

# Package ‘ragtop’

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**Type** Package

**Title** Pricing Equity Derivatives with Extensions of Black-Scholes

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**Description** Algorithms to price American and European equity options, convertible bonds and a variety of other financial derivatives. It uses an extension of the usual Black-Scholes model in which jump to default may occur at a probability specified by a power-law link between stock price and hazard rate as found in the paper by Takahashi, Kobayashi, and Nakagawa (2001) <[doi:10.3905/jfi.2001.319302](https://doi.org/10.3905/jfi.2001.319302)>. We use ideas and techniques from Andersen and Buffum (2002) <[doi:10.2139/ssrn.355308](https://doi.org/10.2139/ssrn.355308)> and Linetsky (2006) <[doi:10.1111/j.1467-9965.2006.00271.x](https://doi.org/10.1111/j.1467-9965.2006.00271.x)>.

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---

*accelerated\_coupon\_value*  
*Present value of coupons according to an acceleration schedule*

---

### Description

Compute "present" value as of time *t* for coupons that would otherwise have been paid up to time *acceleration\_t*, in the case of accelerated coupon provisions for forced conversions (or sometimes even unforced ones).

### Usage

```
accelerated_coupon_value(
  t,
  coupons_df,
  discount_factor_fcn,
  acceleration_t = Inf
)
```

### Arguments

<i>t</i>	The time toward which all coupons should be present valued
<i>coupons_df</i>	A data.frame of details for each coupon. It should have the columns <i>payment_time</i> and <i>payment_size</i> .
<i>discount_factor_fcn</i>	A function specifying how the contract says future coupons should be discounted for this instrument in case the acceleration clause is triggered
<i>acceleration_t</i>	Time limit, up to which coupons will be accelerated

### See Also

Other Bond Coupons: [coupon\\_value\\_at\\_exercise\(\)](#), [value\\_from\\_prior\\_coupons\(\)](#)  
 Other Bond Coupon Acceleration: [coupon\\_value\\_at\\_exercise\(\)](#)

---

adjust\_for\_dividends *Find the sum of time-adjusted dividend values and adjust grid prices according to their size in the given interval*

---

### Description

Analyze dividends to find ones paid in the interval  $(t, t+dt]$ . Form present value as of time  $t$  for them, and then use spline interpolation to adjust instrument values accordingly.

### Usage

```
adjust_for_dividends(grid_values, t, dt, r, h, S, S0, dividends)
```

### Arguments

grid_values	A matrix with one row for each level of $S$ and one column per set of $S$ -associated instrument values
t	Time after this timestep has been taken
dt	Interval to end of timestep
r	risk-free interest rate
h	Default intensities
S	Underlying equity values for the grid
S0	Time zero price of the base equity
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * S / S0

### Value

An object like grid\_values with entries modified according to the dividends

### See Also

Other Dividends: [shift\\_for\\_dividends\(\)](#), [time\\_adj\\_dividends\(\)](#)

---

american                      *Price one or more american-exercise options*

---

### Description

Use a control-variate scheme to simultaneously estimate the present values of a collection of one or more American-exercise options under a default model with survival probabilities not linked to equity prices.

### Usage

```
american(
  callput,
  S0,
  K,
  time,
  const_short_rate = 0,
  const_default_intensity = 0,
  discount_factor_fcn = function(T, t, ...) {
    exp(-const_short_rate * (T - t))
  },
  survival_probability_fcn = function(T, t, ...) {
    exp(-const_default_intensity * (T
    - t))
  },
  default_intensity_fcn = function(t, S, ...) {
    const_default_intensity + 0 * S
  },
  ...,
  num_time_steps = 100,
  structure_constant = 2,
  std_devs_width = 5
)
```

### Arguments

callput	1 for calls, -1 for puts (may be a vector of the same)
S0	initial underlying price
K	strike (may be a vector)
time	Time from 0 until expiration (may be a vector)
const_short_rate	A constant to use for the instantaneous interest rate in case discount_factor_fcn is not given
const_default_intensity	A constant to use for the instantaneous default intensity in case default_intensity_fcn is not given

discount_factor_fcn	A function for computing present values to time $t$ of various cashflows occurring during this timestep, with arguments $T, t$
survival_probability_fcn	(Implied argument) A function for probability of survival, with arguments $T, t$ and $T > t$ . E.g. with a constant volatility $s$ this takes the form $(T - t)s^2$ . Should be matched to default_intensity_fcn
default_intensity_fcn	A function for computing default intensity occurring at a given time, dependent on time and stock price, with arguments $t, S$ . Should be matched to survival_probability_fcn
...	Further arguments passed on to <a href="#">find_present_value</a>
num_time_steps	Number of steps to use in the grid solver. Can usually be set quite low due to the control variate scheme.
structure_constant	The maximum ratio between time intervals $dt$ and the square of space intervals $dz^2$
std_devs_width	The number of standard deviations, in $\sigma * \sqrt{T}$ units, to incorporate into the grid

### Details

The scheme uses `find_present_value()` to price the options and their European-exercise equivalents. It then compares the latter to black-scholes formula output and uses the results as an error correction on the prices of the American-exercise options.

### Value

A vector of estimated option present values

### See Also

Other Equity Independent Default Intensity: [american\\_implied\\_volatility\(\)](#), [black\\_scholes\\_on\\_term\\_structures\(\)](#), [blackscholes\(\)](#), [equivalent\\_bs\\_vola\\_to\\_jump\(\)](#), [equivalent\\_jump\\_vola\\_to\\_bs\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

Other American Exercise Equity Options: [american\\_implied\\_volatility\(\)](#), [control\\_variate\\_pairs\(\)](#)

### Examples

```
american(PUT, S0=100, K=110, time=0.77, const_short_rate = 0.06,
         const_volatility=0.20, num_time_steps=200)
american(callput=-1, S0=100, K=90, time=1, const_short_rate=0.025,
         variance_cumulation_fcn = function(T, t) { # Term structure of vola
           0.45 ^ 2 * (T - t) + 0.15^2 * max(0, T-0.25)
         })
```

---

AmericanOption-class *A standard option contract allowing for early exercise at the choice of the option holder*

---

### Description

A standard option contract allowing for *early* exercise at the choice of the option holder

### Methods

optionality\_fcn(v, ...) Return a version of v at time t corrected for any optionality conditions.

recovery\_fcn(v, S, t, ...) Return recovery value, given non-default values v at time t. Sub-classes may be more elaborate, this method simply returns 0.0.

---

american\_implied\_volatility  
*Implied volatility of an american option with equity-independent term structures*

---

### Description

Use the grid solver to generate american option values under a default model with survival probabilities not linked to equity prices. and run them through a bisection root search method until a constant volatility matching the provided option price has been found.

### Usage

```
american_implied_volatility(
  option_price,
  callput,
  S0,
  K,
  time,
  const_default_intensity = 0,
  survival_probability_fcn = function(T, t, ...) {
    exp(-const_default_intensity * (T
    - t))
  },
  default_intensity_fcn = function(t, S, ...) {
    const_default_intensity + 0 * S
  },
  ...,
  num_time_steps = 30,
  structure_constant = 2,
```

```

    std_devs_width = 5,
    relative_tolerance = 1e-04,
    max.iter = 100,
    max_vola = 4
)

```

### Arguments

option_price	Option price to match
callput	1 for calls, -1 for puts
S0	An initial stock price, for setting grid scale
K	strike
time	Time from 0 until expiration
const_default_intensity	A constant to use for the instantaneous default intensity in case default_intensity_fcn is not given
survival_probability_fcn	(Implied argument) A function for probability of survival, with arguments T, t and T>t.
default_intensity_fcn	A function for computing default intensity occurring at a given time, dependent on time and stock price, with arguments t, S. Should be matched to survival_probability_fcn
...	Additional arguments to be passed on to <a href="#">implied_volatility_with_term_struct</a> and <a href="#">american</a>
num_time_steps	Minimum number of time steps in the grid
structure_constant	The maximum ratio between time intervals dt and the square of space intervals dz^2
std_devs_width	The number of standard deviations, in $\sigma * \sqrt{T}$ units, to incorporate into the grid
relative_tolerance	Relative tolerance in instrument price defining the root-finder halting condition
max.iter	Maximum number of root-finder iterations allowed
max_vola	Maximum volatility to try

### Value

Estimated volatility

### See Also

[implied\\_volatility\\_with\\_term\\_struct](#) for implied volatility of European options under the same conditions, [american](#) for the underlying pricing algorithm

Other Implied Volatilities: [equivalent\\_bs\\_vola\\_to\\_jump\(\)](#), [equivalent\\_jump\\_vola\\_to\\_bs\(\)](#), [fit\\_variance\\_cumulation\(\)](#), [implied\\_jump\\_process\\_volatility\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

Other Equity Independent Default Intensity: `american()`, `black_scholes_on_term_structures()`, `blackscholes()`, `equivalent_bs_vola_to_jump()`, `equivalent_jump_vola_to_bs()`, `implied_volatilities()`, `implied_volatilities_with_rates_struct()`, `implied_volatility()`, `implied_volatility_with_term_struct()`

Other American Exercise Equity Options: `american()`, `control_variate_pairs()`

## Examples

```
american_implied_volatility(25, CALL, S0=100, K=100, time=2.2,
  const_short_rate=0.03, num_time_steps=5)
df250 = function(t) ( exp(-0.02*t)*exp(-0.03*max(0,t-1.0))) # Simple term structure
df25 = function(T,t){df250(T)/df250(t)} # Relative discount factors
american_implied_volatility(25, -1, 100, 100, 2.2,
  discount_factor_fcn=df25, num_time_steps=5)
```

---

blackscholes

---

*Vectorized Black-Scholes pricing of european-exercise options*


---

## Description

Price options according to the famous Black-Scholes formula, with the optional addition of a jump-to-default intensity and discrete dividends.

## Usage

```
blackscholes(
  callput,
  S0,
  K,
  r,
  time,
  vola,
  default_intensity = 0,
  divrate = 0,
  borrow_cost = 0,
  dividends = NULL
)
```

## Arguments

callput	1 for calls, -1 for puts
S0	initial underlying price
K	strike
r	risk-free interest rate
time	Time from 0 until expiration
vola	Default-free volatility of the underlying

default_intensity	hazard rate of underlying default
divrate	A continuous rate for dividends and other cashflows such as foreign interest rates
borrow_cost	A continuous rate for stock borrow costs
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * S / S0. Fixed dividends will be converted to proportional for purposes of this algorithm.

### Details

Note that if the default\_intensity is set larger than zero then put-call parity still holds. Greeks are reduced according to cumulated default probability.

All inputs must either be scalars or have the same nonscalar shape.

### Value

A list with elements

Price The present value(s)

Delta Sensitivity to underlying price

Vega Sensitivity to volatility

### See Also

Other European Options: [black\\_scholes\\_on\\_term\\_structures\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

Other Equity Independent Default Intensity: [american\(\)](#), [american\\_implied\\_volatility\(\)](#), [black\\_scholes\\_on\\_term\\_structures\(\)](#), [equivalent\\_bs\\_vola\\_to\\_jump\(\)](#), [equivalent\\_jump\\_vola\\_to\\_bs\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

### Examples

```
blackscholes(callput=-1, S0=100, K=90, r=0.03, time=1, # -1 is a PUT
             vola=0.5, default_intensity=0.07)
```

---

black\_scholes\_on\_term\_structures

*Black-Scholes pricing of european-exercise options with term structure arguments*

---

### Description

Price an option according to the famous Black-Scholes formula, with the optional addition of a jump-to-default intensity and discrete dividends. Volatility and rates may be provided as constants or as 2+ parameter functions with first argument T corresponding to maturity and second argument t corresponding to model date.

**Usage**

```

black_scholes_on_term_structures(
  callput,
  S0,
  K,
  time,
  const_volatility = 0.5,
  const_short_rate = 0,
  const_default_intensity = 0,
  discount_factor_fcn = function(T, t, ...) {
    exp(-const_short_rate * (T - t))
  },
  survival_probability_fcn = function(T, t, ...) {
    exp(-const_default_intensity * (T
  - t))
  },
  variance_cumulation_fcn = function(T, t) {
    const_volatility^2 * (T - t)
  },
  dividends = NULL,
  borrow_cost = 0,
  dividend_rate = 0
)

```

**Arguments**

callput	1 for calls, -1 for puts
S0	initial underlying price
K	strike
time	Time from 0 until expiration
const_volatility	A constant to use for volatility in case variance_cumulation_fcn is not given
const_short_rate	A constant to use for the instantaneous interest rate in case discount_factor_fcn is not given
const_default_intensity	A constant to use for the instantaneous default intensity in case default_intensity_fcn is not given
discount_factor_fcn	A function for computing present values to time t of various cashflows occurring during this timestep, with arguments T, t
survival_probability_fcn	A function for probability of survival, with arguments T, t and T>t. E.g. with a constant volatility s this takes the form $(T - t)s^2$ .

<code>variance_cumulation_fcn</code>	A function for computing total stock variance occurring during this timestep, with arguments $T, t$ . E.g. with a constant volatility $s$ this takes the form $(T - t)s^2$ .
<code>dividends</code>	A data.frame with columns <code>time</code> , <code>fixed</code> , and <code>proportional</code> . Dividend size at the given time is then expected to be equal to <code>fixed + proportional * S / S0</code> . Fixed dividends will be converted to proportional for purposes of this algorithm.
<code>borrow_cost</code>	A continuous rate for stock borrow costs
<code>dividend_rate</code>	A continuous rate for dividends and other cashflows such as foreign interest rates

### Details

Any term structures will be converted to equivalent constant arguments by calling them with the arguments `(time, 0)`.

### See Also

Other European Options: `blackscholes()`, `implied_volatilities()`, `implied_volatilities_with_rates_struct()`, `implied_volatility()`, `implied_volatility_with_term_struct()`

Other Equity Independent Default Intensity: `american()`, `american_implied_volatility()`, `blackscholes()`, `equivalent_bs_vola_to_jump()`, `equivalent_jump_vola_to_bs()`, `implied_volatilities()`, `implied_volatilities_with_rates_struct()`, `implied_volatility()`, `implied_volatility_with_term_struct()`

### Examples

```
black_scholes_on_term_structures(callput=-1, S0=100, K=90, time=1,
                                discount_factor_fcn = function(T, t, ...) {
                                  exp(-0.03 * (T - t))
                                },
                                survival_probability_fcn = function(T, t, ...) {
                                  exp(-0.07 * (T - t))
                                },
                                variance_cumulation_fcn = function(T, t) {
                                  0.45 ^ 2 * (T - t)
                                })
```

---

CALL

*Constant CALL for defining option contracts*

---

### Description

Constant CALL for defining option contracts

### Usage

CALL

**Format**

An object of class `numeric` of length 1.

---

CallableBond-class      *Callable (and puttable) corporate or government bond.*

---

**Description**

When a bond is *callable*, the issuer may choose to pay the call price to the bond holder and end the life of the contract.

**Details**

When a bond is *puttable*, the bond holder may choose to force the issuer pay the put price to the bond holder thus ending the life of the contract.

**Fields**

`calls` A data.frame of details for each call. It should have the columns `call_price` and `effective_time`.

`puts` A data.frame of details for each put. It should have the columns `put_price` and `effective_time`.

**Methods**

`critical_times()` Important times in the life of this instrument for simulation and grid solvers

---

`construct_implicit_grid_structure`  
*Structure of implicit numerical integration grid*

---

**Description**

Infer a reasonable structure for our implicit grid solver based on the voltime, structure constant, and requested grid width in standard deviations.

**Usage**

```
construct_implicit_grid_structure(
  tenors,
  M,
  S0,
  K,
  c,
  sigma,
  structure_constant,
  std_devs_width,
  min_z_width = 0
)
```

**Arguments**

tenors	Tenors of instruments to be treated on this grid
M	Minimum number of timesteps on this grid
S0	An initial stock price, for setting grid scale
K	An instrument reference stock price, for setting grid scale
c	A continuous stock drift rate
sigma	Volatility of diffusion process (without jumps to default)
structure_constant	The maximum ratio between time intervals dt and the square of space intervals dz <sup>2</sup>
std_devs_width	The number of standard deviations, in $\text{sigma} * \text{sqrt}(T)$ units, to incorporate into the grid
min_z_width	Minimum grid width, in log space

**Details**

Generally speaking pricing will be good to about 10bp of relative accuracy when the ratio of timesteps to voltime (in annualized units) is over 200.

Cases with pathologically low volatility may go awry (in the sense of yielding ultimately inaccurate PDE solutions), as the `structure_constant` will force a step in  $z$  space much bigger than the width in standard deviations.

**Value**

A list with elements
T The maximum time for this grid
dt Largest permissible timestep size
dz Distance between space grid points
z0 Center of space grid
z_width Width in $z$ space
half_N A misnomer, actually $(N - 1)/2$
N The number of space points
z Locations of space points

**See Also**

Other Implicit Grid Solver: [find\\_present\\_value\(\)](#), [form\\_present\\_value\\_grid\(\)](#), [infer\\_conforming\\_time\\_grid\(\)](#), [integrate\\_pde\(\)](#), [iterate\\_grid\\_from\\_timestep\(\)](#), [take\\_implicit\\_timestep\(\)](#), [timestep\\_instruments\(\)](#)

---

 construct\_tridiagonals

*Matrix entries for implicit numerical differentiation using Neumann boundary conditions*

---

### Description

Matrix entries for implicit numerical differentiation using Neumann boundary conditions

### Usage

```
construct_tridiagonals(sigma, structure_constant, drift)
```

### Arguments

sigma	Volatility of diffusion process (without jumps to default)
structure_constant	The ratio between time interval dt and the square of space interval dz^2
drift	Vector of drift rate of underlying equity grid points, including induced drift from default intensity

### Value

A list with elements super, diag and sub containing the superdiagonal, diagonal and subdiagonal of the implicit timestep differencing matrix

---

control\_variate\_pairs *Form instrument objects for vanilla options*

---

### Description

Form a list twice as long as the longest of the arguments callput, K, time whose first half consists of AmericanOption objects and second half consists of EuropeanOption objects having the same exercise specification

### Usage

```
control_variate_pairs(callput, K, time)
```

### Arguments

callput	1 for calls, -1 for puts
K	strike
time	Time from 0 until expiration

**See Also**

Other American Exercise Equity Options: [american\(\)](#), [american\\_implied\\_volatility\(\)](#)

---

ConvertibleBond-class *Convertible bond with exercise into stock*

---

**Description**

Convertible bond with exercise into stock

**Fields**

`conversion_ratio` The number of shares, per bond, that result from exercise  
`dividend_ceiling` The level of dividend protection (if any) specified in terms and conditions

**Methods**

`exercise_decision(v, S, t, discount_factor_fctn = discount_factor_fcn, ...)` Find indexes where hold value  $v$  will be inferior to conversion value at each stock price level in  $S$ , adjusted to include all past coupons

`optionality_fcn(v, S, t, discount_factor_fctn = discount_factor_fcn, ...)` Return the greater of hold value  $v$  or exercise value at each stock price level in  $S$ . If the given date is beyond maturity, return value at maturity.

`terminal_values(v, ...)` Return a terminal value. defaults to simply calling `optionality_fcn`.

`update_cashflows(small_t, big_t, discount_factor_fctn = discount_factor_fcn, include_notional = TRUE, ...)` Update `last_computed_cash` and return cashflow information for the given time period, valued at `big_t`

---

CouponBond-class *Standard corporate or government bond*

---

**Description**

A coupon bond is treated here as the entire collection of cashflows. In particular, coupons are included in the package even after they have been paid, accruing at the risk-free rate.

**Fields**

`coupons` A `data.frame` of details for each coupon. It should have the columns `payment_time` and `payment_size`.

**Methods**

accumulate\_coupon\_values\_before(t, discount\_factor\_fctn = discount\_factor\_fcn) Compute the sum of coupon present values as of t according to discount\_factor\_fctn

critical\_times() Important times in the life of this instrument for simulation and grid solvers

optionality\_fcn(v, S, t, ...) Return the notional value in the shape of S at any time on or after maturity, otherwise just return v

total\_coupon\_values\_between( small\_t, big\_t, discount\_factor\_fctn = discount\_factor\_fcn ) Compute the sum (as of big\_t) of present values of coupons paid between small\_t and big\_t

update\_cashflows( small\_t, big\_t, discount\_factor\_fctn = discount\_factor\_fcn, include\_notional = TRUE, ... ) Update last\_computed\_cash and return cashflow information for the given time period, valued at big\_t

---

coupon\_value\_at\_exercise

*Present value of coupons according to an acceleration schedule*

---

**Description**

Compute "present" value as of time t for coupons that would otherwise have been paid up to time acceleration\_t, in the case of accelerated coupon provisions for forced conversions (or sometimes even unforced ones).

**Usage**

```
coupon_value_at_exercise(
  t,
  coupons_df,
  discount_factor_fcn,
  model_t = 0,
  accelerate_future_coupons = FALSE,
  acceleration_discount_factor_fcn = discount_factor_fcn,
  acceleration_t = Inf
)
```

**Arguments**

t	The time toward which all coupons should be present valued
coupons_df	A data.frame of details for each coupon. It should have the columns payment_time and payment_size.
discount_factor_fcn	A function specifying how future cashflows should generally be discounted for this instrument
model_t	Model timestamp passed to <a href="#">value_from_prior_coupons</a>
accelerate_future_coupons	If TRUE, future coupons will be accelerated on exercise to pad present value

- acceleration\_discount\_factor\_fcn  
A function specifying how future coupons should be discounted for this instrument under coupon acceleration conditions
- acceleration\_t The maximum time up to which future coupons will be counted for acceleration, passed on to [accelerated\\_coupon\\_value](#)

**Value**

A scalar equal to the present value

**See Also**

- Other Bond Coupons: [accelerated\\_coupon\\_value\(\)](#), [value\\_from\\_prior\\_coupons\(\)](#)
- Other Bond Coupon Acceleration: [accelerated\\_coupon\\_value\(\)](#)

---

detail\_from\_AnnivDates

*Convert output of BondValuation::AnnivDates to inputd for Bond*

---

**Description**

The BondValuation package provides day count convention treatments superior to quantmod or any other R package known (as of May 2019). This function takes output from BondValuation::AnnivDates(...) and parses it into notionals, maturity time, and coupon times and sizes.

**Usage**

```
detail_from_AnnivDates(
  anvdates,
  as_of = Sys.time(),
  normalization_factor = 365.25
)
```

**Arguments**

- anvdates Output of BondValuation::AnnivDates(), which must have included a ‘Coup’ argument so that the resulting list contains an entry for ‘PaySched’
- as\_of Date or time from whose perspective times should be computed
- normalization\_factor Factor by which raw R time differences should be multiplied. If volatilities are going to be annualized, then this should typically be 365 or so.

**Details**

Note: volatilities used in ‘ragtop’ must have compatible time units to these times.

**Value**

A list with some of the arguments appropriate for defining a Bond as follows: maturity - maturity notional - notional amount coupons - 'data.frame' with 'payment\_time', 'payment\_size'

---

EquityOption-class      *An option contract with call or put terms*

---

**Description**

An option contract with call or put terms

**Fields**

strike A decision price for the contract  
callput Either 1 for a call or -1 for a put

---

equivalent\_bs\_vola\_to\_jump  
*Find straight Black-Scholes volatility equivalent to jump process with a given default risk*

---

**Description**

Find Black-Scholes volatility based on known interest rates and hazard rates, using an at-the-money put option at the given tenor to set the standard price.

**Usage**

```
equivalent_bs_vola_to_jump(
  jump_process_vola,
  time,
  const_short_rate = 0,
  const_default_intensity = 0,
  discount_factor_fcn = function(T, t, ...) {
    exp(-const_short_rate * (T - t))
  },
  survival_probability_fcn = function(T, t, ...) {
    exp(-const_default_intensity * (T
  - t))
  },
  dividends = NULL,
  borrow_cost = 0,
  dividend_rate = 0,
  relative_tolerance = 1e-06,
  max.iter = 100
)
```

**Arguments**

jump_process_vola	Volatility of default-free process
time	Time to expiration of associated option contracts
const_short_rate	A constant to use for the instantaneous interest rate in case discount_factor_fcn is not given
const_default_intensity	A constant to use for the instantaneous default intensity in case survival_probability_fcn is not given
discount_factor_fcn	A function for computing present values to time t of various cashflows occurring during this timestep, with arguments T, t
survival_probability_fcn	(Implied argument) A function for probability of survival, with arguments T, t and T>t.
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * S / S0. Fixed dividends will be converted to proportional for purposes of this algorithm.
borrow_cost	A continuous rate for stock borrow costs
dividend_rate	A continuous accumulation rate for the stock, affecting the drift
relative_tolerance	Relative tolerance in instrument price defining the root-finder halting condition
max.iter	Maximum number of root-finder iterations allowed

**Value**

A scalar defaultable volatility of an option

**See Also**

Other Implied Volatilities: [american\\_implied\\_volatility\(\)](#), [equivalent\\_jump\\_vola\\_to\\_bs\(\)](#), [fit\\_variance\\_cumulation\(\)](#), [implied\\_jump\\_process\\_volatility\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

Other Equity Independent Default Intensity: [american\(\)](#), [american\\_implied\\_volatility\(\)](#), [black\\_scholes\\_on\\_term\\_structures\(\)](#), [blackscholes\(\)](#), [equivalent\\_jump\\_vola\\_to\\_bs\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

---

 equivalent\_jump\_vola\_to\_bs

*Find jump process volatility with a given default risk from a straight Black-Scholes volatility*

---

### Description

Find default-free volatility (i.e. volatility of a Wiener process with a companion jump process to default) based on known interest rates and hazard rates, using and at-the-money put option at the given tenor to set the standard price.

### Usage

```
equivalent_jump_vola_to_bs(
  bs_vola,
  time,
  const_short_rate = 0,
  const_default_intensity = 0,
  discount_factor_fcn = function(T, t, ...) {
    exp(-const_short_rate * (T - t))
  },
  survival_probability_fcn = function(T, t, ...) {
    exp(-const_default_intensity * (T
    - t))
  },
  dividends = NULL,
  borrow_cost = 0,
  dividend_rate = 0,
  relative_tolerance = 1e-06,
  max.iter = 100
)
```

### Arguments

bs_vola	BlackScholes volatility of an option with no default assumption
time	Time to expiration of associated option contracts
const_short_rate	A constant to use for the instantaneous interest rate in case discount_factor_fcn is not given
const_default_intensity	A constant to use for the instantaneous default intensity in case survival_probability_fcn is not given
discount_factor_fcn	A function for computing present values to time t of various cashflows occurring during this timestep, with arguments T, t

survival_probability_fcn	(Implied argument) A function for probability of survival, with arguments $T$ , $t$ and $T > t$ .
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to $\text{fixed} + \text{proportional} * S / S_0$
borrow_cost	Stock borrow cost, affecting the drift rate
dividend_rate	A continuous accumulation rate for the stock, affecting the drift
relative_tolerance	Relative tolerance in instrument price defining the root-finder halting condition
max.iter	Maximum number of root-finder iterations allowed

**Value**

A scalar volatility

**See Also**

Other Implied Volatilities: [american\\_implied\\_volatility\(\)](#), [equivalent\\_bs\\_vola\\_to\\_jump\(\)](#), [fit\\_variance\\_cumulation\(\)](#), [implied\\_jump\\_process\\_volatility\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

Other Equity Independent Default Intensity: [american\(\)](#), [american\\_implied\\_volatility\(\)](#), [black\\_scholes\\_on\\_term\\_structures\(\)](#), [blackscholes\(\)](#), [equivalent\\_bs\\_vola\\_to\\_jump\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

---

EuropeanOption-class    *A standard option contract*

---

**Description**

At maturity, the call option holder will "exercise", i.e. choose stock, with value  $S$ , if the stock price is above the strike  $K$ , paying  $K$  to the option issuer, realizing value  $S-K$ . The put option holder will exercise, receiving  $K$  while surrendering stock worth  $S$ , if the stock price is below  $K$ .

**Details**

Therefore the value at maturity is equal to  $\max(0, \text{callput} * (S-K))$

**Methods**

- `optionality_fcn(v, ...)` Return a version of  $v$  at time  $t$  corrected for any optionality conditions.
- `recovery_fcn(v, S, t, ...)` Return recovery value, given non-default values  $v$  at time  $t$ . Sub-classes may be more elaborate, this method simply returns 0.0.

---

find\_present\_value      *Use a model to estimate the present value of financial derivatives*

---

### Description

Use a finite difference scheme to form estimates of present values for a variety of stock prices. Once the grid has been created, interpolate to obtain the value of each instrument at the present stock price  $S_0$

### Usage

```
find_present_value(
    S0,
    num_time_steps,
    instruments,
    const_volatility = 0.5,
    const_short_rate = 0,
    const_default_intensity = 0,
    override_Tmax = NA,
    discount_factor_fcn = function(T, t, ...) {
        exp(-const_short_rate * (T - t))
    },
    default_intensity_fcn = function(t, S, ...) {
        const_default_intensity + 0 * S
    },
    variance_cumulation_fcn = function(T, t) {
        const_volatility^2 * (T - t)
    },
    dividends = NULL,
    borrow_cost = 0,
    dividend_rate = 0,
    structure_constant = 2,
    std_devs_width = 3
)
```

### Arguments

<code>S0</code>	An initial stock price, for setting grid scale
<code>num_time_steps</code>	Minimum number of time steps in the grid
<code>instruments</code>	A list of instruments to be priced. Each one must have a strike and a <code>optionality_fcn</code> , as with <a href="#">GridPricedInstrument</a> and its subclasses.
<code>const_volatility</code>	A constant to use for volatility in case <code>variance_cumulation_fcn</code> is not given
<code>const_short_rate</code>	A constant to use for the instantaneous interest rate in case <code>discount_factor_fcn</code> is not given

const_default_intensity	A constant to use for the instantaneous default intensity in case default_intensity_fcn is not given
override_Tmax	A different maximum time on the grid to enforce
discount_factor_fcn	A function for computing present values to time t of various cashflows occurring during this timestep, with arguments T, t
default_intensity_fcn	A function for computing default intensity occurring during this timestep, dependent on time and stock price, with arguments t, S.
variance_cumulation_fcn	A function for computing total stock variance occurring during this timestep, with arguments T, t. E.g. with a constant volatility s this takes the form $(T - t)s^2$ .
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * S / S0
borrow_cost	Stock borrow cost, affecting the drift rate
dividend_rate	Continuous dividend rate, affecting the drift rate
structure_constant	The maximum ratio between time intervals dt and the square of space intervals dz^2
std_devs_width	The number of standard deviations, in $\sigma * \sqrt{T}$ units, to incorporate into the grid

**Value**

A list of present values, with the same names as instruments

**See Also**

Other Equity Dependent Default Intensity: [fit\\_to\\_option\\_market\\_df\(\)](#), [fit\\_variance\\_cumulation\(\)](#), [form\\_present\\_value\\_grid\(\)](#), [implied\\_jump\\_process\\_volatility\(\)](#)

Other Implicit Grid Solver: [construct\\_implicit\\_grid\\_structure\(\)](#), [form\\_present\\_value\\_grid\(\)](#), [infer\\_conforming\\_time\\_grid\(\)](#), [integrate\\_pde\(\)](#), [iterate\\_grid\\_from\\_timestep\(\)](#), [take\\_implicit\\_timestep\(\)](#), [timestep\\_instruments\(\)](#)

---

fit\_to\_option\_market    *Calibrate volatilities and equity-linked default intensity*

---

**Description**

Given derivative instruments (subclasses of GridPricedInstrument, though typically either [AmericanOption](#) or [EuropeanOption](#) objects), along with their prices and spreads, calibrate variance cumulation (the at-the-money volatility of the continuous process) and equity linked default intensity of the form  $h(s + (1-s)(S_0/S_t)^p)$ .

**Usage**

```

fit_to_option_market(
    variance_instruments,
    variance_instrument_prices,
    variance_instrument_spreads,
    fit_instruments,
    fit_instrument_prices,
    fit_instrument_spreads,
    fit_instrument_weights,
    S0,
    num_time_steps = 30,
    const_short_rate = 0,
    discount_factor_fcn = function(T, t) {
        exp(-const_short_rate * (T - t))
    },
    ...,
    base_default_intensity = 0.05,
    relative_spread_tolerance = 0.15,
    num_variance_time_steps = 30
)

```

**Arguments**

**variance\_instruments**  
A list of instruments in strictly increasing order of maturity, from which the volatility term structure will be inferred. Once the calibration is finished, the chosen parameters will reproduce the prices of these instruments with fairly high precision.

**variance\_instrument\_prices**  
Central price targets for the variance instruments

**variance\_instrument\_spreads**  
Bid-offer spreads used to normalize errors in variance instrument prices during term structure fitting

**fit\_instruments**  
A list of instruments in any order, from which the mispricing penalties used for judging fit quality will be computed

**fit\_instrument\_prices**  
Central price targets for the variance instruments

**fit\_instrument\_spreads**  
Bid-offer spreads used to normalize errors in fit instrument prices during default intensity

**fit\_instrument\_weights**  
Weights applied to relative errors in fit instrument prices before summing to form the penalty

**S0**  
Current underlying price

**num\_time\_steps**  
Time step count passed on to [find\\_present\\_value](#) while fitting instrument values

`const_short_rate`  
 A constant to use for the instantaneous interest rate in case `discount_factor_fcn` is not given

`discount_factor_fcn`  
 A function for computing present values to time `t` of various cashflows occurring during this timestep, with arguments `T`, `t`

`...`  
 Further arguments passed to [penalty\\_with\\_intensity\\_link](#)

`base_default_intensity`  
 Overall default intensity (in natural units)

`relative_spread_tolerance`  
 Tolerance to apply in calling [fit\\_variance\\_cumulation](#)

`num_variance_time_steps`  
 Number of time steps to use in calling [fit\\_variance\\_cumulation](#)

### Details

In its present form, this function uses a brain-dead grid search.

### See Also

[penalty\\_with\\_intensity\\_link](#) for the penalty function used as an optimization target

---

`fit_to_option_market_df`

*Calibrate volatilities and equity-linked default intensity making many assumptions*

---

### Description

This is a convenience function for calibrating variance cumulation (the at-the-money volatility of the continuous process) and equity linked default intensity of the form  $h(s + (1-s)(S_0/S_t)^p)$ , using a `data.frame` of option market data.

### Usage

```

fit_to_option_market_df(
  S0 = ragtop::TSLAMarket$S0,
  discount_factor_fcn = spot_to_df_fcn(ragtop::TSLAMarket$risk_free_rates),
  options_df = ragtop::TSLAMarket$options,
  min_maturity = 1/12,
  min_moneyness = 0.8,
  max_moneyness = 1.2,
  base_default_intensity = 0.05
)

```

**Arguments**

<code>S0</code>	Current underlying price
<code>discount_factor_fcn</code>	A function for computing present values to time <code>t</code> of various cashflows occurring during this timestep, with arguments <code>T</code> , <code>t</code>
<code>options_df</code>	A data frame of American option details. It should have columns <code>callput</code> , <code>K</code> , <code>time</code> , <code>mid</code> , <code>bid</code> , and <code>ask</code> ,
<code>min_maturity</code>	Minimum option maturity to allow in calibration
<code>min_moneyness</code>	Maximum option strike as a proportion of <code>S0</code> to allow in calibration
<code>max_moneyness</code>	Maximum option strike as a proportion of <code>S0</code> to allow in calibration
<code>base_default_intensity</code>	Overall default intensity (in natural units)

**See Also**

[fit\\_to\\_option\\_market](#) the underlying fit algorithm

Other Equity Dependent Default Intensity: [find\\_present\\_value\(\)](#), [fit\\_variance\\_cumulation\(\)](#), [form\\_present\\_value\\_grid\(\)](#), [implied\\_jump\\_process\\_volatility\(\)](#)

---

`fit_variance_cumulation`

*Fit piecewise constant volatilities to a set of equity options*

---

**Description**

Given a set of equity options with increasing tenors, along with target prices for those options, and a set of equity-lined default SDE parameters, fit a vector of piecewise constant volatilities and an associated cumulative variance function to them.

**Usage**

```
fit_variance_cumulation(
  S0,
  eq_options,
  mid_prices,
  spreads = NULL,
  initial_vols_guess = 0.55 + 0 * mid_prices,
  use_impvol = TRUE,
  relative_spread_tolerance = 0.01,
  force_same_grid = FALSE,
  num_time_steps = 40,
  const_short_rate = 0,
  const_default_intensity = 0,
  discount_factor_fcn = function(T, t, ...) {
```

```

    exp(-const_short_rate * (T - t))
  },
  survival_probability_fcn = function(T, t, ...) {
    exp(-const_default_intensity * (T
      - t))
  },
  default_intensity_fcn = function(t, S, ...) {
    const_default_intensity + 0 * S
  },
  dividends = NULL,
  borrow_cost = 0,
  dividend_rate = 0,
  ...
)

```

### Arguments

<code>S0</code>	Current stock price
<code>eq_options</code>	A list of options to find prices for. Each must have fields <code>callput</code> , <code>maturity</code> , and <code>strike</code> . This list must be in strictly increasing order of maturity.
<code>mid_prices</code>	Prices to match
<code>spreads</code>	Spreads within which any match is tolerable
<code>initial_vols_guess</code>	Initial set of volatilities to try in the root finder
<code>use_impvol</code>	Judge fit quality on implied vol distance rather than price distance
<code>relative_spread_tolerance</code>	Tolerance multiplier on bid-ask spreads taken from vol normalization
<code>force_same_grid</code>	Price all options on the same grid, rather than having smaller timestep sizes for earlier maturities
<code>num_time_steps</code>	Minimum number of time steps in the grid
<code>const_short_rate</code>	A constant to use for the instantaneous interest rate in case <code>discount_factor_fcn</code> is not given
<code>const_default_intensity</code>	A constant to use for the instantaneous default intensity in case <code>default_intensity_fcn</code> is not given
<code>discount_factor_fcn</code>	A function for computing present values to time <code>t</code> of various cashflows occurring, with arguments <code>T</code> , <code>t</code>
<code>survival_probability_fcn</code>	A function for probability of survival, with arguments <code>T</code> , <code>t</code> and $T > t$ . E.g. with a constant volatility $s$ this takes the form $(T - t)s^2$ . This argument is only used in normalization of prices to vols for root finder tolerance, and is therefore entirely optional

default_intensity_fcn	A function for computing default intensity occurring during this timestep, dependent on time and stock price, with arguments $t$ , $S$ . Should be consistent with <code>survival_probability_fcn</code> if specified
dividends	A <code>data.frame</code> with columns <code>time</code> , <code>fixed</code> , and <code>proportional</code> . Dividend size at the given time is
borrow_cost	Stock borrow cost, affecting the drift rate
dividend_rate	Continuous dividend rate, affecting the drift rate
...	Further arguments to <code>find_present_value</code>

### Details

By default, the fitting happens in implied Black-Scholes volatility space for better normalization. That is to say, the fitting does pricing using the *full* SDE and PDE solver via `find_present_value`, but judges fit quality on the basis of running resulting prices through a nonlinear transformation that just happens to come from the straight Black-Scholes model.

### Value

A list with two elements, `volatilities` and `cumulation_function`. The `cumulation_function` will be a 2-parameter function giving cumulated variances, as created by `variance_cumulation_from_vols`

### See Also

Other Implied Volatilities: `american_implied_volatility()`, `equivalent_bs_vola_to_jump()`, `equivalent_jump_vola_to_bs()`, `implied_jump_process_volatility()`, `implied_volatilities()`, `implied_volatilities_with_rates_struct()`, `implied_volatility()`, `implied_volatility_with_term_struct()`

Other Equity Dependent Default Intensity: `find_present_value()`, `fit_to_option_market_df()`, `form_present_value_grid()`, `implied_jump_process_volatility()`

---

form\_present\_value\_grid

*Use a model to estimate the present value of financial derivatives on a grid of initial underlying values*

---

### Description

Use a finite difference scheme to form estimates of present values for a variety of stock prices on a grid of initial underlying prices, determined by constructing a logarithmic equivalent conforming to the grid parameters `structure_constant` and `structure_constant`

**Usage**

```

form_present_value_grid(
  S0,
  num_time_steps,
  instruments,
  const_volatility = 0.5,
  const_short_rate = 0,
  const_default_intensity = 0,
  override_Tmax = NA,
  discount_factor_fcn = function(T, t, ...) {
    exp(-const_short_rate * (T - t))
  },
  default_intensity_fcn = function(t, S, ...) {
    const_default_intensity + 0 * S
  },
  variance_cumulation_fcn = function(T, t) {
    const_volatility^2 * (T - t)
  },
  dividends = NULL,
  borrow_cost = 0,
  dividend_rate = 0,
  structure_constant = 2,
  std_devs_width = 3,
  grid_center = NA
)

```

**Arguments**

**S0** An initial stock price, for setting grid scale

**num\_time\_steps** Minimum number of time steps in the grid

**instruments** A list of instruments to be priced. Each one must have a strike and a `optionality_fcn`, as with [GridPricedInstrument](#) and its subclasses.

**const\_volatility** A constant to use for volatility in case `variance_cumulation_fcn` is not given

**const\_short\_rate** A constant to use for the instantaneous interest rate in case `discount_factor_fcn` is not given

**const\_default\_intensity** A constant to use for the instantaneous default intensity in case `default_intensity_fcn` is not given

**override\_Tmax** A different maximum time on the grid to enforce

**discount\_factor\_fcn** A function for computing present values to time `t` of various cashflows occurring during this timestep, with arguments `T, t`

**default\_intensity\_fcn** A function for computing default intensity occurring during this timestep, dependent on time and stock price, with arguments `t, S`.

variance_cumulation_fcn	A function for computing total stock variance occurring during this timestep, with arguments $T, t$ . E.g. with a constant volatility $s$ this takes the form $(T - t)s^2$ .
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * $S / S_0$
borrow_cost	Stock borrow cost, affecting the drift rate
dividend_rate	Continuous dividend rate, affecting the drift rate
structure_constant	The maximum ratio between time intervals $dt$ and the square of space intervals $dz^2$
std_devs_width	The number of standard deviations, in $\sigma * \sqrt{T}$ units, to incorporate into the grid
grid_center	A reasonable central value for the grid, defaults to $S_0$ or an instrument strike

**Details**

If any instrument in the instruments has a strike, then the grid will be normalized to the last such instrument's strike.

**See Also**

Other Equity Dependent Default Intensity: [find\\_present\\_value\(\)](#), [fit\\_to\\_option\\_market\\_df\(\)](#), [fit\\_variance\\_cumulation\(\)](#), [implied\\_jump\\_process\\_volatility\(\)](#)

Other Implicit Grid Solver: [construct\\_implicit\\_grid\\_structure\(\)](#), [find\\_present\\_value\(\)](#), [infer\\_conforming\\_time\\_grid\(\)](#), [integrate\\_pde\(\)](#), [iterate\\_grid\\_from\\_timestep\(\)](#), [take\\_implicit\\_timestep\(\)](#), [timestep\\_instruments\(\)](#)

---

GridPricedInstrument-class

*Representation of financial instrument amenable to grid pricing schemes*

---

**Description**

Our basic instrument defines a tenor/maturity, a method to provide values in case of default, and a method to correct instrument prices in light of exercise decisions.

**Fields**

maturity The tenor, expiration date or terminal date by which the value of this security will be certain.

last\_computed\_grid The most recently computed set of values from a grid pricing scheme. Used internally for pricing chains of derivatives.

name A mnemonic name for the instrument, not used by ragtop

**Methods**

`optionality_fcn(v, ...)` Return a version of  $v$  at time  $t$  corrected for any optionality conditions.

`recovery_fcn(v, S, t, ...)` Return recovery value, given non-default values  $v$  at time  $t$ . Subclasses may be more elaborate, this method simply returns 0.0.

`terminal_values(v, ...)` Return a terminal value. defaults to simply calling `optionality_fcn`.

---

`implied_jump_process_volatility`

*Implied volatility of any instrument*

---

**Description**

Use the grid solver to generate instrument prices via `find_present_value` and run them through a bisection root search method until a constant volatility matching the provided instrument price has been found.

**Usage**

```
implied_jump_process_volatility(
    instrument_price,
    instrument,
    ...,
    starting_volatility_estimate = 0.85,
    relative_tolerance = 0.005,
    max.iter = 100,
    max_vola = 4
)
```

**Arguments**

<code>instrument_price</code>	Target price for root finder
<code>instrument</code>	Instrument to search for the target price on, passed as the sole instrument to <a href="#">find_present_value</a>
<code>...</code>	Additional arguments to be passed on to <a href="#">find_present_value</a>
<code>starting_volatility_estimate</code>	Bisection method original guess
<code>relative_tolerance</code>	Relative tolerance in instrument price defining the root-finder halting condition
<code>max.iter</code>	Maximum number of root-finder iterations allowed
<code>max_vola</code>	Maximum volatility to try

**Details**

Unlike `american_implied_volatility`, this routine allows for any legal term structures and equity-linked default intensities. For that reason, it eschews the control variate tricks that make `american_implied_volatility` so much faster.

Note that equity-linked default intensities can result in instrument prices that are not monotonic in volatility. This bisection root finder will find a solution but not necessarily any particular one.

**Value**

A list of present values, with the same names as instruments

**See Also**

`find_present_value` for the underlying pricing algorithm, `implied_volatility_with_term_struct` for European options without equity dependence of default intensity, `american_implied_volatility` for the same on American options

Other Implied Volatilities: `american_implied_volatility()`, `equivalent_bs_vola_to_jump()`, `equivalent_jump_vola_to_bs()`, `fit_variance_cumulation()`, `implied_volatilities()`, `implied_volatilities_v`, `implied_volatility()`, `implied_volatility_with_term_struct()`

Other Equity Dependent Default Intensity: `find_present_value()`, `fit_to_option_market_df()`, `fit_variance_cumulation()`, `form_present_value_grid()`

**Examples**

```
implied_jump_process_volatility(
    25, AmericanOption(maturity=1.1, strike=100, callput=-1),
    S0=100, num_time_steps=50, relative_tolerance=1.e-3)
```

---

`implied_volatilities`    *Implied volatilities of european-exercise options under Black-Scholes or a jump-process extension*

---

**Description**

Find default-free volatilities based on known interest rates and hazard rates, using a given option price.

**Usage**

```
implied_volatilities(
    option_price,
    callput,
    S0,
    K,
    r,
```

```

time,
const_default_intensity = 0,
divrate = 0,
borrow_cost = 0,
dividends = NULL,
relative_tolerance = 1e-06,
max.iter = 100,
max_vola = 4
)

```

### Arguments

option_price	Present option values (may be a vector)
callput	1 for calls, -1 for puts (may be a vector)
S0	initial underlying price (may be a vector)
K	strike (may be a vector)
r	risk-free interest rate (may be a vector)
time	Time from 0 until expiration (may be a vector)
const_default_intensity	hazard rate of underlying default (may be a vector)
divrate	A continuous rate for dividends and other cashflows such as foreign interest rates (may be a vector)
borrow_cost	A continuous rate for stock borrow costs (may be a vector)
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * S / S0. Fixed dividends will be converted to proportional for purposes of this algorithm.
relative_tolerance	Relative tolerance in option price to achieve before halting the search
max.iter	Number of iterations to try before abandoning the search
max_vola	Maximum volatility to try in the search

### Value

Scalar volatilities

### See Also

Other Implied Volatilities: [american\\_implied\\_volatility\(\)](#), [equivalent\\_bs\\_vola\\_to\\_jump\(\)](#), [equivalent\\_jump\\_vola\\_to\\_bs\(\)](#), [fit\\_variance\\_cumulation\(\)](#), [implied\\_jump\\_process\\_volatility\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

Other European Options: [black\\_scholes\\_on\\_term\\_structures\(\)](#), [blackscholes\(\)](#), [implied\\_volatilities\\_with\\_rat](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

Other Equity Independent Default Intensity: [american\(\)](#), [american\\_implied\\_volatility\(\)](#), [black\\_scholes\\_on\\_term\\_structures\(\)](#), [blackscholes\(\)](#), [equivalent\\_bs\\_vola\\_to\\_jump\(\)](#), [equivalent\\_jump\\_vola\\_to\\_bs\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#), [implied\\_volatility\\_with\\_term\\_struct\(\)](#)

---

 implied\_volatilities\_with\_rates\_struct

*Find the implied volatility of european-exercise options with a term structure of interest rates*

---

### Description

Use the provided discount factor function to infer constant short rates applicable to each expiration time, then use the Black-Scholes formula to generate European option values and run them through Newton's method until a constant volatility matching each provided option price has been found.

### Usage

```
implied_volatilities_with_rates_struct(
  option_price,
  callput,
  S0,
  K,
  discount_factor_fcn,
  time,
  const_default_intensity = 0,
  divrate = 0,
  borrow_cost = 0,
  dividends = NULL,
  relative_tolerance = 1e-06,
  max.iter = 100,
  max_vola = 4
)
```

### Arguments

option_price	Present option values (may be a vector)
callput	1 for calls, -1 for puts (may be a vector)
S0	initial underlying prices (may be a vector)
K	strikes (may be a vector)
discount_factor_fcn	A function for computing present values to time t, with arguments T, t
time	Time from 0 until expirations (may be a vector)
const_default_intensity	hazard rates of underlying default (may be a vector)
divrate	A continuous rate for dividends and other cashflows such as foreign interest rates (may be a vector)
borrow_cost	A continuous rate for stock borrow costs (may be a vector)

dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * S / S0. Fixed dividends will be converted to proportional for purposes of this algorithm.
relative_tolerance	Relative tolerance in option price to achieve before halting the search
max.iter	Number of iterations to try before abandoning the search
max_vola	Maximum volatility to try in the search

### Details

Differs from `implied_volatility_with_term_struct` by first computing constant interest rates for each option, and then calling `implied_volatilities`

### Value

Scalar volatilities

### See Also

`implied_volatility` for simpler cases with constant parameters, `implied_volatilities` for the underlying algorithm with constant rates, `implied_volatility_with_term_struct` when volatilities or survival probabilities also have a nontrivial term structure

Other Implied Volatilities: `american_implied_volatility()`, `equivalent_bs_vola_to_jump()`, `equivalent_jump_vola_to_bs()`, `fit_variance_cumulation()`, `implied_jump_process_volatility()`, `implied_volatilities()`, `implied_volatility()`, `implied_volatility_with_term_struct()`

Other European Options: `black_scholes_on_term_structures()`, `blackscholes()`, `implied_volatilities()`, `implied_volatility()`, `implied_volatility_with_term_struct()`

Other Equity Independent Default Intensity: `american()`, `american_implied_volatility()`, `black_scholes_on_term_structures()`, `blackscholes()`, `equivalent_bs_vola_to_jump()`, `equivalent_jump_vola_to_bs()`, `implied_volatilities()`, `implied_volatility()`, `implied_volatility_with_term_struct()`

### Examples

```
d_fcn = function(T,t) {exp(-0.03*(T-t))}
implied_volatilities_with_rates_struct(c(23,24,25),
  c(-1,1,1), 100, 100,
  discount_factor_fcn=d_fcn, time=c(4,4,5))
```

---

<code>implied_volatility</code>	<i>Implied volatility of european-exercise option under Black-Scholes or a jump-process extension</i>
---------------------------------	---

---

### Description

Find default-free volatility (not necessarily just Black-Scholes) based on known interest rates and hazard rates, using a given option price.

**Usage**

```

implied_volatility(
  option_price,
  callput,
  S0,
  K,
  r,
  time,
  const_default_intensity = 0,
  divrate = 0,
  borrow_cost = 0,
  dividends = NULL,
  relative_tolerance = 1e-06,
  max.iter = 100,
  max_vola = 4
)

```

**Arguments**

option_price	Present option value
callput	1 for calls, -1 for puts
S0	initial underlying price
K	strike
r	risk-free interest rate
time	Time from 0 until expiration
const_default_intensity	hazard rate of underlying default
divrate	A continuous rate for dividends and other cashflows such as foreign interest rates
borrow_cost	A continuous rate for stock borrow costs
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * S / S0. Fixed dividends will be converted to proportional for purposes of this algorithm. To handle truly fixed dividends, see <a href="#">implied_jump_process_volatility</a>
relative_tolerance	Relative tolerance in option price to achieve before halting the search
max.iter	Number of iterations to try before abandoning the search
max_vola	Maximum volatility to try in the search

**Details**

To get a straight Black-Scholes implied volatility, simply call this function with `const_default_intensity` set to zero (the default).

**Value**

A scalar volatility

**See Also**

Other Implied Volatilities: `american_implied_volatility()`, `equivalent_bs_vola_to_jump()`, `equivalent_jump_vola_to_bs()`, `fit_variance_cumulation()`, `implied_jump_process_volatility()`, `implied_volatilities()`, `implied_volatilities_with_rates_struct()`, `implied_volatility_with_term_struct()`

Other Equity Independent Default Intensity: `american()`, `american_implied_volatility()`, `black_scholes_on_term_structures()`, `blackscholes()`, `equivalent_bs_vola_to_jump()`, `equivalent_jump_vola_to_bs()`, `implied_volatilities()`, `implied_volatilities_with_rates_struct()`, `implied_volatility_with_term_struct()`

Other European Options: `black_scholes_on_term_structures()`, `blackscholes()`, `implied_volatilities()`, `implied_volatilities_with_rates_struct()`, `implied_volatility_with_term_struct()`

**Examples**

```
implied_volatility(2.5, 1, 100, 105, 0.01, 0.75)
implied_volatility(option_price = 17,
                   callput = CALL, S0 = 250, K=245,
                   r = 0.005, time = 2,
                   const_default_intensity = 0.03)
```

---

`implied_volatility_with_term_struct`

*Find the implied volatility of a european-exercise option with term structures*

---

**Description**

Use the Black-Scholes formula to generate European option values and run them through Newton's method until a constant volatility matching the provided option price has been found.

**Usage**

```
implied_volatility_with_term_struct(
  option_price,
  callput,
  S0,
  K,
  time,
  ...,
  starting_volatility_estimate = 0.5,
  relative_tolerance = 1e-06,
  max.iter = 100,
  max_vola = 4
)
```

**Arguments**

option_price	Option price to match
callput	1 for calls, -1 for puts
S0	initial underlying price
K	strike
time	Time to expiration
...	Further arguments to be passed on to <code>black_scholes_on_term_structures</code>
starting_volatility_estimate	The Newton method's original guess
relative_tolerance	Relative tolerance in instrument price defining the root-finder halting condition
max.iter	Maximum number of root-finder iterations allowed
max_vola	Maximum volatility to try

**Details**

Differs from `implied_volatility` by calling `black_scholes_on_term_structures` for pricing, thereby allowing term structures of rates, and a nontrivial `survival_probability_fcn`

**Value**

Estimated volatility

**See Also**

[implied\\_volatility](#) for simpler cases with constant parameters, [black\\_scholes\\_on\\_term\\_structures](#) for the underlying pricing algorithm, [implied\\_volatilities\\_with\\_rates\\_struct](#) when neither volatilities nor survival probabilities have a nontrivial term structure

Other Implied Volatilities: [american\\_implied\\_volatility\(\)](#), [equivalent\\_bs\\_vola\\_to\\_jump\(\)](#), [equivalent\\_jump\\_vola\\_to\\_bs\(\)](#), [fit\\_variance\\_cumulation\(\)](#), [implied\\_jump\\_process\\_volatility\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#)

Other Equity Independent Default Intensity: [american\(\)](#), [american\\_implied\\_volatility\(\)](#), [black\\_scholes\\_on\\_term\\_structures\(\)](#), [blackscholes\(\)](#), [equivalent\\_bs\\_vola\\_to\\_jump\(\)](#), [equivalent\\_jump\\_vola\\_to\\_bs\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#)

Other European Options: [black\\_scholes\\_on\\_term\\_structures\(\)](#), [blackscholes\(\)](#), [implied\\_volatilities\(\)](#), [implied\\_volatilities\\_with\\_rates\\_struct\(\)](#), [implied\\_volatility\(\)](#)

**Examples**

```
## Dividends
divs = data.frame(time=seq(from=0.11, to=2, by=0.25),
                  fixed=seq(1.5, 1, length.out=8),
                  proportional = seq(1, 1.5, length.out=8))
surv_prob_fcn = function(T, t, ...) {
  exp(-0.07 * (T - t)) }
```

```

disc_factor_fcn = function(T, t, ...) {
  exp(-0.03 * (T - t)) }
implied_volatility_with_term_struct(
  option_price = 12, S0 = 150, callput=PUT,
  K = 147.50, time=1.5,
  discount_factor_fcn=disc_factor_fcn,
  survival_probability_fcn=surv_prob_fcn,
  dividends=divs)

```

---

infer\_conforming\_time\_grid

*A time grid with extra times inserted for coupons, calls and puts*

---

### Description

At its base, this function chooses a time grid with  $1 + \text{min\_num\_time\_steps}$  elements from 0 to Tmax. Any coupon, call, or put times occurring in one of the supplied instruments are also inserted.

### Usage

```
infer_conforming_time_grid(min_num_time_steps, Tmax, instruments = NULL)
```

### Arguments

min_num_time_steps	The minimum number of timesteps the output vector should have
Tmax	The maximum time on the grid
instruments	A set of instruments whose maturity and terms and conditions can introduce extra timesteps. Each will be queried for the output of a <code>critical_times</code> function.

### Value

A vector of times at which the grid should have nodes

### See Also

Other Implicit Grid Solver: [construct\\_implicit\\_grid\\_structure\(\)](#), [find\\_present\\_value\(\)](#), [form\\_present\\_value\\_grid\(\)](#), [integrate\\_pde\(\)](#), [iterate\\_grid\\_from\\_timestep\(\)](#), [take\\_implicit\\_timestep\(\)](#), [timestep\\_instruments\(\)](#)

---

integrate_pde	<i>Numerically integrate the pricing differential equation</i>
---------------	--

---

### Description

Use an implicit integration scheme to numerically integrate the pricing differential equation for each of the given instruments, backwardating from time Tmax to time 0.

### Usage

```
integrate_pde(
    z,
    min_num_time_steps,
    S0,
    Tmax,
    instruments,
    stock_level_fcn,
    discount_factor_fcn,
    default_intensity_fcn,
    variance_cumulation_fcn,
    dividends = NULL
)
```

### Arguments

z	Space grid value morphable to stock prices using <code>stock_level_fcn</code>
min_num_time_steps	The minimum number of timesteps used. Calls, puts and coupons may result in extra timesteps taken.
S0	Time zero price of the base equity
Tmax	The maximum time on the grid, from which all backwardation steps will take place.
instruments	A list of instruments to be priced. Each one must have a <code>strike</code> and a <code>optionality_fcn</code> , as with <a href="#">GridPricedInstrument</a> and its subclasses.
stock_level_fcn	A function for changing space grid value to stock prices, with arguments <code>z</code> and <code>t</code>
discount_factor_fcn	A function for computing present values to time <code>t</code> of various cashflows occurring during this timestep, with arguments <code>T</code> , <code>t</code>
default_intensity_fcn	A function for computing default intensity occurring during this timestep, dependent on time and stock price, with arguments <code>t</code> , <code>S</code> .

variance_cumulation_fcn	A function for computing total stock variance occurring during this timestep, with arguments $T$ , $t$ . E.g. with a constant volatility $s$ this takes the form $(T - t)s^2$ .
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * $S / S_0$

**Value**

A grid of present values of derivative prices, adapted to  $z$  at each timestep. Time zero value will appear in the first index.

**See Also**

Other Implicit Grid Solver: [construct\\_implicit\\_grid\\_structure\(\)](#), [find\\_present\\_value\(\)](#), [form\\_present\\_value\\_grid\(\)](#), [infer\\_conforming\\_time\\_grid\(\)](#), [iterate\\_grid\\_from\\_timestep\(\)](#), [take\\_implicit\\_timestep\(\)](#), [timestep\\_instruments\(\)](#)

---

is.blank	<i>Return TRUE if the argument is empty, NULL or NA</i>
----------	---

---

**Description**

Return TRUE if the argument is empty, NULL or NA

**Usage**

```
is.blank(x, false.triggers = FALSE)
```

**Arguments**

$x$  Argument to test  
false.triggers Whether to allow nonempty vectors of all FALSE to trigger this condition

---

iterate_grid_from_timestep	<i>Iterate over a set of timesteps to integrate the pricing differential equation</i>
----------------------------	---

---

**Description**

Timestep an implicit integration scheme to numerically integrate the pricing differential equation for each of the given instruments, backwardating from time  $T_{max}$  to time 0.

**Usage**

```

iterate_grid_from_timestep(
    starting_time_step,
    time_pts,
    z,
    S0,
    instruments,
    stock_level_fcn,
    discount_factor_fcn,
    default_intensity_fcn,
    variance_cumulation_fcn,
    dividends = NULL,
    grid = NULL,
    original_grid_values = as.matrix(grid[1 + starting_time_step, , ])
)

```

**Arguments**

starting_time_step	The index into time_pts of the first timestep to be employed. This must be no larger than the length of time_pts, minus one
time_pts	Time nodes to be treated on the grid
z	Space grid value morphable to stock prices using stock_level_fcn
S0	Time zero price of the base equity
instruments	A list of instruments to be priced. Each one must have a strike and a optionality_fcn, as with <a href="#">GridPricedInstrument</a> and its subclasses.
stock_level_fcn	A function for changing space grid value to stock prices, with arguments z and t
discount_factor_fcn	A function for computing present values to time t of various cashflows occurring during this timestep, with arguments T, t
default_intensity_fcn	A function for computing default intensity occurring during this timestep, dependent on time and stock price, with arguments t, S.
variance_cumulation_fcn	A function for computing total stock variance occurring during this timestep, with arguments T, t. E.g. with a constant volatility $s$ this takes the form $(T - t)s^2$ .
dividends	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * S / S0
grid	An optional grid into which results at each timestep will be written. Its size should be at least (1+starting_time_step, length(z), length(instruments))
original_grid_values	Grid values to timestep from

**Value**

Either a populated grid of present values of derivative prices, or a matrix of values at the first time point, adapted to  $z$  at each timestep. Time zero value will appear in the first index of any grid.

**See Also**

Other Implicit Grid Solver: [construct\\_implicit\\_grid\\_structure\(\)](#), [find\\_present\\_value\(\)](#), [form\\_present\\_value\\_grid\(\)](#), [infer\\_conforming\\_time\\_grid\(\)](#), [integrate\\_pde\(\)](#), [take\\_implicit\\_timestep\(\)](#), [timestep\\_instruments\(\)](#)

---

penalty\_with\_intensity\_link

*Helper function (volatility-normalized pricing error) for calibration of equity-linked default intensity*

---

**Description**

Given a set SDE parameters, form a volatility term structure that fairly precisely matches the supplied prices of the variance\_instruments. Then use that term structure and the default intensity to price all the fit\_instruments, and compare them to the fit\_instrument\_prices.

**Usage**

```
penalty_with_intensity_link(
    p,
    s,
    h,
    variance_instruments,
    variance_instrument_prices,
    variance_instrument_spreads,
    fit_instruments,
    fit_instrument_prices,
    fit_instrument_spreads,
    fit_instrument_weights,
    S0,
    num_time_steps = 30,
    const_short_rate = 0,
    discount_factor_fcn = function(T, t) {
        exp(-const_short_rate * (T - t))
    },
    ...,
    relative_spread_tolerance = 0.15,
    num_variance_time_steps = 30
)
```

**Arguments**

p	Power of default intensity
s	Proportion of constant default intensity
h	Base default intensity
variance_instruments	A list of instruments in strictly increasing order of maturity, from which the volatility term structure will be inferred. Once the calibration is finished, the chosen parameters will reproduce the prices of these instruments with fairly high precision.
variance_instrument_prices	Central price targets for the variance instruments
variance_instrument_spreads	Bid-offer spreads used to normalize errors in variance instrument prices during term structure fitting
fit_instruments	A list of instruments in any order, from which the mispricing penalties used for judging fit quality will be computed
fit_instrument_prices	Central price targets for the variance instruments
fit_instrument_spreads	Bid-offer spreads used to normalize errors in fit instrument prices during default intensity
fit_instrument_weights	Weights applied to relative errors in fit instrument prices before summing to form the penalty
S0	Current underlying price
num_time_steps	Time step count passed on to <a href="#">find_present_value</a> while fitting instrument values
const_short_rate	A constant to use for the instantaneous interest rate in case <code>discount_factor_fcn</code> is not given
discount_factor_fcn	A function for computing present values to time <code>t</code> of various cashflows occurring during this timestep, with arguments <code>T</code> , <code>t</code>
...	Further arguments passed to <a href="#">price_with_intensity_link</a>
relative_spread_tolerance	Tolerance to apply in calling <a href="#">fit_variance_cumulation</a>
num_variance_time_steps	Number of time steps to use in calling <a href="#">fit_variance_cumulation</a>

**Details**

Forms implied Black-Scholes volatilities from all supplied mid prices, and their implied bid and offer prices, as well as from the prices computed by the grid solver. Each instrument is then assigned an error term component in proportion to its weight and the pricing error (in implied vol terms) divided by the spread (also in implied vol terms).

**See Also**

[price\\_with\\_intensity\\_link](#) for the pricing function

---

price\_with\_intensity\_link

*Helper function (instrument pricing) for calibration of equity-linked default intensity*

---

**Description**

Given derivative instruments (subclasses of GridPricedInstrument, though typically either [AmericanOption](#) or [EuropeanOption](#) objects), along with their prices and spreads, calibrate variance cumulation (the at-the-money volatility of the continuous process) and then price the instruments via equity linked default intensity of the form  $h(s + (1-s)(S_0/S_t)^p)$ .

**Usage**

```
price_with_intensity_link(
    p,
    s,
    h,
    variance_instruments,
    variance_instrument_prices,
    variance_instrument_spreads,
    fit_instruments,
    S0,
    num_time_steps = 30,
    ...,
    relative_spread_tolerance = 0.15,
    num_variance_time_steps = 30
)
```

**Arguments**

p	Power of default intensity
s	Proportion of constant default intensity
h	Base default intensity
variance_instruments	A list of instruments in strictly increasing order of maturity, from which the volatility term structure will be inferred. Once the calibration is finished, the chosen parameters will reproduce the prices of these instruments with fairly high precision.
variance_instrument_prices	Central price targets for the variance instruments

variance_instrument_spreads	Bid-offer spreads used to normalize errors in variance instrument prices during term structure fitting
fit_instruments	A list of instruments in any order, from which the mispricing penalties used for judging fit quality will be computed
S0	Current underlying price
num_time_steps	Time step count passed on to <code>find_present_value</code> while fitting instrument values
...	Further arguments passed to both <code>fit_variance_cumulation</code> and to <code>find_present_value</code>
relative_spread_tolerance	Tolerance to apply in calling <code>fit_variance_cumulation</code>
num_variance_time_steps	Number of time steps to use in calling <code>fit_variance_cumulation</code>

---

PUT	<i>Constant PUT for defining option contracts</i>
-----	---

---

**Description**

Constant PUT for defining option contracts

**Usage**

PUT

**Format**

An object of class `numeric` of length 1.

---

ragtop	<i>Pricing schemes for derivatives using equity-linked default intensity</i>
--------	--

---

**Description**

Using numerical integration, we price convertible bonds, straight bonds, equity options and various other derivatives consistently using a jump-diffusion model in which default intensity can vary with equity price in a user-specified deterministic manner.

## Details

We apply the stochastic model

$$dS/S = (r + h - q)dt + \sigma dZ - dJ$$

where  $r$  and  $q$  play their usual roles,  $h$  is a deterministic function of stock price and time, and  $J$  is a Poisson jump process adapted to the *default intensity* or *hazard rate*  $h$ . This model is a *jump-diffusion* extension of Black-Scholes, with the jump process  $J$  representing default, compensated by extra drift in the equity at rate  $h$ .

Volatilities, default intensities and risk-free rates may all be represented with arbitrary term structures. Default intensity term structures may also take the underlying equity price into account.

Pricing in the standard Black-Scholes model is a special case with default intensity set to zero. Therefore this package *also* serves to price securities in the standard Black-Scholes model, while still allowing risk-free rates and volatilities have nontrivial term structures.

## Important Features

**Black-Scholes** The standard model is automatically supported as a special case, but also has optimized routines

**Term Structures** The package allows for any kind of instrument to be priced with time-varying rates, volatility and default intensity

**Dividends** Allows for discrete dividends in an arbitrary combination of fixed and proportional amounts. The difference between fixed and proportional can be up to 10 percent in implied volatility terms.

**Calibration** Model calibration routines are included

**Bankruptcy Realism** A parsimonious deterministic model of default intensity gives rich behavior and conforms reasonably well to observed market data

**Algorithm Parameters** Default parameters for the algorithm work well for a very wide variety of pricing and implied volatility scenarios

## Author(s)

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## Examples

```
## Vanilla European exercise
blackscholes(callput=-1, S0=100, K=90, r=0.03, time=1, vola=0.5)
blackscholes(PUT, S0=100, K=90, r=0.03, time=1, vola=0.5,
             default_intensity=0.07, borrow_cost=0.005)
## With a term structure of volatility
## Not run:
black_scholes_on_term_structures(callput=-1, S0=100, K=90, time=1,
                                const_short_rate=0.025,
                                variance_cumulation_fcn = function(T, t) {
                                  0.45 ^ 2 * (T - t) + 0.15^2 * max(0, T-0.25)
                                })
```

```

## End(Not run)

## Vanilla American exercise
## Not run:
american(PUT, S0=100, K=110, time=0.77, const_short_rate = 0.06,
          const_volatility=0.20, num_time_steps=200)

## End(Not run)
## With a term structure of volatility
## Not run:
american(callput=-1, S0=100, K=90, time=1, const_short_rate=0.025,
          variance_cumulation_fcn = function(T, t) {
            0.45 ^ 2 * (T - t) + 0.15^2 * max(0, T-0.25)
          })

## End(Not run)
## With discrete dividends, combined fixed and proportional
divs = data.frame(time=seq(from=0.11, to=2, by=0.25),
                  fixed=seq(1.5, 1, length.out=8),
                  proportional = seq(1, 1.5, length.out=8))
## Not run:
american(callput=-1, S0=100, K=90, time=1, const_short_rate=0.025,
          const_volatility=0.20, dividends=divs)

## End(Not run)

## American Exercise Implied Volatility
american_implied_volatility(25,CALL,S0=100,K=100,time=2.2, const_short_rate=0.03)
df250 = function(t) ( exp(-0.02*t)*exp(-0.03*max(0,t-1.0))) # Simple term structure
df25 = function(T,t){df250(T)/df250(t)} # Relative discount factors
## Not run:
american_implied_volatility(25,-1,100,100,2.2,discount_factor_fcn=df25)

## End(Not run)

## Convertible Bond
## Not Run
pct4 = function(T,t=0) { exp(-0.04*(T-t)) }
cb = ConvertibleBond(conversion_ratio=3.5, maturity=1.5, notional=100,
                    discount_factor_fcn=pct4, name='Convertible')
S0 = 10; p = 6.0; h = 0.10
h_fcn = function(t, S, ...){0.9 * h + 0.1 * h * (S0/S)^p } # Intensity linked to equity price
## Not run:
find_present_value(S0=S0, instruments=list(Convertible=cb), num_time_steps=250,
                  default_intensity_fcn=h_fcn,
                  const_volatility = 0.4, discount_factor_fcn=pct4,
                  std_devs_width=5)

## End(Not run)

## Fitting Term Structure of Volatility
## Not Run
opts = list(m1=AmericanOption(callput=-1, strike=9.9, maturity=1/12, name="m1"),

```

```

        m2=AmericanOption(callput=-1, strike=9.8, maturity=1/6, name="m2"))
## Not run:
vfit = fit_variance_cumulation(S0, opts, c(0.6, 0.8), default_intensity_fcn=h_fcn)
print(vfit$volatilities)

## End(Not run)

```

---

shift\_for\_dividends     *Shift a set of grid values for dividends paid, using spline interpolation*

---

### Description

Shift a set of grid values for dividends paid, using spline interpolation

### Usage

```
shift_for_dividends(grid_values_before_shift, stock_prices, div_sum)
```

### Arguments

grid_values_before_shift	Values on grid before accounting for expected dividends
stock_prices	Stock prices for which to shift the grid
div_sum	Sum of dividend values at each grid point

### Value

An object like `grid_values_before_shift` with entries shifted according to the dividend sums

### See Also

Other Dividends: [adjust\\_for\\_dividends\(\)](#), [time\\_adj\\_dividends\(\)](#)

---

spot\_to\_df\_fcn     *Create a discount factor function from a yield curve*

---

### Description

Use a piecewise constant approximation to the given spot curve to generate a function capable of returning corresponding discount factors

### Usage

```
spot_to_df_fcn(yield_curve)
```

**Arguments**

yield\_curve      A data.frame with numeric columns time (in increasing order) and rate (in natural units)

**Value**

A function taking two time arguments, which returns the discount factor from the second to the first

**Examples**

```
disct_fcn = ragtop::spot_to_df_fcn(
  data.frame(time=c(1, 5, 10, 15),
             rate=c(0.01, 0.02, 0.03, 0.05)))
print(disct_fcn(1, 0.5))
```

---

take\_implicit\_timestep

*Backwarddate grid values one timestep*

---

**Description**

Take one timestep of an implicit solver for a given instrument

**Usage**

```
take_implicit_timestep(
  t,
  S,
  full_discount_factor,
  local_discount_factor,
  discount_factor_fcn,
  prev_grid_values,
  survival_probabilities,
  tridiag_matrix_entries,
  instrument = NULL,
  dividends = NULL,
  instr_name = "this instrument"
)
```

**Arguments**

t                      Time after this timestep has been taken

S                      Underlying equity values for the grid

full\_discount\_factor      A discount factor for the transform from grid values to actual derivative prices

local\_discount\_factor      A discount factor to apply to recovery values

discount_factor_fcn	A function for computing present values to time $t$ of various cashflows occurring during this timestep, with arguments $T, t$
prev_grid_values	A vector of space grid values from the previously calculated timestep
survival_probabilities	Vector of probabilities of survival for each space grid node
tridiag_matrix_entries	Diagonal, superdiagonal and subdiagonal of tridiagonal matrix from the numerical integrator
instrument	If not NULL/NA, must have a <code>recovery_fcn</code> and an <code>optionality_fcn</code> though those properties are themselves allowed to be NA.
dividends	A <code>data.frame</code> with columns <code>time</code> , <code>fixed</code> , and <code>proportional</code> . Dividend size at the given time is then expected to be equal to <code>fixed + proportional * S / S0</code>
instr_name	Name of instrument to use in log messages

**Value**

Grid values for the instrument after taking the implicit timestep

**See Also**

Other Implicit Grid Solver: [construct\\_implicit\\_grid\\_structure\(\)](#), [find\\_present\\_value\(\)](#), [form\\_present\\_value\\_grid\(\)](#), [infer\\_conforming\\_time\\_grid\(\)](#), [integrate\\_pde\(\)](#), [iterate\\_grid\\_from\\_timestep\(\)](#), [timestep\\_instruments\(\)](#)

---

`timestep_instruments` *Take an implicit timestep for all the given instruments*

---

**Description**

Backwarddate grid values for all the given instruments from a set of grid values matched to time  $t+dt$  to form a new set of grid value as of time  $t$ .

**Usage**

```
timestep_instruments(
  z,
  prev_grid_values,
  t,
  dt,
  S0,
  instruments,
  stock_level_fcn,
  discount_factor_fcn,
```

```

    default_intensity_fcn,
    variance_cumulation_fcn,
    dividends = NULL
)

```

### Arguments

**z** Space grid value morphable to stock prices using `stock_level_fcn`

**prev\_grid\_values** A matrix with one column for each instrument and one row for each of the  $N$  values of `z`

**t** Time after this timestep has been taken

**dt** Interval to the end of this timestep

**S0** Time zero price of the base equity

**instruments** Instruments corresponding to layers of the value grid in `prev_grid_values`

**stock\_level\_fcn** A function for changing space grid value to stock prices, with arguments `z` and `t`

**discount\_factor\_fcn** A function for computing present values to time `t` of various cashflows occurring during this timestep, with arguments `T`, `t`

**default\_intensity\_fcn** A function for computing default intensity occurring during this timestep, dependent on time and stock price, with arguments `t`, `S`.

**variance\_cumulation\_fcn** A function for computing total stock variance occurring during this timestep, with arguments `T`, `t`. E.g. with a constant volatility  $s$  this takes the form  $(T - t)s^2$ .

**dividends** A `data.frame` with columns `time`, `fixed`, and `proportional`. Dividend size at the given time is then expected to be equal to `fixed + proportional * S / S0`

### Value

Grid values after applying an implicit timestep

### See Also

Other Implicit Grid Solver: [construct\\_implicit\\_grid\\_structure\(\)](#), [find\\_present\\_value\(\)](#), [form\\_present\\_value\\_grid\(\)](#), [infer\\_conforming\\_time\\_grid\(\)](#), [integrate\\_pde\(\)](#), [iterate\\_grid\\_from\\_timestep\(\)](#), [take\\_implicit\\_timestep\(\)](#)

---

time\_adj\_dividends      *Find the sum of time-adjusted dividend values*

---

### Description

For each of the N elements of S/h find the sum of the given M dividends, discounted to t\_final by r and h

### Usage

```
time_adj_dividends(relevant_divs, t_final, r, h, S, S0)
```

### Arguments

relevant_divs	A data.frame with columns time, fixed, and proportional. Dividend size at the given time is then expected to be equal to fixed + proportional * S / S0
t_final	Time beyond which to ignore dividends
r	risk-free interest rate
h	Default intensities
S	Stock prices
S0	initial underlying price

### Value

Sum of dividends, at each grid node

### See Also

Other Dividends: [adjust\\_for\\_dividends\(\)](#), [shift\\_for\\_dividends\(\)](#)

---

TIME\_RESOLUTION\_FACTOR

*Constant to define when times are considered so close to each other that they should be treated as simultaneous*

---

### Description

Constant to define when times are considered so close to each other that they should be treated as simultaneous

### Usage

```
TIME_RESOLUTION_FACTOR
```

**Format**

An object of class `numeric` of length 1.

---

TIME\_RESOLUTION\_SIGNIF\_DIGITS

*Constant to define when times are considered so close to each other that they should be treated as simultaneous, in terms of significant digits*

---

**Description**

Constant to define when times are considered so close to each other that they should be treated as simultaneous, in terms of significant digits

**Usage**

TIME\_RESOLUTION\_SIGNIF\_DIGITS

**Format**

An object of class `numeric` of length 1.

---

treasury_df	<i>Get a US Treasury curve discount factor function</i>
-------------	---

---

**Description**

This is a caching wrapper for [treasury\\_df\\_raw](#)

**Usage**

```
treasury_df(..., envir = parent.frame())
```

**Arguments**

...	Arguments passed to <a href="#">treasury_df_raw</a>
envir	Environment passed to <a href="#">treasury_df_raw</a>

**Value**

A function taking two time arguments, which returns the discount factor from the second to the first (see [spot\\_to\\_df\\_fcn](#))

---

treasury_df_raw	<i>Get a US Treasury curve discount factor function</i>
-----------------	---

---

**Description**

Get a US Treasury curve discount factor function

**Usage**

```
treasury_df_raw(on_date)
```

**Arguments**

on\_date            Date for which to query for the curve, year-month-day format

**Value**

A function taking two time arguments, which returns the discount factor from the second to the first

---

TSLAMarket	<i>Market information snapshot for TSLA options</i>
------------	---

---

**Description**

A dataset containing option contract details and a snapshot of market prices for Tesla Motors (TSLA) equity options, interest rates and an equity price.

**Usage**

```
data(TSLAMarket)
```

**Format**

A list with these prices and rates

**Details**

The TSLAMarket list contains three elements:

S0 The stock price as of snapshot time

risk\_free\_rates The spot risk-free rate curve as of snapshot time

options A data frame with details of the options market

---

 value\_from\_prior\_coupons

*Present value of past coupons paid*


---

**Description**

Present value as of time `t` for coupons paid since the `model_t`

**Usage**

```
value_from_prior_coupons(t, coupons_df, discount_factor_fcn, model_t = 0)
```

**Arguments**

<code>t</code>	The time toward which all coupons should be present valued
<code>coupons_df</code>	A data.frame of details for each coupon. It should have the columns <code>payment_time</code> and <code>payment_size</code> .
<code>discount_factor_fcn</code>	A function specifying how the contract says future coupons should be discounted for this instrument in case the acceleration clause is triggered
<code>model_t</code>	The payment time beyond which coupons will be included in this computation

**See Also**

Other Bond Coupons: [accelerated\\_coupon\\_value\(\)](#), [coupon\\_value\\_at\\_exercise\(\)](#)

---

 variance\_cumulation\_from\_vols

*Create a variance cumulation function from a volatility term structure*


---

**Description**

Given a volatility term structure, create a corresponding variance cumulation function. The function assumes piecewise constant forward volatility, with the final such forward volatility extending to infinity.

**Usage**

```
variance_cumulation_from_vols(vols_df)
```

**Arguments**

<code>vols_df</code>	A data.frame with numeric columns <code>time</code> (in increasing order) and <code>volatility</code> (not decreasing so quickly as to give negative forward variance)
----------------------	--

**Value**

A function taking two time arguments, which returns the cumulated variance from the second to the first

**Examples**

```
vc = variance_cumulation_from_vols(  
    data.frame(time=c(0.1,2,3),  
               volatility=c(0.2,0.5,1.2)))  
vc(1.5, 0)
```

---

ZeroCouponBond-class    *A simple contract paying the notional amount at the maturity*

---

**Description**

A simple contract paying the notional amount at the maturity

**Fields**

`notional` The amount that will be paid at maturity, conditional on survival

`recovery_rate` The proportion of notional that would be expected to be paid to bond holders after bankruptcy court proceedings

`discount_factor_fcn` A function specifying how cashflows should generally be discounted for this instrument

**Methods**

`optionality_fcn(v, ...)` Return a version of `v` at time `t` corrected for any optionality conditions.

`recovery_fcn(v, S, t, ...)` Return recovery value, given non-default values `v` at time `t`. Sub-classes may be more elaborate, this method simply returns 0.0.

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