

# Package ‘sharpPen’

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**Version** 2.0

**Title** Penalized Data Sharpening for Local Polynomial Regression

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**Depends** KernSmooth, glmnet, np, Matrix, locpol

**Description** Functions and data sets for data sharpening.  
Nonparametric regressions are computed subject to smoothness  
and other kinds of penalties.

**License** Unlimited

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data_sharpening	<i>Penalized data sharpening for Local Linear, Quadratic and Cubic Regression</i>
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## Description

Penalized data sharpening has been proposed as a way to enforce certain constraints on a local polynomial regression estimator. In addition to a bandwidth, a coefficient of the penalty term is also required. We propose propose systematic approaches for choosing these tuning parameters, in part, by considering the optimization problem from the perspective of ridge regression.

## Usage

```
data_sharpening(xx,yy,zz,p,h=NULL,gammaest=NULL,penalty,lambda=NULL)
```

## Arguments

xx	numeric vector of x data. Missing values are not accepted.
yy	numeric vector of y data. This must be same length as x, and missing values are not accepted.
zz	numeric vector of gridpoint z data. Missing values are not accepted.
p	degree of local polynomial used.
h	the kernel bandwidth smoothing parameter. If NULL, this value will be estimated by function dpill for Local Linear Regression, and will be estimated by function dpilc for Local Quadratic and Cubic Regression.
gammaest	the shape constraint parameter. Cannot be NULL for Periodic shape constraint. Can be NULL for Exponential shape constraint.
penalty	the type of shape constraint, can be "Exponential" and "Periodicity".
lambda	a coefficient of the penalty term, default is NULL.

## Value

the sharpened response variable.

## Author(s)

D.Wang and W.J.Braun

**Examples**

```

set.seed(1234567)
gam<-4
gamest<-gam
g <- function(x) 3*sin(x*(gam*pi))+5*cos(x*(gam*pi))+6*x
sigma<-3
xx<-seq(0,1,length=100)
yy<-g(xx)+rnorm(100,sd=sigma)
zz<-xx
h1<-dpilc(xx,yy)
local_fit<-t(lprOperator(h=h1,xx=xx,zz=zz,p=2))%*%yy
y_sharp<-data_sharpening(xx=xx,yy=yy,zz=zz,p=2,gammaest=gamest,penalty="Periodicity")
sharp_fit<-t(lprOperator(h=h1,xx=xx,zz=zz,p=2))%*%y_sharp
plot(c(min(xx),max(xx)),c(min(yy)-0.5,max(yy)+0.5),type="n",,xlab="x",ylab="y")
legend("bottomright",legend=c("curve_local","curve_sharpen"),col=c(1,3),bty="n",pch=c("-", "-"))
lines(xx,local_fit)
lines(xx,sharp_fit,col=3,lwd=2)
points(xx,yy,col=rgb(0.8,0.2,0.2,0.2))

```

---

derivOperator

*Shape Constraint Matrix Construction*


---

**Description**

Construct a shape constraint matrix at a corresponding sequence of x data and sequence of gridpoint z.

**Usage**

```
derivOperator(penalty,gamma,h, xx,zz,p)
```

**Arguments**

penalty	the type of shape constraint, can be "drv1", "drv2", "drv3", "drv4", "Exponential" and "Periodicity".
gamma	the shape constraint parameter
h	the kernel bandwidth smoothing parameter.
xx	numeric vector of x data. Missing values are not accepted.
zz	numeric vector of gridpoint z data. Missing values are not accepted.
p	degree of local polynomial used.

**Value**

shape constraint matrix

**Author(s)**

X.J. Hu

---

 dpilc
 

---

*Select a Bandwidth for Local Quadratic and Cubic Regression*


---

### Description

Use direct plug-in methodology to select the bandwidth of a local quadratic and local cubic Gaussian kernel regression estimate, as an extension of Wand's `dpill` function.

### Usage

```
dpilc(xx, yy, blockmax = 5, divisor = 20, trim = 0.01,
      proptrun = 0.05, gridsize = 401L, range.x = range(x))
```

### Arguments

<code>xx</code>	numeric vector of x data. Missing values are not accepted.
<code>yy</code>	numeric vector of y data. This must be same length as x, and missing values are not accepted.
<code>blockmax</code>	the maximum number of blocks of the data for construction of an initial parametric estimate.
<code>divisor</code>	the value that the sample size is divided by to determine a lower limit on the number of blocks of the data for construction of an initial parametric estimate.
<code>trim</code>	the proportion of the sample trimmed from each end in the x direction before application of the plug-in methodology.
<code>proptrun</code>	the proportion of the range of x at each end truncated in the functional estimates.
<code>gridsize</code>	number of equally-spaced grid points over which the function is to be estimated.
<code>range.x</code>	vector containing the minimum and maximum values of x at which to compute the estimate. For density estimation the default is the minimum and maximum data values with 5% of the range added to each end. For regression estimation the default is the minimum and maximum data values.

### Details

This function is a local cubic (also quadratic) extension of the `dpill` function of Wand's KernSmooth package. The kernel is the standard normal density. Least squares octic fits over blocks of data are used to obtain an initial estimate. As in Wand's implementation of the Ruppert, Sheather and Wand selector, Mallow's  $C_p$  is used to select the number of blocks. An option is available to make use of a periodic penalty (with possible trend) relating the 4th derivative of the regression function to a constant ( $\gamma$ ) times the 2nd derivative. This avoids the need to calculate the octic fits and reverts back to the original quartic fits of `dpill` with appropriate adjustments to the estimated functionals needed in the direct-plug-in bandwidth calculation. This code is similar to `dpilq` but uses a 6th degree polynomial approximation instead of an 8th degree polynomial approximation.

### Value

the selected bandwidth.

**Warning**

If there are severe irregularities (i.e. outliers, sparse regions) in the x values then the local polynomial smooths required for the bandwidth selection algorithm may become degenerate and the function will crash. Outliers in the y direction may lead to deterioration of the quality of the selected bandwidth.

**Author(s)**

D.Wang and W.J.Braun

**References**

Ruppert, D., Sheather, S. J. and Wand, M. P. (1995). An effective bandwidth selector for local least squares regression. *Journal of the American Statistical Association*, **90**, 1257–1270.

Wand, M. P. and Jones, M. C. (1995). *Kernel Smoothing*. Chapman and Hall, London.

**See Also**

[ksmooth](#), [locpoly](#).

**Examples**

```
x <- faithful$eruptions
y <- faithful$waiting
plot(x, y)
h <- dpilc(x, y)
fit <- locpoly(x, y, bandwidth = h, degree=1)
lines(fit)
h <- dpilc(x, y)
fit <- locpoly(x, y, bandwidth = h, degree=2)
lines(fit, col=3, lwd=2)
fit <- locpoly(x, y, bandwidth = h, degree=3)
lines(fit, col=2, lwd=2)
```

---

dpilc\_PTW

*dpilc\_PTW: Local Polynomial Bandwidth Estimation with Blockwise Selection and Pointwise Results*

---

**Description**

The function uses raw or trimmed data, applies grid-based binning, and estimates local bandwidth based on the provided parameters.

**Usage**

```
dpilc_PTW(xx, yy, blockmax = 5, divisor = 20, trim = 0.01, proptrun = 0.05,
          gridsize = 401L, range.x = range(x), use_raw_data = FALSE)
```

**Arguments**

xx	A numeric vector of x-values.
yy	A numeric vector of y-values, corresponding to the x-values in xx.
blockmax	An integer specifying the maximum number of blocks to be used in the block-wise selection. Default is 5.
divisor	An integer that controls the block size. Default is 20.
trim	A numeric value between 0 and 1 specifying the proportion of data to be trimmed from the extremes. Default is 0.01.
proptrun	A numeric value between 0 and 1 indicating the proportion of data to be excluded from the running procedure. Default is 0.05.
gridsize	An integer specifying the number of grid points to be used. Default is 401L.
range.x	A numeric vector of length 2 indicating the range over which the smoothing is applied. Default is the range of xx.
use_raw_data	A logical value indicating whether to use the raw data (TRUE) or trimmed data (FALSE) for analysis (default is FALSE).

**Details**

This function provides a point-wise calculation of the functional  $\theta(4,4)$  at each data point  $(x_i)$ . It employs various auxiliary functions for binning the data, calculating local polynomial estimations, and performing necessary cross-validation. The function returns a point-wise estimate of the relevant quantity, which is used for localized analysis of the data distribution.

The core methodology used in this function is based on the nonparametric regression framework. For detailed information on the theoretical aspects and derivations, refer to Chapter 3 of Fan and Gijbels (1996).

**Value**

A list with three elements:

x	A numeric vector of x-values.
y	A numeric vector of y-values.
h	A numeric vector of bandwidth values computed for each corresponding x-value.

**Author(s)**

D.Wang and W.J.Braun

**References**

Fan, J., & Gijbels, I. (1996). *Local Polynomial Modelling and its Applications*. Chapman and Hall/CRC.

**See Also**

[locpoly](#)

**Examples**

```
# Example usage:
x <- rnorm(100)
y <- rnorm(100)

# Run the pointwise estimation
result <- dpilc_PTW(x, y, blockmax = 5, divisor = 20, trim = 0.01,
  proptrun = 0.05, gridsize = 40, range.x = range(x),
  use_raw_data = TRUE)

# Inspect the result
plot(result$x, result$h, type = "l", col = "blue", xlab = "X", ylab = "Bandwidth Estimate")
```

DR\_sharpen

*Shape-Constrained Local Linear Regression via Douglas-Rachford***Description**

Local linear regression is applied to bivariate data. The response is ‘sharpened’ or perturbed in a way to render a curve estimate that satisfies some specified shape constraints.

**Usage**

```
DR_sharpen(
  x, y, xgrid=NULL, M=200, h=NULL, mode=NULL,
  ratio_1=0.14, ratio_2=0.14, ratio_3=0.14, ratio_4=0.14,
  constraint_1=NULL, constraint_2=NULL, constraint_3=NULL,
  constraint_4=NULL, norm="l2", augmentation=FALSE, maxit = 10^5)
```

**Arguments**

x	a vector of explanatory variable observations
y	binary vector of responses
xgrid	gridpoints on x-axis where estimates are taken
M	number of equally-spaced gridpoints (if xgrid not specified)
h	bandwidth
mode	the location of the peak on the x-axis, valid in the unimode case
ratio_1	control the first derivative shape constraint gap around the peak, valid in the unimode case
ratio_2	control the second derivative shape constraint gap around the peak, valid in the unimode case
ratio_3	control the third derivative shape constraint gap around the peak, valid in the unimode case
ratio_4	control the fourth derivative shape constraint gap around the peak, valid in the unimode case

constraint_1	a vector of the first derivative shape constraint
constraint_2	a vector of the second derivative shape constraint
constraint_3	a vector of the third derivative shape constraint
constraint_4	a vector of the fourth derivative shape constraint
norm	the smallest possible distance type: "l2", "l1" or "linf". Default is "l2"
augmentation	data augmentation: "TRUE" or "FALSE", default is "FALSE"
maxit	maximum iteration number, default is 10 <sup>5</sup>

### Details

Data are perturbed the smallest possible L2 or L1 or Linf distance subject to the constraint that the local linear estimate satisfies some specified shape constraints.

### Value

ysharp	sharpened responses
iteration	number of iterations the function has been spend for the convergence

### Author(s)

D.Wang and W.J.Braun

### References

Wang, D. (2022). Penalized and constrained data sharpening methods for kernel regression (Doctoral dissertation, University of British Columbia).

### Examples

```
set.seed(1234567)
gam<-4
g <- function(x) (3*sin(x*(gam*pi))+5*cos(x*(gam*pi))+6*x)*x
n<-100
M<-200
noise <- 1
x<-sort(runif(n,0,1))
y<-g(x)+rnorm(n,sd=noise)
z<- seq(min(x)+1/M, max(x)-1/M, length=M) #####xgrid points
h1<-dpill(x,y)
A<-lprOperator(h=h1,x=x,z=z,p=1)
local_fit<-t(A)
ss_1<-c(sign(numericalDerivative(z,g,k=1)))
DR_sharpen(x=x, y=y, xgrid=z, h=h1, constraint_1=ss_1, norm="linf",maxit =10^3)
```

---

`lprOperator`*Local Polynomial Estimator Matrix Construction*

---

**Description**

Construct a matrix based on the local polynomial estimation at a corresponding sequence of x data and sequence of gridpoint z.

**Usage**

```
lprOperator(h, xx, zz, p)
```

**Arguments**

h	the kernel bandwidth smoothing parameter.
xx	numeric vector of x data. Missing values are not accepted.
zz	numeric vector of gridpoint z data. Missing values are not accepted.
p	degree of local polynomial used.

**Value**

local polynomial estimator matrix

**Author(s)**

X.J. Hu

---

`noontemp`*Noon Temperatures in Winnipeg, Manitoba*

---

**Description**

Time Series of noon temperature observations from the Winnipeg International Airport from January 1, 1960 through December 31, 1980.

**Usage**

```
data(noontemp)
```

**Format**

A single vector.

---

numericalDerivative    *Numerical Derivative of Smooth Function*

---

### Description

Cubic spline interpolation of columns of a matrix for purpose of computing numerical derivatives at a corresponding sequence of gridpoints.

### Usage

```
numericalDerivative(x, g, k, delta=.001)
```

### Arguments

x	numeric vector
g	numeric-valued function of x
k	number of derivatives to be computed
delta	denominator of Newton quotient approximation

### Value

numeric vector of kth derivative of g(x)

### Author(s)

W.J. Braun

---

projection\_C    *Projection operator for rectangle or nonnegative space*

---

### Description

Compute the projection operator for rectangle or nonnegative space. For example, we construct

$$\lambda P_C(x/\lambda) = \text{projection}_C(\lambda, C, x)$$

, where  $C$  can be rectangle or nonnegative space.

### Usage

```
projection_C(
  lambda, family=c("rectangle", "nonnegative"),
  input, bound=c(-1, 1))
```

**Arguments**

lambda	parameter $\lambda$ in the above equation
family	type of $C$ , can be rectangle or nonnegative space
input	input $x$ in the above equation
bound	lower bound and upper bound for rectangle

**Details**

Take  $x$  as input,  $\lambda$  as parameter. Calculate  $\lambda P_C(x/\lambda)$  for a given  $C$  family

**Value**

projection  $\lambda P_C(x/\lambda)$

**Author(s)**

D.Wang and W.J.Braun

**Examples**

```
set.seed(1234567)
family <- "nonnegative"
temp_p1 <- runif(10, -1, 1)
projection_C(0.5, family=family, temp_p1)
```

---

projection\_nb

*Projection operator for norm balls.*

---

**Description**

Compute the projection operator for norm balls. For example, we construct

$$\lambda P_{B_{\|\cdot\|_*}[0,r]}(x/\lambda) = \text{projection}_{nb}(\lambda, r, \|\cdot\|_*, x)$$

, where  $\|\cdot\|_*$  can be  $l_1$ -norm,  $l_2$ -norm, and  $l_\infty$ -norm.

**Usage**

```
projection_nb(
  lambda, radius, family=c("norm2", "norm1", "norminf"),
  input)
```

**Arguments**

lambda	parameter $\lambda$ in the above equation
radius	parameter $r$ in the above equation
family	select the norm ball type, can be $l_1$ -norm, $l_2$ -norm, and $l_\infty$ -norm.
input	input $x$ in the above equation

**Details**

Take  $x$  as input,  $\lambda$  and  $r$  as parameters. Calculate  $\lambda P_{B_{\|\cdot\|_*}[0,r]}(x/\lambda)$  for a given norm ball type.

**Value**

projection  $\lambda P_{B_{\|\cdot\|_*}[0,r]}(x/\lambda)$

**Author(s)**

D.Wang and W.J.Braun

**Examples**

```
set.seed(1234567)
family <- "norm1"
temp_p1 <- rep(10, 100)
projection_nb(3, 1, family=family, temp_p1)
```

---

relsharpen

*Ridge/Enet/LASSO Sharpening via the penalty matrix.*


---

**Description**

This is a data sharpening function to remove roughness, prior to use in local polynomial regression.

**Usage**

```
relsharpen(x, y, h, alpha, p=2, M=51)
```

**Arguments**

x	numeric vector of equally spaced x data. Missing values are not accepted.
y	vector of y data. Missing values are not accepted.
h	the kernel bandwidth smoothing parameter.
alpha	the elasticnet mixing parameter vector, with alpha in [0,1].
p	the order of the polynomial regression.
M	the length of the constraint points.

**Details**

Note that the predictor values are assumed to be equally spaced.

**Value**

numeric matrix of sharpened responses, with each column corresponding to different values of alpha

**Author(s)**

D.Wang

**Examples**

```

x<-seq(0,10,length=100)
g <- function(x) sin(x)
y<-g(x)+rnorm(100)
ys<-relsharpen(x, y, dpill(x,y), alpha=c(0.2,0.8), p=2, M=51)
y.lp2<-locpoly(x,ys[,1],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp8<-locpoly(x,ys[,2],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp<-locpoly(x,y,bandwidth=dpill(x,y),degree=1,gridsize=100)
curve(g,x,xlim=c(0,10))
lines(y.lp2,col=2)
lines(y.lp8,col=3)
lines(y.lp,col=5)
norm(as.matrix(g(x) - y.lp2$y),type="2")
norm(as.matrix(g(x) - y.lp8$y),type="2")
norm(as.matrix(g(x) - y.lp$y),type="2")

```

RELsharpening

*Ridge/Enet/LASSO Sharpening via the mean/local polynomial regression with large bandwidth/linear regression.*

**Description**

This is a function to shrink responses towards their mean/estimations of local polynomial regression with large bandwidth/estimations of linear regression as a form of data sharpening to remove roughness, and reduce the bias (when "combine=TRUE"), prior to use in local polynomial regression.

**Usage**

```
RELsharpening(x,y,alpha,type,bigh,hband,combine)
```

**Arguments**

x	numeric vector of equally spaced x data. Missing values are not accepted.
y	vector of y data. Missing values are not accepted.
alpha	the elasticnet mixing parameter vector, with alpha in [0,1].
type	The type of the base line. In total, we have three types: "mean", "big_h", and "linear".
bigh	the kernel bandwidth smoothing parameter.
hband	the kernel bandwidth smoothing parameter, which will be used in the residual sharpening method.
combine	Should the smoother combined with residual method or not, default=FALSE.

**Details**

Note that the predictor values are assumed to be equally spaced.

**Value**

numeric matrix of sharpened responses, with each column corresponding to different values of alpha

**Author(s)**

D.Wang

**Examples**

```
x<-seq(0,10,length=100)
g <- function(x) sin(x)
y<-g(x)+rnorm(100)
ys<-RELsharpening(x, y,alpha=c(0.2,0.8),"big_h", dpill(x,y)*4, dpill(x,y),combine=TRUE)
y.lp2<-locpoly(x,ys[,1],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp8<-locpoly(x,ys[,2],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp<-locpoly(x,y,bandwidth=dpill(x,y),degree=1,gridsize=100)
curve(g,x,xlim=c(0,10))
lines(y.lp2,col=2)
lines(y.lp8,col=3)
lines(y.lp,col=5)
norm(as.matrix(g(x) - y.lp2$y),type="2")
norm(as.matrix(g(x) - y.lp8$y),type="2")
norm(as.matrix(g(x) - y.lp$y),type="2")
```

---

relsharp\_bigh

*Ridge/Enet/LASSO Sharpening via the local polynomial regression with large bandwidth.*

---

**Description**

This is a function to shrink responses towards their estimations of local polynomial regression with large bandwidth as a form of data sharpening to remove roughness, prior to use in local polynomial regression.

**Usage**

```
relsharp_bigh(x, y, alpha, bigh)
```

**Arguments**

x                    numeric vector of equally spaced x data. Missing values are not accepted.  
y                    vector of y data. Missing values are not accepted.  
alpha                the elasticnet mixing parameter vector, with alpha in [0,1].  
bigh                 the kernel bandwidth smoothing parameter.

**Details**

Note that the predictor values are assumed to be equally spaced.

**Value**

numeric matrix of sharpened responses, with each column corresponding to different values of alpha

**Author(s)**

D.Wang

**Examples**

```
x<-seq(0,10,length=100)
g <- function(x) sin(x)
y<-g(x)+rnorm(100)
ys<-relsharp_bigh(x, y,alpha=c(0.2,0.8), dpill(x,y)*4)
y.lp2<-locpoly(x,ys[,1],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp8<-locpoly(x,ys[,2],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp<-locpoly(x,y,bandwidth=dpill(x,y),degree=1,gridsize=100)
curve(g,x,xlim=c(0,10))
lines(y.lp2,col=2)
lines(y.lp8,col=3)
lines(y.lp,col=5)
norm(as.matrix(g(x) - y.lp2$y),type="2")
norm(as.matrix(g(x) - y.lp8$y),type="2")
norm(as.matrix(g(x) - y.lp$y),type="2")
```

---

relsharp_bigh_c	<i>Ridge/Enet/LASSO Sharpening via the local polynomial regression with large bandwidth and then applying the residual sharpening method.</i>
-----------------	---

---

**Description**

This is a function to shrink responses towards their estimations of local polynomial regression with large bandwidth and then apply residual sharpening as a form of data sharpening to remove roughness, prior to use in local polynomial regression.

**Usage**

```
relsharp_bigh_c(x, y, alpha, bigh, hband)
```

**Arguments**

x	numeric vector of equally spaced x data. Missing values are not accepted.
y	vector of y data. Missing values are not accepted.
alpha	the elasticnet mixing parameter vector, with alpha in [0,1].
bigh	the kernel bandwidth smoothing parameter.
hband	the kernel bandwidth smoothing parameter, which will be used in the residual sharpening method.

**Details**

Note that the predictor values are assumed to be equally spaced.

**Value**

numeric matrix of sharpened responses, with each column corresponding to different values of alpha

**Author(s)**

D.Wang

**Examples**

```
x<-seq(0,10,length=100)
g <- function(x) sin(x)
y<-g(x)+rnorm(100)
ys<-relsharp_bigh_c(x, y,alpha=c(0.2,0.8), dpill(x,y)*4, dpill(x,y))
y.lp2<-locpoly(x,ys[,1],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp8<-locpoly(x,ys[,2],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp<-locpoly(x,y,bandwidth=dpill(x,y),degree=1,gridsize=100)
curve(g,x,xlim=c(0,10))
lines(y.lp2,col=2)
lines(y.lp8,col=3)
lines(y.lp,col=5)
norm(as.matrix(g(x) - y.lp2$y),type="2")
norm(as.matrix(g(x) - y.lp8$y),type="2")
norm(as.matrix(g(x) - y.lp$y),type="2")
```

---

relsharp\_linear

*Ridge/Enet/LASSO Sharpening via the linear regression.*


---

**Description**

This is a function to shrink responses towards their estimations of linear regression as a form of data sharpening to remove roughness, prior to use in local polynomial regression.

**Usage**

```
relsharp_linear(x, y, alpha)
```

**Arguments**

`x` numeric vector of equally spaced `x` data. Missing values are not accepted.  
`y` vector of `y` data. Missing values are not accepted.  
`alpha` the elasticnet mixing parameter vector, with `alpha` in  $[0,1]$ .

**Details**

Note that the predictor values are assumed to be equally spaced.

**Value**

numeric matrix of sharpened responses, with each column corresponding to different values of `alpha`

**Author(s)**

D.Wang

**Examples**

```
x<-seq(0,10,length=100)
g <- function(x) sin(x)
y<-g(x)+rnorm(100)
ys<-relsharp_linear(x, y,alpha=c(0.2,0.8))
y.lp2<-locpoly(x,ys[,1],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp8<-locpoly(x,ys[,2],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp<-locpoly(x,y,bandwidth=dpill(x,y),degree=1,gridsize=100)
curve(g,x,xlim=c(0,10))
lines(y.lp2,col=2)
lines(y.lp8,col=3)
lines(y.lp,col=5)
norm(as.matrix(g(x) - y.lp2$y),type="2")
norm(as.matrix(g(x) - y.lp8$y),type="2")
norm(as.matrix(g(x) - y.lp$y),type="2")
```

---

relsharp_linear_c	<i>Ridge/Enet/LASSO Sharpening via the linear regression and then applying the residual sharpening method.</i>
-------------------	--

---

**Description**

This is a function to shrink responses towards their estimations of linear regression and then apply residual sharpening as a form of data sharpening to remove roughness, prior to use in local polynomial regression.

**Usage**

```
relsharp_linear_c(x, y, alpha, hband)
```

**Arguments**

x	numeric vector of equally spaced x data. Missing values are not accepted.
y	vector of y data. Missing values are not accepted.
alpha	the elasticnet mixing parameter vector, with alpha in [0,1].
hband	the kernel bandwidth smoothing parameter, which will be used in the residual sharpening method.

**Details**

Note that the predictor values are assumed to be equally spaced.

**Value**

numeric matrix of sharpened responses, with each column corresponding to different values of alpha

**Author(s)**

D.Wang

**Examples**

```
x<-seq(0,10,length=100)
g <- function(x) sin(x)
y<-g(x)+rnorm(100)
ys<-relsharp_linear_c(x, y,alpha=c(0.2,0.8),dpill(x,y))
y.lp2<-locpoly(x,ys[,1],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp8<-locpoly(x,ys[,2],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp<-locpoly(x,y,bandwidth=dpill(x,y),degree=1,gridsize=100)
curve(g,x,xlim=c(0,10))
lines(y.lp2,col=2)
lines(y.lp8,col=3)
lines(y.lp,col=5)
norm(as.matrix(g(x) - y.lp2$y),type="2")
norm(as.matrix(g(x) - y.lp8$y),type="2")
norm(as.matrix(g(x) - y.lp$y),type="2")
```

---

relsharp\_mean

*Ridge/Enet/LASSO Sharpening via the Mean*


---

**Description**

This is a function to shrink responses towards their mean as a form of data sharpening to remove roughness, prior to use in local polynomial regression.

**Usage**

```
relsharp_mean(y, alpha)
```

**Arguments**

`y` vector of y data. Missing values are not accepted.  
`alpha` The elasticnet mixing parameter vector, with alpha in [0,1].

**Details**

Note that the predictor values are assumed to be equally spaced.

**Value**

numeric matrix of sharpened responses, with each column corresponding to different values of alpha

**Author(s)**

D.Wang

**Examples**

```
x<-seq(0,10,length=100)
g <- function(x) sin(x)
y<-g(x)+rnorm(100)
ys<-relsharp_mean(y,alpha=c(0.2,0.8))
y.lp2<-locpoly(x,ys[,1],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp8<-locpoly(x,ys[,2],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp<-locpoly(x,y,bandwidth=dpill(x,y),degree=1,gridsize=100)
curve(g,x,xlim=c(0,10))
lines(y.lp2,col=2)
lines(y.lp8,col=3)
lines(y.lp,col=5)
norm(as.matrix(g(x) - y.lp2$y),type="2")
norm(as.matrix(g(x) - y.lp8$y),type="2")
norm(as.matrix(g(x) - y.lp$y),type="2")
```

---

relsharp\_mean\_c

*Ridge/Enet/LASSO Sharpening via the Mean and then applying the residual sharpening method.*

---

**Description**

This is a function to shrink responses towards their mean and then apply residual sharpening as a form of data sharpening to remove roughness, prior to use in local polynomial regression.

**Usage**

```
relsharp_mean_c(x, y, alpha, hband)
```

**Arguments**

x	numeric vector of equally spaced x data. Missing values are not accepted.
y	vector of y data. Missing values are not accepted.
alpha	the elasticnet mixing parameter vector, with alpha in [0,1].
hband	the kernel bandwidth smoothing parameter, which will be used in the residual sharpening method.

**Details**

Note that the predictor values are assumed to be equally spaced.

**Value**

numeric matrix of sharpened responses, with each column corresponding to different values of alpha

**Author(s)**

D.Wang

**Examples**

```
x<-seq(0,10,length=100)
g <- function(x) sin(x)
y<-g(x)+rnorm(100)
ys<-relsharp_mean_c(x, y,alpha=c(0.2,0.8), dpill(x,y))
y.lp2<-locpoly(x,ys[,1],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp8<-locpoly(x,ys[,2],bandwidth=dpill(x,y),degree=1,gridsize=100)
y.lp<-locpoly(x,y,bandwidth=dpill(x,y),degree=1,gridsize=100)
curve(g,x,xlim=c(0,10))
lines(y.lp2,col=2)
lines(y.lp8,col=3)
lines(y.lp,col=5)
norm(as.matrix(g(x) - y.lp2$y),type="2")
norm(as.matrix(g(x) - y.lp8$y),type="2")
norm(as.matrix(g(x) - y.lp$y),type="2")
```

---

testfun

*Functions for Testing Purposes*

---

**Description**

Functions that can be used in simulations to test the effectiveness of the sharpening procedures.

**Usage**

```
testfun(x, k)
```

**Arguments**

- x                    numeric vector
- k                    a numeric constant that controls the height of the peak of the test function; if missing, a periodic function is supplied

**Value**

numeric vector of function output

**Author(s)**

D.Wang

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