$$

- `likelihoodRatioDistribution="unif"`: calculates the likelihood ratio for a uniformly distributed prior of  $\vartheta$  on the support  $[0, \Delta \cdot \sqrt{I_1}]$ , where  $\Delta$  is specified as `deltaMaxLR` and  $I_1$  is the `firstStageInformation`.

$$l(p_1) = \frac{\sqrt{2\pi}}{\Delta \cdot \sqrt{I_1}} \cdot e^{\Phi^{-1}(1-p_1)^2/2} \cdot (\Phi(\Delta \cdot \sqrt{I_1} - \Phi^{-1}(1-p_1)) - p_1)$$

- `likelihoodRatioDistribution="maxlr"`: the non-centrality parameter  $\vartheta$  is estimated from the data and no additional parameters must be specified. The likelihood ratio is estimated from the data as:

$$l(p_1) = e^{\max(0, \Phi^{-1}(1-p_1))^2/2}$$

The maximum likelihood ratio is always restricted to effect sizes  $\vartheta \geq 0$  (corresponding to  $p_1 \leq 0.5$ ).

### Value

The value of the likelihood ratio for the given specification.

### References

Brannath, W. & Bauer, P. (2004). Optimal conditional error functions for the control of conditional power. *Biometrics*. <https://www.jstor.org/stable/3695393>

Hung, H. M. J., O'Neill, R. T., Bauer, P. & Kohne, K. (1997). The behavior of the p-value when the alternative hypothesis is true. *Biometrics*. <https://www.jstor.org/stable/2533093>

### Examples

```
# Get a design
design <- getDesignOptimalConditionalErrorFunction(
  alpha = 0.025, alpha1 = 0.001, alpha0 = 0.5, conditionalPower = 0.9,
  delta1 = 0.25, likelihoodRatioDistribution = "fixed", deltaLR = 0.25,
  firstStageInformation = 80, useInterimEstimate = FALSE,
)

getLikelihoodRatio(firstStagePValue = c(0.05, 0.1, 0.2), design = design)
```

---

`getMonotoneFunction`     *Return Monotone Function Values*

---

### Description

Applies the provided monotonisation constants to a specified, possibly non-monotone function. The returned function values are non-increasing.

**Usage**

```

getMonotoneFunction(
  x,
  fun,
  lower = NULL,
  upper = NULL,
  argument = NULL,
  nSteps = 10^4,
  epsilon = 10^(-5),
  numberOfIterationsQ = 10^4,
  design
)

```

**Arguments**

|                     |  |
|---------------------|--|
| x                   | Argument values.   |
| fun                 | The function to be made monotone.  |
| lower               | The lower limit of the interval on which the function should be monotonised. Must be a numeric value.  |
| upper               | The upper limit of the interval on which the function should be monotonised.   |
| argument            | The argument in which the function should be monotonised, given as a character.  |
| nSteps              | The number of steps to be taken when checking the function for monotonicity. Must be a numeric value. Default 10^4.  |
| epsilon             | Maximum allowed difference between the initial and monotone integral. Must be a numeric value. Default 10^-5.  |
| numberOfIterationsQ | Maximum number of iterations allowed to determine each value of q. Must be a numeric value. Default 10^4.  |
| design              | An object of class <code>TrialDesignOptimalConditionalError</code> created by <code>getDesignOptimalConditionalError</code> . Contains all necessary arguments to calculate the optimal conditional error function for the specified case. |

**Details**

The exact monotonisation process is outlined in Brannath et al. (2024), but specified in terms of the first-stage test statistic  $z_1$  rather than the first-stage p-value  $p_1$ .

The algorithm can easily be translated to the use of p-values by switching the maximum and minimum functions, i.e., replacing  $\min\{q, Q(z_1)\}$  by  $\max\{q, Q(p_1)\}$  and  $\min\{q, Q(z_1)\}$  by  $\max\{q, Q(p_1)\}$ .

**Value**

Monotone function values.

**References**

Brannath, W., Dreher, M., zur Verth, J., Scharpenberg, M. (2024). Optimal monotone conditional error functions. <https://arxiv.org/abs/2402.00814>

---

 getMonotonisationConstants

*Calculate the Constants for Monotonisation*


---

### Description

Computes the constants required to make a function non-increasing on the specified interval. The output of this function is necessary to calculate the monotone optimal conditional error function. The output object is a list that contains the intervals on which constant values are required, specified by the minimum dls and maximum dus of the interval and the respective constants, qs.

### Usage

```
getMonotonisationConstants(
  fun,
  lower = 0,
  upper = 1,
  argument,
  nSteps = 10^4,
  epsilon = 10^(-5),
  numberOfIterationsQ = 10^4,
  design
)
```

### Arguments

|                     |   |
|---------------------|---|
| fun                 | The function to be made monotone.   |
| lower               | The lower limit of the interval on which the function should be monotonised. Must be a numeric value.   |
| upper               | The upper limit of the interval on which the function should be monotonised.  |
| argument            | The argument in which the function should be monotonised, given as a character.   |
| nSteps              | The number of steps to be taken when checking the function for monotonicity. Must be a numeric value. Default 10 <sup>4</sup> .   |
| epsilon             | Maximum allowed difference between the initial and monotone integral. Must be a numeric value. Default 10 <sup>-5</sup> .   |
| numberOfIterationsQ | Maximum number of iterations allowed to determine each value of q. Must be a numeric value. Default 10 <sup>4</sup> .   |
| design              | An object of class TrialDesignOptimalConditionalError created by getDesignOptimalConditionalError. Contains all necessary arguments to calculate the optimal conditional error function for the specified case. |

### Value

A list containing the monotonisation constants (element \$qs) and the intervals on which they must be applied, specified via minimum (element qls) and maximum (element qus).

## References

Brannath, W., Dreher, M., zur Verth, J., Scharpenberg, M. (2024). Optimal monotone conditional error functions. <https://arxiv.org/abs/2402.00814>

---

getNu

*Calculate Nu*

---

## Description

Calculate the factor which relates  $\alpha_2$  to the second-stage information for given conditional power.

## Usage

```
getNu(alpha, conditionalPower)
```

## Arguments

alpha                    The (conditional) type I error rate of the design. Must be a numeric vector with values between 0 and 1.

conditionalPower        The target conditional power  $CP$  of the design. Must be a numeric value.

## Details

Note that this function uses factor 1 instead of factor 2 (Brannath & Bauer 2004). This has no impact on the optimal conditional error function, as constant factors are absorbed by the level constant  $c_0$ . The calculation is:

$$\nu(\alpha_2(p_1)) = (\Phi^{-1}(1 - \alpha_2(p_1)) + \Phi^{-1}(CP))^2.$$

## Value

Factor linking information and  $\alpha_2$ .

## References

Brannath, W. & Bauer, P. (2004). Optimal conditional error functions for the control of conditional power. *Biometrics*. <https://www.jstor.org/stable/3695393>

## Examples

```
getNu(alpha = 0.05, conditionalPower = 0.9)

# Returns 0 if alpha exceeds conditionalPower
getNu(alpha = 0.8, conditionalPower = 0.7)
```

---

`getNuPrime`*Calculate the Derivate of Nu*

---

**Description**

Calculates the derivative of nu for a given conditional error and conditional power.

**Usage**

```
getNuPrime(alpha, conditionalPower)
```

**Arguments**

`alpha` The (conditional) type I error rate of the design. Must be a numeric vector with values between 0 and 1.

`conditionalPower` The target conditional power  $CP$  of the design. Must be a numeric value.

**Details**

The function  $\nu'$  is defined as

$$\nu'(p_1) = -2 \cdot (\Phi^{-1}(1 - \alpha_2(p_1)) + \Phi^{-1}(CP)) / \phi(\Phi^{-1}(1 - \alpha_2(p_1))).$$

Note that in this implementation, the the factor -2 is used instead of -4, which is used in by Brannath & Bauer (2004), who explicitly investigate the setting of a balanced two-group trial. The argument `conditionalPower` is either the fixed target conditional power or the value of the conditional power function at the corresponding first-stage p-value.

**Value**

Value for nu prime.

**References**

Brannath, W. & Bauer, P. (2004). Optimal conditional error functions for the control of conditional power. *Biometrics*. <https://www.jstor.org/stable/3695393>

**Examples**

```
getNuPrime(alpha = 0.05, conditionalPower = 0.9)
```

---

```
getOptimalConditionalError
```

*Calculate the Optimal Conditional Error*

---

### Description

Calculate the Optimal Conditional Error

### Usage

```
getOptimalConditionalError(firstStagePValue, design)
```

### Arguments

firstStagePValue

First-stage p-value or p-values. Must be a numeric vector between 0 and 1.

design

An object of class `TrialDesignOptimalConditionalError` created by `getDesignOptimalConditionalErrorFunction`. Contains all necessary arguments to calculate the optimal conditional error function for the specified case.

### Details

The optimal conditional error  $\alpha_2$  given a first-stage p-value  $p_1$  is calculated as:

$$\alpha_2(p_1) = \psi\left(-e^{c_0} \cdot \frac{\Delta_1^2}{l(p_1)}\right).$$

The level constant  $c_0$  as well as the specification of the effect size  $\Delta_1$  and the likelihood ratio  $l(p_1)$  must be contained in the design object (see `?getDesignOptimalConditionalErrorFunction`). Early stopping rules are supported, i.e., for  $p_1 \leq \alpha_1$ , the returned conditional error is 1 and for  $p_1 > \alpha_0$ , the returned conditional error is 0.

### Value

Value of the optimal conditional error function.

### References

Brannath, W. & Bauer, P. (2004). Optimal conditional error functions for the control of conditional power. *Biometrics*. <https://www.jstor.org/stable/3695393>

### See Also

[getDesignOptimalConditionalErrorFunction\(\)](#)

**Examples**

```
# Create a design
design <- getDesignOptimalConditionalErrorFunction(
  alpha = 0.025, alpha1 = 0.001, alpha0 = 0.5, conditionalPower = 0.9,
  delta1 = 0.5, firstStageInformation = 40, useInterimEstimate = FALSE,
  likelihoodRatioDistribution = "fixed", deltaLR = 0.5)

# Calculate optimal conditional error
getOptimalConditionalError(
  firstStagePValue = c(0.1, 0.2, 0.3), design = design
)
```

---

|                 |                                    |
|-----------------|------------------------------------|
| getOverallPower | <i>Calculate the overall power</i> |
|-----------------|------------------------------------|

---

**Description**

Calculate the overall power and other operating characteristics of a design.

**Usage**

```
getOverallPower(design, alternative)
```

**Arguments**

|             |  |
|-------------|--|
| design      | An object of class <code>TrialDesignOptimalConditionalError</code> created by <code>getDesignOptimalConditionalErrorFunction()</code> . Contains all necessary arguments to calculate the optimal conditional error function for the specified case. |
| alternative | Assumed relative effect size.  |

**Details**

This function is used to evaluate the overall performance of a design. The probabilities for first-stage futility, first-stage efficacy and overall efficacy (i.e., overall power) are saved in an object of class `PowerResultsOptimalConditionalError`.

**Value**

The overall power of the design at the provided effect size.

**See Also**

[getDesignOptimalConditionalErrorFunction\(\)](#), [getSimulationResults\(\)](#)

**Examples**

```
# Get a design
design <- getDesignOptimalConditionalErrorFunction(
  alpha = 0.025, alpha1 = 0.001, alpha0 = 0.5, conditionalPower = 0.9,
  delta1 = 0.25, likelihoodRatioDistribution = "fixed", deltaLR = 0.25,
  firstStageInformation = 80, useInterimEstimate = FALSE,
)

getOverallPower(design, alternative = 0.25)
```

---

getPsi

*Calculate Psi, the Inverse of Nu Prime*


---

**Description**

Get point-wise values of psi (inverse of nu prime)

**Usage**

```
getPsi(nuPrime, conditionalPower)
```

**Arguments**

nuPrime            The function value to be inverted.  
conditionalPower    The target conditional power  $CP$  of the design. Must be a numeric value.

**Details**

The function  $\psi$  is the inverse of:

$$\nu'(\alpha) = -2 \cdot (\Phi^{-1}(1 - \alpha) + \Phi^{-1}(1 - CP)) / \phi(\Phi^{-1}(1 - \alpha))$$

. If the conditional power  $CP$  lies outside of the range  $1 - \Phi(2) \leq CP \leq \Phi(2)$ , the calculation is slightly more complicated. The argument conditionalPower is either the fixed target conditional power or the value of the conditional power function at the corresponding first-stage p-value.

**Value**

The value of alpha which corresponds to nuPrime and lies between 0 and conditionalPower.

**Examples**

```
# Returns 0.05
getPsi(getNuPrime(alpha = 0.05, conditionalPower = 0.9), conditionalPower = 0.9)
```

---

 getQ

*Calculate Q*


---

**Description**

Calculate the ratio of likelihood ratio and squared effect size.

**Usage**

```
getQ(firstStagePValue, design)
```

**Arguments**

firstStagePValue

First-stage p-value or p-values. Must be a numeric vector between 0 and 1.

design

An object of class `TrialDesignOptimalConditionalError` created by `getDesignOptimalConditionalErrorFunction()`. Contains all necessary arguments to calculate the optimal conditional error function for the specified case.

**Details**

For more information on how to specify the likelihood ratio, see `?getLikelihoodRatio()`. In case the optimal conditional error function is ever increasing in the first-stage p-value  $p_1$ , a monotone transformation of `getQ()` is needed for logical consistency and type I error rate control.

The formula for  $Q(p_1)$  is:

$$Q(p_1) = l(p_1) / \Delta_1^2,$$

where  $l(p_1)$  is the likelihood ratio and  $\Delta_1$  is the effect size at which the conditional power should be achieved. The effect size may also depend on the interim data (i.e., on  $p_1$ ) in case `useInterimEstimate = TRUE` was specified for the design object.

**Value**

Ratio of likelihood ratio and squared effect size.

**References**

Brannath, W., Dreher, M., zur Verth, J., Scharpenberg, M. (2024). Optimal monotone conditional error functions. <https://arxiv.org/abs/2402.00814>

**Examples**

```
# Get a design
design <- getDesignOptimalConditionalErrorFunction(
  alpha = 0.025, alpha1 = 0.001, alpha0 = 0.5, conditionalPower = 0.9,
  delta1 = 0.25, likelihoodRatioDistribution = "fixed", deltaLR = 0.25,
  firstStageInformation = 80, useInterimEstimate = FALSE,
)
```

```
getQ(firstStagePValue = c(0.05, 0.1, 0.2), design = design)
```

---

```
getSecondStageInformation
```

*Calculate the Second-stage Information*

---

### Description

Calculate second-stage information for given first-stage p-value and design.

### Usage

```
getSecondStageInformation(firstStagePValue, design)
```

### Arguments

firstStagePValue

First-stage p-value or p-values. Must be a numeric vector between 0 and 1.

design

An object of class `TrialDesignOptimalConditionalError` created by `getDesignOptimalConditionalError`. Contains all necessary arguments to calculate the optimal conditional error function for the specified case.

### Details

The second-stage information  $I_2$  is calculated given a first-stage p-value  $p_1$  as:

$$I_2(p_1) = \frac{(\Phi^{-1}(1 - \alpha_2(p_1)) + \Phi^{-1}(CP))^2}{\Delta_1^2} = \frac{\nu(\alpha_2(p_1))}{\Delta_1^2},$$

where

- $\alpha_2(p_1)$  is the conditional error function
- $CP$  is the target conditional power
- $\Delta_1$  is the assumed treatment effect (expressed as a mean difference).

The conditional error is calculated according to the specification provided in the design argument. For p-values smaller or equal to the first-stage efficacy boundary as well as p-values greater than the first-stage futility boundary, the returned information is 0 (since the trial is ended early in both cases).

### Value

The second-stage information.

### References

Brannath, W. & Bauer, P. (2004). Optimal conditional error functions for the control of conditional power. *Biometrics*. <https://www.jstor.org/stable/3695393>

**See Also**

[getDesignOptimalConditionalErrorFunction\(\)](#), [getExpectedSecondStageInformation\(\)](#), [getOptimalConditional](#)

**Examples**

```
design <- getDesignOptimalConditionalErrorFunction(
  alpha = 0.025, alpha1 = 0.001, alpha0 = 0.5,
  conditionalPower = 0.9, delta1 = 0.25, useInterimEstimate = FALSE,
  firstStageInformation = 40, likelihoodRatioDistribution = "maxlr"
)

getSecondStageInformation(
  firstStagePValue = c(0.05, 0.1, 0.2), design = design
)
```

---

getSimulationResults    *Simulate trials*

---

**Description**

Simulate the rejection probability for a given design and alternative.

**Usage**

```
getSimulationResults(
  design,
  maxNumberOfIterations = 10000,
  alternative,
  seed = NULL
)
```

**Arguments**

|                       |  |
|-----------------------|--|
| design                | An object of class <code>TrialDesignOptimalConditionalError</code> created by <code>getDesignOptimalConditionalErrorFunction()</code> . Contains all necessary arguments to calculate the optimal conditional error function for the specified case. |
| maxNumberOfIterations | Number of trials to be simulated.  |
| alternative           | Assumed relative effect size.  |
| seed                  | An optional seed for reproducibility.  |

**Details**

Simulates the probabilities of overall rejection as well as early futility and early efficacy for the provided scenario and design. This is done by generating random normally distributed test statistics and calculating their p-values.

**Value**

An object of class `SimulationResultsOptimalConditionalError` containing the simulation results.

**See Also**

`getDesignOptimalConditionalErrorFunction()`, `getOverallPower()`

**Examples**

```
design <- getDesignOptimalConditionalErrorFunction(
  alpha = 0.025, alpha1 = 0.001, alpha0 = 0.5, delta1 = 0.25,
  useInterimEstimate = FALSE,
  conditionalPower = 0.9, likelihoodRatioDistribution = "maxlr",
  firstStageInformation = 10
)

# Simulate under the null hypothesis and for a mean difference of 0.5
getSimulationResults(
  design = design, alternative = c(0, 0.5)
)
```

---

`plot.TrialDesignOptimalConditionalError`  
*Plot the optimal conditional error function*

---

**Description**

The returned plot is a `ggplot2` object and can be supplemented with additional layers using `ggplot2` commands.

**Usage**

```
## S3 method for class 'TrialDesignOptimalConditionalError'
plot(x, range = c(0, 1), type = 1, plotNonMonotoneFunction = FALSE, ...)
```

**Arguments**

|                    |   |
|--------------------|---|
| <code>x</code>     | Design object of class <code>TrialDesignOptimalConditionalError</code> .  |
| <code>range</code> | Numeric vector with two entries specifying the range of the x-axis of the plot.   |
| <code>type</code>  | Type of plot to be created. Options are: <ul style="list-style-type: none"> <li>• <code>type = 1</code>: Plot the values of the optimal conditional error function against the first-stage p-value.</li> <li>• <code>type = 2</code>: Plot the second-stage information resulting from the optimal conditional error function against the first-stage p-value.</li> </ul> |

- type = 3: Plot the likelihood ratio of the given specification of the optimal conditional error function against the first-stage p-value.
- type = 4: Plot the function Q of the given specification of the optimal conditional error function against the first-stage p-value.

plotNonMonotoneFunction

Logical. Should the non-monotone version of the plot be drawn? Not applicable for plot type 3. Default: FALSE.

... Additional arguments required for generic compatibility

### Value

No return value, plots the design.

---

PowerResultsOptimalConditionalError

*Power results for optimal conditional error design*

---

### Description

A class for power results of the optimal conditional error function.

---

print.PowerResultsOptimalConditionalError

*Print power results*

---

### Description

Print an overview of exact power results.

### Usage

```
## S3 method for class 'PowerResultsOptimalConditionalError'
print(x, ...)
```

### Arguments

x Power results object of class PowerResultsOptimalConditionalError  
 ... Additional arguments required for generic compatibility

### Value

No return value, prints the power calculation results.

---

```
print.SimulationResultsOptimalConditionalError
    Print simulation results
```

---

**Description**

Print an overview of simulation results.

**Usage**

```
## S3 method for class 'SimulationResultsOptimalConditionalError'
print(x, ...)
```

**Arguments**

|     |  |
|-----|--|
| x   | Simulation results object of class <code>SimulationResultsOptimalConditionalError</code> |
| ... | Additional arguments required for generic compatibility                                  |

**Value**

No return value, prints the simulation results.

---

```
print.TrialDesignOptimalConditionalError
    Print optimal conditional error trial design
```

---

**Description**

Print an overview of the specified design parameters.

**Usage**

```
## S3 method for class 'TrialDesignOptimalConditionalError'
print(x, ...)
```

**Arguments**

|     |  |
|-----|--|
| x   | Design object of class <code>TrialDesignOptimalConditionalError</code> |
| ... | Additional arguments required for generic compatibility                |

**Value**

No return value, prints the design.

---

SimulationResultsOptimalConditionalError  
*Simulation results for optimal conditional error design*

---

**Description**

A class for simulation results of the optimal conditional error function.

---

summary.TrialDesignOptimalConditionalError  
*Summary of the optimal conditional error trial design*

---

**Description**

Provide an overview of the operating characteristics of the optimal conditional error trial design.

**Usage**

```
## S3 method for class 'TrialDesignOptimalConditionalError'  
summary(object, ...)
```

**Arguments**

|        |   |
|--------|---|
| object | Design object of class TrialDesignOptimalConditionalError |
| ...    | Additional arguments required for generic compatibility   |

**Value**

No return value, prints a summary of design performance.

---

TrialDesignOptimalConditionalError  
*Optimal Conditional Error Design*

---

**Description**

A class for a trial design object using the optimal conditional error function.

**Details**

This object should not be created directly; use `getDesignOptimalConditionalErrorFunction()` with suitable arguments to create a design.

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